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## **PROGRAM OUTCOME (PO)-**

**PO1: Basic and Discipline specific knowledge-** Apply knowledge of basic mathematics, science and engineering fundamentals and engineering specialization to solve the engineering problems.

**PO2: Problem Analysis-** Identify and analyze well defined engineering problems using codified standard methods.

**PO3: Design/ development of solutions-** Design solutions for well-defined technical problems and assist with the design of systems components or processes to meet specified needs.

**PO4: Engineering Tools, Experimentation and Testing-** Apply modern engineering tools and appropriate technique to conduct standard tests and measurements.

**PO5: Engineering Practices for society, sustainability and environment-** Apply appropriate technology in context of society, sustainability, environment and ethical practices.

**PO6: Project Management-** Use engineering management principles individually, as a team member or a leader to manage projects and effectively communicate about well-defined engineering activities.

**PO7: Life-long learning-** Ability to analyze individual needs and engage in updating in the context of technological changes.

## **COURSE OUTCOME**

After the completion of the course the students will be able to

C01-Identify the elements of communication system and explain them.

C02-Compare the performance of AM, FM and PM schemes and describe the working of modulator and demodulator circuits.

C03-Analyze and explain the working of transmitter and receiver circuits.

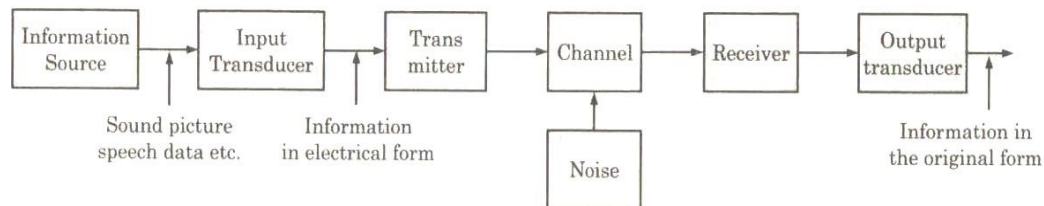
C04-Differentiate the types of pulse modulation techniques and explain the working of PAM, PWM, PPM & PCM modulator and demodulator circuits.

C05-Analyze the performance of various digital modulation techniques.

## **UNIT-1: ELEMENTS OF COMMUNICATION SYSTEMS**

### **1.1 ELEMENTS OF COMMUNICATION SYSTEM-**

Communication involves the transmission of information from one point to another.



*Block diagram of a communication system*

#### **INFORMATION SOURCE-**

Communication system serves to communicate a message or information. This message originates in the information source. There can be various messages in the form of words, groups of words, code, symbols, sound signals etc.

#### **INPUT TRANSDUCER-**

A transducer is a device which converts one form of energy into another form. The message from the information source may or may not be electrical in nature. When the message produced by the information source is not electrical in nature, an input transducer is used to convert it into a time varying electrical signal.

#### **TRANSMITTER-**

The function of the transmitter is to process the electrical signal from different aspects. Inside the transmitter, signal processing such as restriction of range of audio frequencies, amplification and modulation are achieved.

#### **THE CHANNEL AND THE NOISE-**

There are two types of channels, namely point to point channels and broadcast channels. Examples of point to point channels are wire lines, microwave links and optical fibers. Wire lines operate by guided electromagnetic waves and they are used for local telephone transmission. Microwave links are used in long distance telephone transmission. Optical fibers are used in optical communication. On the other hand the broadcast channels provide a capability where several receiving stations can be reached simultaneously from a single transmitter. During the

process of transmission and reception the signal gets distorted due to noise introduced in the system. Noise is an unwanted signal which tends to interfere with the required signal. Noise may interfere with signal at any point in a communication system.

## RECEIVER-

The main function of the receiver is to reproduce the message signal in electrical form from the distorted received signal. This reproduction of the original signal is accomplished by a process known as the demodulation. Demodulation is the reverse process of modulation carried out in transmitter.

**DESTINATION-**

Destination is the final stage which is used to convert an electrical message signal into its original form.

## 1.2 SOURCE OF INFORMATION & COMMUNICATION CHANNELS

**SOURCE OF INFORMATION-**

Some of the important source of information in the communication environment given below-

- (i) Speech                      (iii) Picture  
(ii) Music                      (iv) Computer data

A source of information is basically a signal which carries the information.

**Signal-**

A signal may be defined as the single valued function of time. Time plays the role of an independent variable. This means that at every instant of time, the signal has a unique value.

The signals may be classified as:

**(i) Speech**

Speech involves transfer of information from the speaker to the listener. Such a transfer of information takes place in following three stages:

- (1) Production
- (2) Propagation and
- (3) Perception

(ii) **Music signal-**

It is originated from the instruments such as the piano, violin, flute etc. Music signal has following two possible structure:

(1) Melodic structure

(2) Harmonic structure

### **(iii) Picture**

The picture can be either static or dynamic. Examples of static picture is the picture sent by fax machine and that of a dynamic picture is the one produced on T.V.

### **(iv) Computer Data**

Personal computers are used for electronic mail, exchange of software, and sharing of resources.

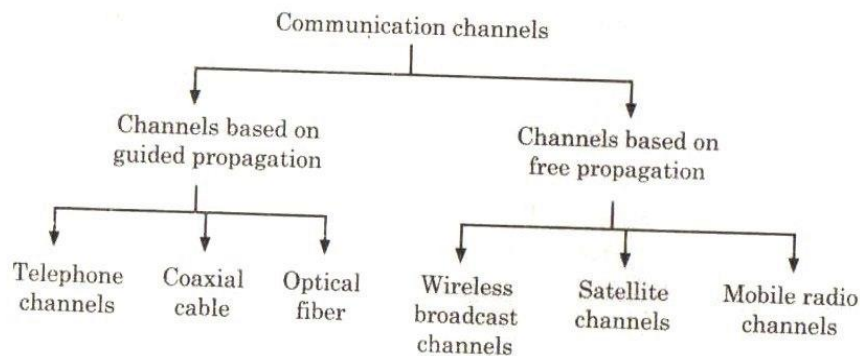
## **COMMUNICATION CHANNEL-**

The medium over which the information is passed from the transmitter to the receiver is called as a communication channel. Depending on the mode of transmission, the communication channels classified in to two categories.

(i) Guided medium

(ii) Unguided medium

The classification of channels has been shown below:

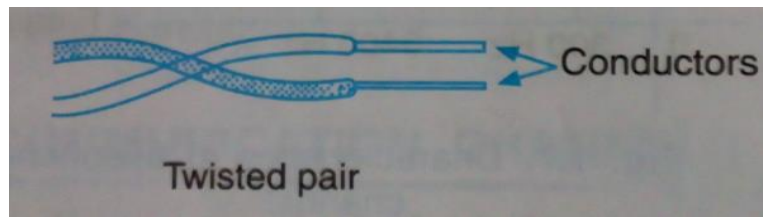


*Classification of communication channels*

## **Guided Medium-**

Telephone Channels-

It is designed for providing service to voice signals such as telephones. The telephone channels are also used for the worldwide internet connection. Therefore, telephone channel is the best possible option for the data transmission over long distances.

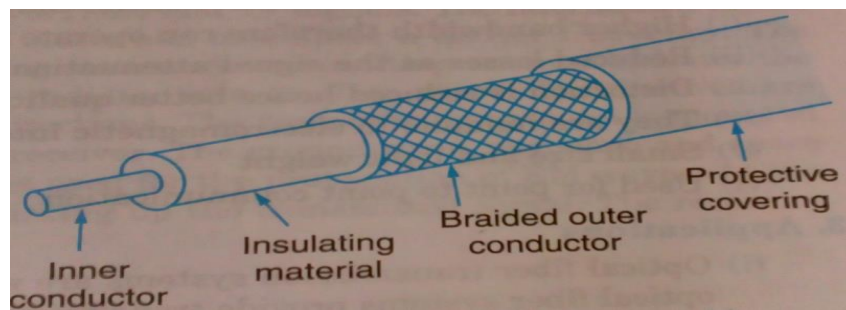


The telephone channels are built using the twisted pair of wires. A twisted pair consists of two insulated conductor twisted together in the spiral form. It can be shielded or unshielded.

The un-shielded twisted pair cables are very cheap and easy to install. However, they are badly affected by the noise interference.

The noise immunity can be improved by using shielded twisted pair cable.

Co-axial cable-

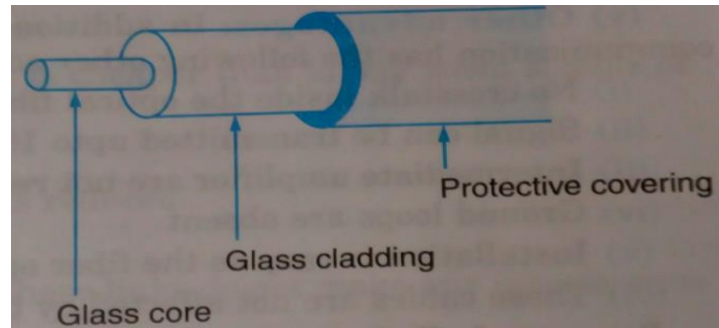


It consists of two concentric conductors separated by a dielectric material. The external conductor is metallic braid and used for the purpose of shielding. The co-axial cable may contain one or more co-axial pairs.

One more application is Ethernet LAN using the co-axial cable.

The co-axial cable is used for its large bandwidth and high noise immunity.

Optical fiber cables-



It consists of an inner glass core surrounded by a glass cladding which has a lower refractive index.

Digital signals are transmitted in the form of intensity-modulated light signal which is trapped in the glass core.

Light is launched into the fiber using a light source such as a LED or laser.

It is detected on the other side using a photo detector such as a phototransistor.

### **Unguided Medium-**

#### Wireless Broadcast channel-

These channels are used for the transmission of radio and TV signals.

The information signal which represents the speech, music etc. modulates a carrier frequency.

The carrier frequency is different for every transmitting station.

A transmitting antenna radiates the modulated signal in the form of electromagnetic radiation into the free space.

These waves are radiated in all directions or in some specified directions.

The transmitting antenna is mounted on a tower or a hill in order to reach the farther receiver.

The ground wave, sky wave and space wave are three types of propagation techniques used for the propagation of EM waves.

At the receiving end, the receiving antenna is used for picking up the transmitted signal.

#### Satellite Channels-



Satellite microwave systems transmits signals between directional parabolic antennas.

They use low gigahertz frequencies and line of sight communication.

These systems use satellites which are in the geostationary orbit (36000 km above the earth).

The satellites act as repeaters with receiving antennas, transponder and transmitting antenna.

Satellite microwave systems can reach the most remote places on earth and communicate with mobile devices.

In this method signal is sent through cable media to an antenna which beams the signal to the satellite, the satellite then transmits the signal back to another location on earth.

### Mobile Radio Channels-

In mobile communication, the sender and the receiver both are allowed to move with respect to each other.

The radio propagation takes place due to scattering of EM waves from the surface of the surrounding buildings and diffraction over and around them. Hence, the transmitted energy reaches the receiver via multiple paths. This is called as multi path communication.

The signals taking different paths will have to travel different path lengths. So, they have different phase shifts when they reach the receiver.

The total signal strength at the receiver is equal to the vector sum of all the signals.

Therefore it keeps changing continuously. Hence, mobile channels are called as the linear time varying channels and it is statistical in nature.

### **1.3 CLASSIFICATION OF COMMUNICATION SYSTEM-**

➤ Depending upon the message signal, communication system may be classified as-

- i) Analog communication system
- ii) Digital communication system

Analog communication system-

It is a type of communication in which the message or information signal to be transmitted is analog in nature. This means that in analog communication the modulating signal is an analog signal.

Digital communication system-

It is a type of communication in which the message signal to be transmitted is digital in nature. This means that digital communication involves the transmission of information in digital form.

➤ Based on communication channel used, communication system may be classified as-

- i) Line communication system
- ii) Radio communication system

Line communication system-

There is a physical link present between the transmitter and receiver in line communication system.

Ex- Landline telephony is purely a line communication system

Radio communication system-

In this system there is no link present between transmitter and receiver.

Ex.- Radio broadcast

➤ Based on transmission mode, communication system may be classified as-

- i) Simplex communication system
- ii) Duplex communication system

Simplex communication system-

In this communication system, one way transmission is used. Ex.- TV transmission

Duplex communication system-

In this communication system, two way transmission is used. Ex.- Telephony system.

## **1.4 MODULATION PROCESS, NEED OF MODULATION AND CLASSIFY MODULATION PROCESS**

## **MODULATION:**

Modulation is the process in which parameters (i.e, Amplitude, Phase and Frequency) of the carrier signal changes according to the message signal or modulating signal.

## **NEED OF MODULATION:**

### 1) Practicality of Antenna-

The voice frequencies in the band of 20HZ to 20KHZ, For the efficient transmission and reception of radio frequency signals. The antenna length 'L' required in terms of wavelength

$$L = \frac{\lambda}{4}$$
$$= \frac{C}{4f} \quad (C = 3 \times 10^8 \text{ m/sec})$$

Where  $\lambda$  = wavelength

C = Speed of light

f = Frequency

### 2) To remove Interference

### 3) Reduction of noise

### 4) Multiplexing-

- Simultaneously transmission of multiple message over a single channel is known as multiplexing.
- If it transmits without modulation, the different message signal over a single channel will interfere with one another.
- Multiplexing helps in transmitting numbers of message signal simultaneously over a single channel & therefore a number of channel needed will be less.

## **CLASSIFY MODULATION PROCESS-**

### Continuous wave modulation-

When the carrier wave is continuous in nature, the modulation process is known as continuous wave modulation or analog modulation.

### Pulse modulation-

When the carrier wave is a pulse type waveform, the modulation process is known as pulse modulation. In pulse modulation, the carrier consists of a periodic sequence of rectangular pulses.

## **ANALOG AND DIGITAL SIGNALS-**

- The analog signal is that type of signal which varies smoothly and continuously with time.

- This means that analog signals are defined for every value of time and they take on continuous values in a given time interval.
- An alternative form of signal representation is that of a sequence of numbers, each number representing the signal magnitude at an instant of time. The resulting signal is called a digital signal.

## **1.5 CONVERSION OF ANALOG SIGNALS TO DIGITAL SIGNALS-**

There are three steps for conversion process.

1. The signal is sampled.
2. The sampled signal is quantized.
3. The quantized signal is digitally coded.

### **Sampling**

Sampling generally is done with a Sample-And-Hold circuit. To be able to reconstruct the signal we must consider the Sampling Theorem which says that a sampling frequency twice of the highest frequency. In a simple way sampling can be defined as the process of taking samples from the continuous time function  $x(t)$  and for the signal to reconstruct we must consider the sampling theorem which states that the sampling frequency must be always greater than or equal to twice the highest frequency.

### **Quantization**

Quantization is the process of taking a continuous voltage signal and mapping it to a discrete number of voltage levels. The number of voltage levels affects the quantization noise that occurs. Since digital computers are binary in nature, the number of quantization levels is usually a power of 2, i.e.,

$$N=2^n$$

where  $n$  is the number of quantization bits.

### **Encoding**

Encoding is the process of converting the quantized signals into a digital representation. This encoding is performed by giving each quantization level a unique label. For instance, if four bits are used, the lowest level may be (in binary) 0000, and the next highest level 0001, etc.

## **1.6 BASIC CONCEPT OF SIGNALS & SIGNALS CLASSIFICATION**

### **BASIC CONCEPT OF SIGNALS-**

A signal is a physical quantity which varies with respect to time, space and contains some information from source to destination. The term signal includes audio, video, speech, image etc.

The signals are functions of one or more variables and the systems respond to an input signal by producing an output signal.

### **CLASSIFICATION OF SIGNAL-**

Signals are classified into the following categories:

- 1) Continuous Time and Discrete Time Signals
- 2) Deterministic and Non-deterministic Signals
- 3) Even and Odd Signals
- 4) Periodic and Aperiodic Signals
- 5) Energy and Power Signals
- 6) Real and Imaginary Signals

#### **Continuous Time and Discrete Time Signals-**

Continuous signal-

A signal is said to be continuous when it is defined for all instants of time.

Discrete signal-

A signal is said to be discrete when it is defined at only discrete instants of time.

#### **Deterministic and Non-deterministic Signals-**

Deterministic signal-

A signal is said to be deterministic if there is no uncertainty with respect to its value at any instant of time. Or, signals which can be defined exactly by a mathematical formula are known as deterministic signals.

Non-Deterministic signal-

A signal is said to be non-deterministic if there is uncertainty with respect to its value at some instant of time. Non-deterministic signals are random in nature hence they are called random signals. Random signals cannot be described by a mathematical equation.

#### **Even and Odd Signals-**

Even signals-

A signal is said to be even when it satisfies the condition  $x(t) = x(-t)$ .

Odd signals-

A signal is said to be odd when it satisfies the condition  $x(t) = -x(-t)$ .

#### **Periodic and Aperiodic Signals-**

Periodic signals-

A signal is said to be periodic if it satisfies the condition  $x(t) = x(t + T)$  or  $x(n) = x(n + N)$ .

Where

$T$  = fundamental time period,

$1/T = f$  = fundamental frequency.

Aperiodic signals-

The above signal will repeat for every time interval  $T_0$  hence it is periodic with period  $T_0$ .

#### **Energy and Power Signals-**

Energy signals-

A signal is said to be energy signal when it has finite energy.

Power signals-

A signal is said to be power signal when it has finite power.

### **Real and complex signals-**

Real signals-

A signal  $x(t)$  is a real signal if its value is a real number.

Complex signals-

A signal  $x(t)$  is a complex signal if its value is a complex number.

## **1.7 BANDWIDTH LIMITATION-**

While designing a communication system, an engineer generally faces several limitations.

These are:

- 1) Noise limitation
- 2) Bandwidth limitation
- 3) Equipment limitation

Noise Limitation-

The noise may be defined as an unwanted form of energy which tend to interfere with the transmission and reception of the desired signals in a communication system. The noise cannot be eliminated completely. However the effect of noise on desired signals can be minimized.

The noise limits our ability to identify the intended or desired message correctly.

Bandwidth Limitation-

The bandwidth limitation is another major limitation in a communication system. The frequency range needed for a particular transmission is known as bandwidth.

This band of frequencies or bandwidth for a particular transmission is also called channel and it is always allocated by some international regulatory agencies. This type of regulation is essential to avoid interference among the signals having same frequency.

The information theory states that the greater is the transmission bandwidth of a communication system, the more is the information can be transmitted.

Equipment Limitation-

The noise and bandwidth limitation dictate theoretical limit may not be realized in a practical system due to equipment limitations.

## **UNIT-2: AMPLITUDE (LINEAR) MODULATION SYSTEM**

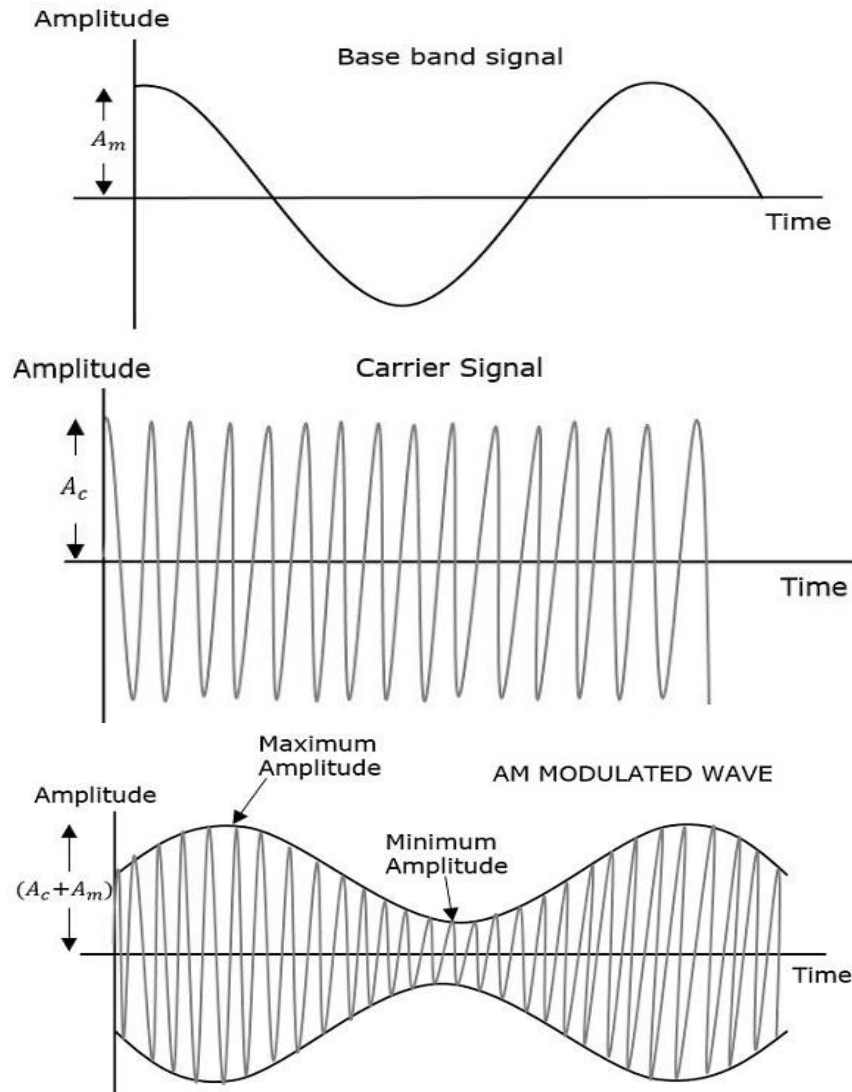
### **2.1 AMPLITUDE MODULATION & DERIVE THE EXPRESSION FOR AMPLITUDE MODULATION SIGNAL, POWER RELATION IN AM WAVE & FIND MODULATION INDEX**

#### **AMPLITUDE MODULATION AND DERIVE THE EXPRESSION FOR AMPLITUDE MODULATED SIGNAL:-**

Amplitude modulation may be defined as a system in which the maximum amplitude of the carrier wave is proportional to the instantaneous value of the modulating signal.

A continuous-wave goes on continuously without any intervals and it is the baseband message signal, which contains the information. This wave has to be modulated.

According to the standard definition, "The amplitude of the carrier signal varies in accordance with the instantaneous amplitude of the modulating signal." Which means, the amplitude of the carrier signal containing no information varies as per the amplitude of the signal containing information, at each instant. This can be well explained by the following figures.



The first figure shows the modulating wave, which is the message signal. The next one is the carrier wave, which is a high frequency signal and contains no information. While, the last one is the resultant modulated wave.

It can be observed that the positive and negative peaks of the carrier wave, are interconnected with an imaginary line. This line helps recreating the exact shape of the modulating signal. This imaginary line on the carrier wave is called as **Envelope**. It is the same as that of the message signal.

### Mathematical Expressions

Modulating signal-  $x(t) = A_m \cos \omega_m t$

Carrier Signal,  $C(t) = A_c \cos \omega_c t$



Where,  $A_m$  and  $A_c$  are the amplitude of the modulating signal and the carrier signal respectively.  
 $w_m$  and  $w_c$  are the frequency of the modulating signal and the carrier signal.

### Modulated Signal-

$$\begin{aligned}
 m(t) &= [A_c + x(t)] \cos w_c t \\
 &= (A_c + A_m \cos w_m t) \cos w_c t \\
 &= A_c \left( 1 + \frac{A_m}{A_c} \cos w_m t \right) \cos w_c t \\
 &= A_c (1 + m_a \cos w_m t) \cos w_c t \quad \left( \frac{A_m}{A_c} = m_a \right) \\
 &= A_c \cos w_c t + A_c m_a \cos w_m t \cos w_c t \\
 &= A_c \cos w_c t + \frac{A_c m_a}{2} [\cos (w_c - w_m) t + \cos (w_c + w_m) t] \\
 &= A_c \cos w_c t + \frac{A_c m_a}{2} \cos (w_c - w_m) t + \frac{A_c m_a}{2} \cos (w_c + w_m) t
 \end{aligned}$$

### Bandwidth-

$$f_{max} = w_c + w_m$$

$$f_{min} = w_c - w_m$$

$$\text{Bandwidth} = f_{max} - f_{min}$$

$$= (w_c + w_m) - (w_c - w_m)$$

$$= w_c + w_m - w_c + w_m$$

$$= 2w_m$$

### MODULATION INDEX

Modulation Index-

It is the ratio of amplitude of modulating signal to the amplitude of the carrier signal. It is denoted as  $m_a$ .

$$m_a = \frac{A_m}{A_c} = \frac{\text{Maximum Amplitude of modulating signal}}{\text{Amplitude of the carrier signal}}$$

Modulation index means how much energy of the carrier wave used during modulation.

$$\text{Maximum amplitude} = A_{max} = A_c + A_m$$

$$\text{Minimum amplitude} = A_{min} = A_c - A_m$$

When,  $A_{max} + A_{min}$

$$= A_c + A_m + A_c - A_m$$

$$= 2A_c$$

$$\Rightarrow A_{max} + A_{min} = 2A_c$$

$$\Rightarrow A_c = \frac{A_{max} + A_{min}}{2}$$

When,  $A_{max} - A_{min}$

$$= A_c + A_m - A_c + A_m$$

$$= 2A_m$$

$$\Rightarrow A_{max} - A_{min} = 2A_m$$

$$\Rightarrow A_m = \frac{A_{max} - A_{min}}{2}$$

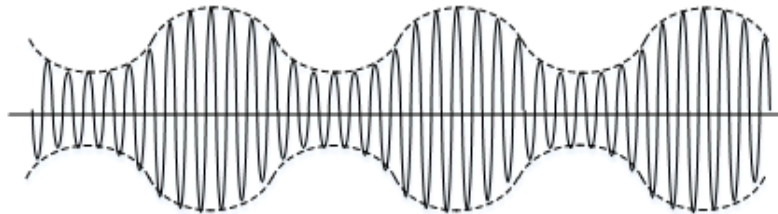
$$m_a = \frac{A_m}{A_c} = \frac{\frac{A_{max} - A_{min}}{2}}{\frac{A_{max} + A_{min}}{2}} = \frac{A_{max} - A_{min}}{A_{max} + A_{min}}$$

There are three cases of  $m_a$ .

#### Case-I

When  $A_m < A_c, m_a < 1$ . This condition is known as under modulation.

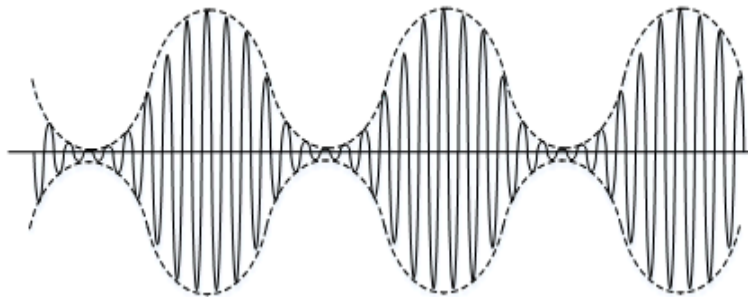
Under modulation ( $m < 1$ )



#### Case-II

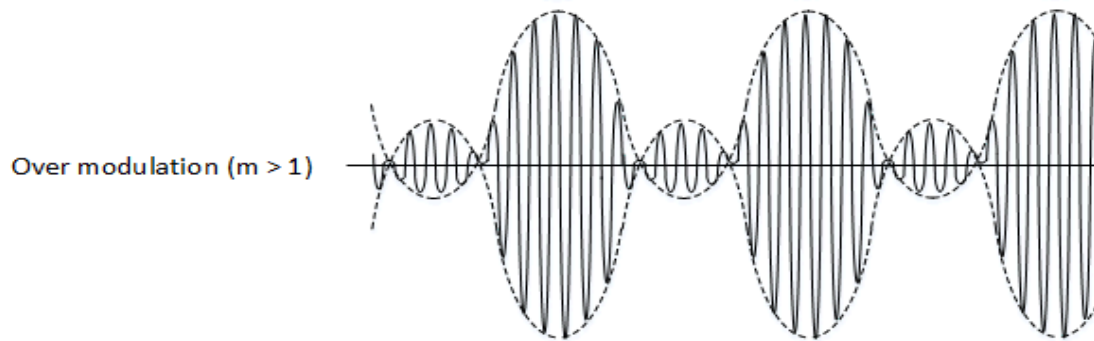
When  $A_m = A_c, m_a = 1$ . This condition is known as 100% modulation.

100 % modulation ( $m = 1$ )



#### Case-III

When  $A_m > A_c, m_a > 1$ . This condition is known as over modulation.



Questions –

- Carrier wave of frequency 1 MHz with peak voltage of 20V used to modulate a signal of frequency 1 KHz with peak voltage of 10V.  
Find out the following-
  - $\mu$
  - Frequencies of modulated signal
  - Bandwidth
- A modulating signal is  $x(t) = 10 \cos(2\pi \times 10^3 t)$  and carrier signal is  $c(t) = 50 \cos(2\pi \times 10^5 t)$ . Find out the percentage of modulation.
- What is the modulation index value if  $V_{max} = 5.9 V$  and  $V_{min} = 1.2 V$ .

**POWER RELATION IN AM WAVE:-**

$$P_t(\text{total power}) = P_c + P_{USB} + P_{LSB}$$

$$= P_c + P_s$$

$$\begin{aligned}
 P &= \frac{V^2}{R} \\
 &= \frac{(V_{rms})^2}{R} \\
 &= \frac{(V_m / \sqrt{2})^2}{R} \\
 P_c &= \frac{(A_c / \sqrt{2})^2}{R} \\
 &= \frac{A_c^2}{2R} \\
 P_{USB} &= \frac{(V_m / \sqrt{2})^2}{R}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{\left(\frac{m_a A_c}{2\sqrt{2}}\right)^2}{R} \\
 P_{USB} &= \frac{m_a^2 A_c^2}{8R} = P_{LSB} \\
 P_S &= P_{USB} + P_{LSB} \\
 &= \frac{m_a^2 A_c^2}{8R} + \frac{m_a^2 A_c^2}{8R} \\
 &= 2 \frac{m_a^2 A_c^2}{8R} = \frac{m_a^2 A_c^2}{4R}
 \end{aligned}$$

$$\begin{aligned}
 P_t &= P_c + P_s \\
 &= \frac{A_c^2}{2R} + \frac{m_a^2 A_c^2}{4R} \\
 &= \frac{A_c^2}{2R} \left[ 1 + \frac{m_a^2}{2} \right]
 \end{aligned}$$

$$P_t = P_c \left[ 1 + \frac{m_a^2}{2} \right]$$

Current Relation-

$$P = I^2 R$$

$$P_t = P_c \left[ 1 + \frac{m_a^2}{2} \right]$$

$$\Rightarrow I_t^2 R = I_c^2 R \left[ 1 + \frac{m_a^2}{2} \right]$$

$$\Rightarrow I_t^2 = I_c^2 \left[ 1 + \frac{m_a^2}{2} \right]$$

$$\Rightarrow I_t = \sqrt{I_c^2 \left[ 1 + \frac{m_a^2}{2} \right]}$$

Questions-

- 1) A 800watt carrier is modulated to a depth of 50%. Find the total power in the AM wave.
- 2) An AM broadcast radio transmitter radiates 10Kwatt of power of modulation percentage is 60%. Calculate how much of this is carrier power.

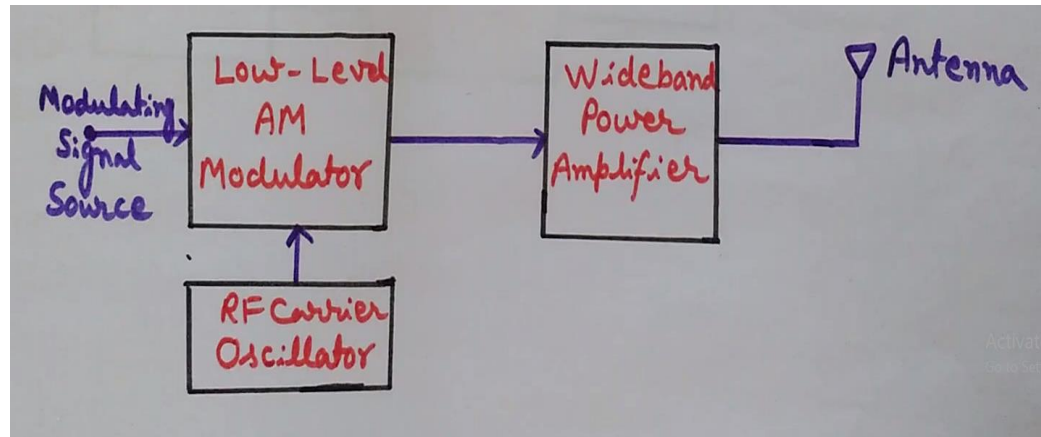
## 2.2 GENERATION OF AM WAVES-

The device which is used to generate an amplitude modulation (AM) wave is known as amplitude modulator. The methods as amplitude modulator Generation may be broadly classified as following:-

- 1) Low level AM Modulation.
- 2) High level AM Modulation.

### 1) Low Level Amplitude Modulation:-

In a low level amplitude modulation system, the modulation is done at low power level. At low power levels, a very small power is associated with the carrier signal and the modulation signal. Because of this the output power of modulation is low. Therefore the power amplifiers are required to boost the amplitude modulated signals up to the desired output level.

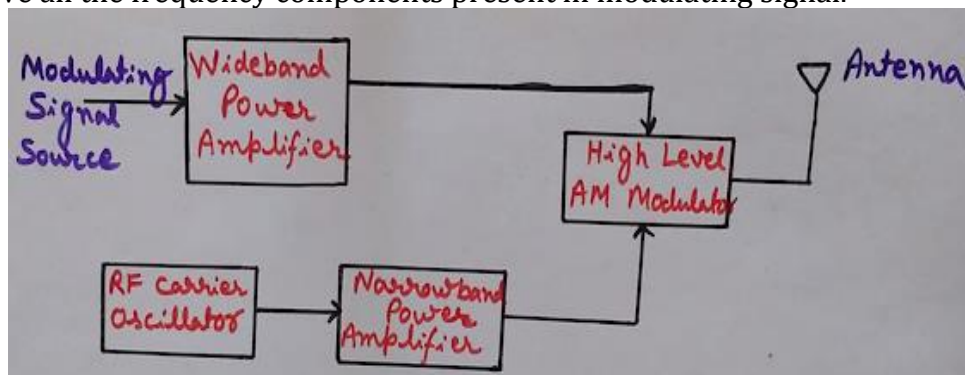


A wide band power amplifier is used just to preserve the sidebands of the modulated signal. Amplitude modulated systems, employing modulation at low power levels are also called low level amplitude modulation transmitters.

Square-law diode modulation and switching modulation are examples of low-level modulation.

### 2) High level Amplitude Modulation:-

In a high-level amplitude -modulation system, the modulation is done at high power level. Therefore, to produce amplitude modulation at these high power levels, the base band signal and the carrier signal must be at high power levels. In block diagram of figure the modulating signal and carrier signal are first power amplified and then applied to AM high level modulator. For modulating signal the wide band power amplifier is required just to preserve all the frequency components present in modulating signal.



On the other hand for carrier signal, the narrow band power amplifier is required because it is a fixed frequency signal. The collector modulation method is the example of high level modulation.

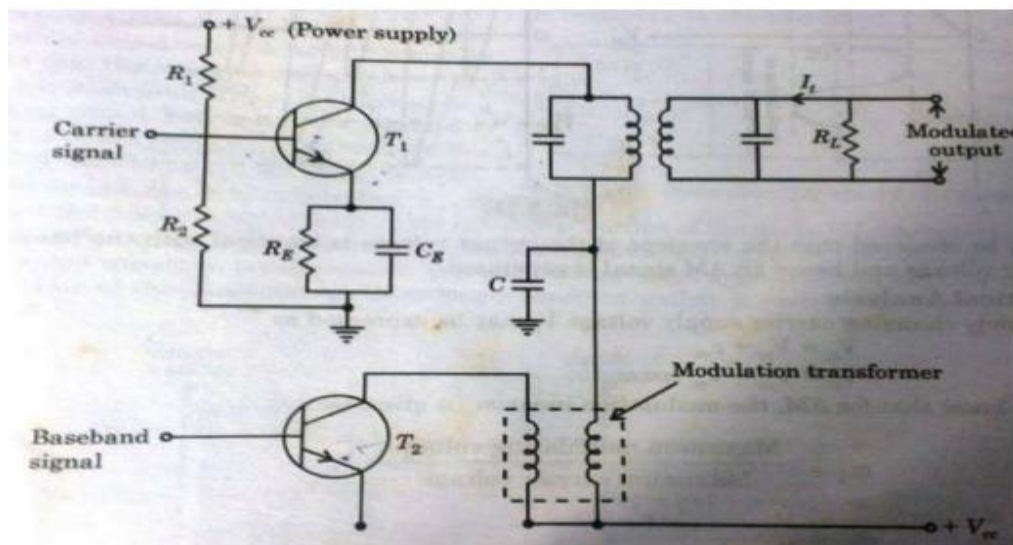
### **COLLECTOR MODULATION (LINEAR LEVEL AM MODULATION)-**

Collector modulator is a linear modulator.

The circuit consists of two transistors  $T_1$  and  $T_2$ . The transistor  $T_1$  makes a radio frequency class-C amplifier. At the base of the  $T_1$  carrier signal is applied.

The transistor  $T_2$  makes a class B amplifier, which is used to amplify the modulating signal appears across the modulation transformer. For biasing purpose voltage divider circuit is used.

A capacitor is used to isolate the modulation transformer from the high frequency carrier signal. Here double tuned circuit is used for better performance. The resonance frequency of tank circuit is equal to the carrier frequency.



Operation-

As we know class C amplifier gives 80% efficiency but more distortion. But here a high frequency carrier signal is used. So, distortion is less.

A linear relationship exists between the output tank current ( $I_t$ ) and the variable supply voltage  $V_c$ .

During absence of modulating signal, the output voltage will be an exact replica of the input voltage waveform.

So, if  $R_L$  is the resistance of the output tank circuit at resonance, then the magnitude of the magnitude of the output voltage is

$$R_L I_t \cong V_{cc}$$

But, if a modulating signal voltage appears across the modulating transformer, this signal will be added to the carrier supply voltage  $V_{cc}$ .

$$\text{So, } V_c = V_{cc} + V_m$$

$$\text{Where } V_m = V_m \cos \omega_m t$$

$V_{cc}$  = amplitude of the carrier signal

Carrier signal represented as

$$V_c = V_{cc} \cos \omega_c t$$

*The modulated signal is*

$$V_o = (V_{cc} + V_m \cos \omega_m t) \cos \omega_c t$$

$$\Rightarrow V_o = V_{cc} \left( 1 + \frac{V_m}{V_{cc}} \cos \omega_m t \right) \cos \omega_c t$$

$$\Rightarrow V_o = V_{cc} (1 + m_a \cos \omega_m t) \cos \omega_c t$$

### **DEMODULATION OF AM WAVE:-**

The process of extracting a modulating signal from the modulated signal is called demodulation. The devices used for demodulation are called demodulators.

Types of detector (1) square-law detectors

(2) Envelope detectors

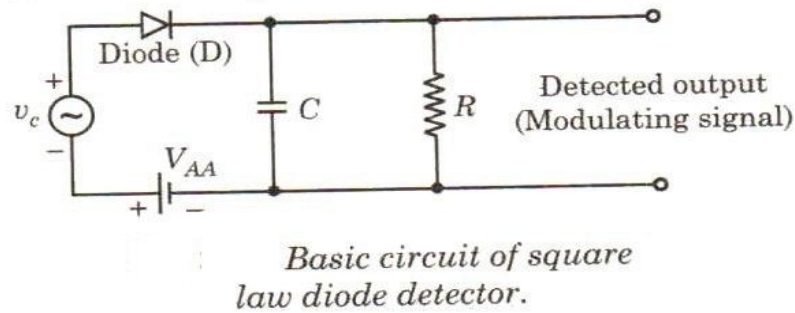
(3) PLL AM detector

AM signal with large carrier are detected by using the envelope detector uses the circuit which extracts the envelope of the am wave but detected by using square-law detectors.

## **2.3 DEMODULATION OF AM WAVES**

### **SQUARE-LAW DETECTORS/LINEAR DIODE DETECTOR:-**

The Square-Law Detector ckt is used for detecting modulated signal of small magnitude, so that operating region may be restricted to the non-linear portion of the v-characteristics of the device it may be observed that the circuit is very similar to the square law modulator. The only difference is that in square law modulator the filter used is a band pass filter where in a square law detector, a low pass filter is used.



In the circuit, the dc supply voltage  $V_{AA}$  is used to get the fixed operating point in the non-linear portion of the diode V-I characteristics. Since, the operation is limited to the non-linear region of the diode characteristics, the lower half portion of the modulated wave form is compressed. This produces envelope applied distortion. Due to this the average value of the diode current is no longer constant, rather it varies with time.

This distorted output diode current is expressed by

$$I = av + bv^2$$

$v$  is the i/p modulated voltage

AM wave is expressed as

$$v = A (1 + m_a \cos \omega_m t) \cos \omega_c t$$

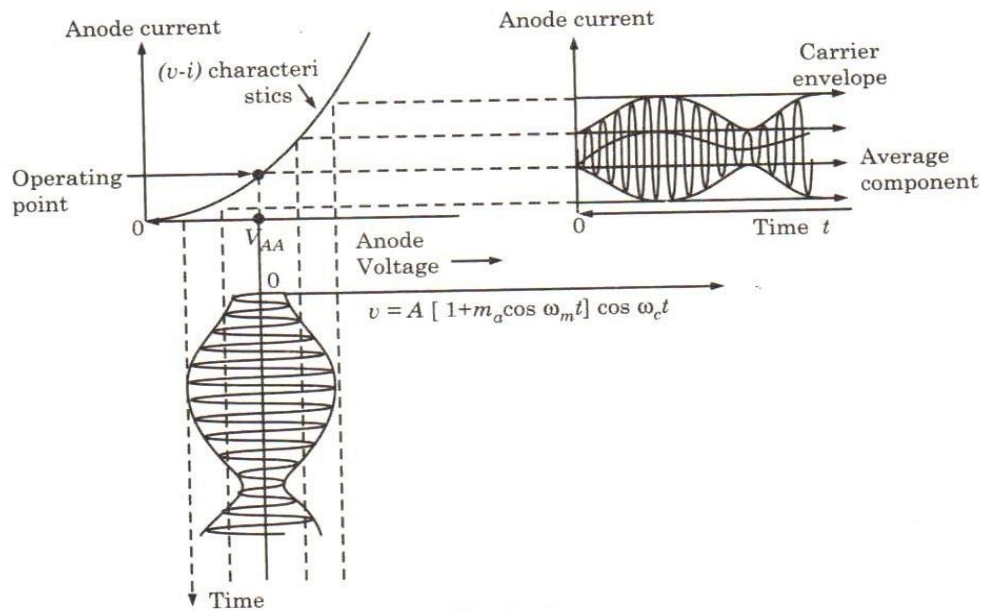
Substituting, the value of  $v$ , we get

$$I = a [A (1 + m_a \cos \omega_m t) \cos \omega_c t] + b [A (1 + m_a \cos \omega_m t) \cos \omega_c t]^2$$

If above expression is expanded, then we get terms of frequencies like  $2\omega_c$ ,  $2(\omega_c \pm \omega_m)$ ,  $\omega_m$  &  $2\omega_m$  besides the input frequency terms.

Hence this diode current  $I$  containing all these frequencies terms is passed through a low pass filter, which allows to pass the frequency below or up to modulating frequency  $\omega_m$  and rejects the other higher frequency components. Therefore, the modulating signal with frequency  $\omega_m$  is recovered from the input modulated signal.

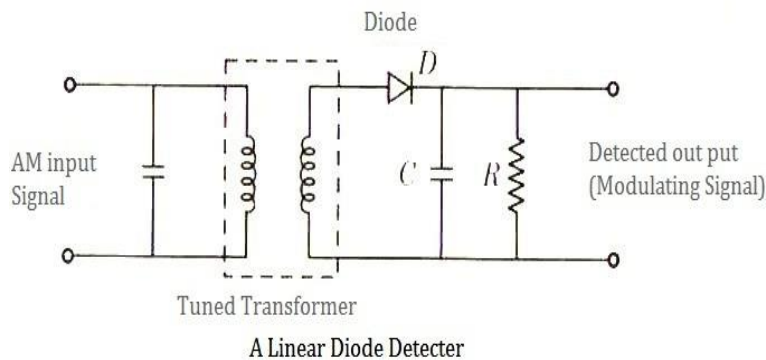




### **ENVELOPE DETECTOR:-**

A diode operating in a linear region of its V-I characteristics can extract the envelope of an AM wave. This type of detector is known as envelope detector. Envelope detector is most popular in commercial receiver circuits. Since it is very simple and is not expensive.

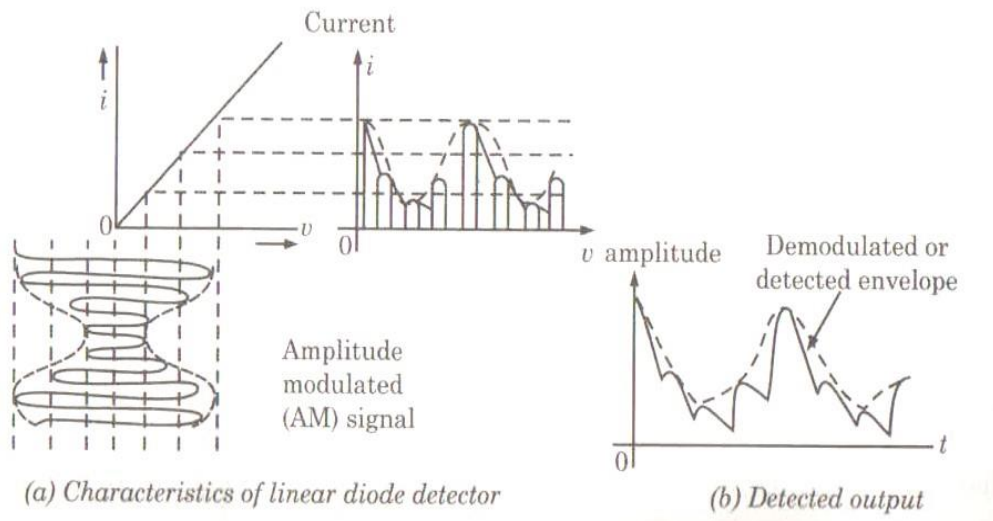
In the input portion of the ckt, the tuned transformer provides perfect tuning at the desired carrier frequency. RC network is the time-constant network. If the magnitude of the modulated signal at the input of the detector is 1 volt or more, the operation takes place in the linear portion of the V-I characteristics of diode.



### **Operation:-**

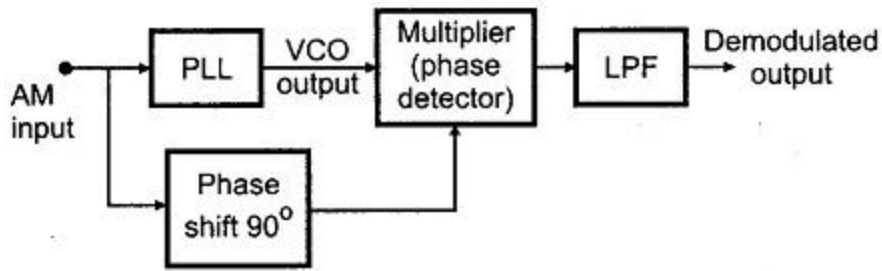
First, let us assume that the capacitor is absent in the ckt. In this case, the detector ckt will work as a half-wave rectifier. Therefore, the output waveform would be a half rectified modulated signal. Now let us consider that the capacitor is introduced in the circuit. For the +ve half cycle, the diode conducts and the capacitor is charged to the peak value of the carrier voltage. However, for a -ve half cycle, the diode is reverse biased and does not conduct. This means that the input carrier voltage is disconnected from the RC circuit. Therefore the capacitor starts discharging through the resistance with a time constant  $\tau = RC$  is suitably chosen, the voltage across the capacitor  $C$  will not fall appreciably during the small period of -ve half cycle, and by that time the next +ve cycle appears. The +ve cycle again charges the capacitor  $C$  to the peak value of the voltage and thus this process repeats again and again.

Hence the output voltage across the capacitor  $C$  is spiky modulating signal. However spikes are introduced because of charging and discharging of the capacitor  $C$ .



### **AM Demodulator using Phase locked loop**

A PLL can be used to demodulate AM signals.



- The PLL is locked to the carrier frequency of the incoming AM signal. Once locked the output frequency of VCO is same as the carrier frequency, but it is in unmodulated form.
- The modulated signal with 90° phase shift and the unmodulated carrier from output of PLL are fed to the multiplier. Since VCO output is always 90° out of phase with the incoming AM signal under the locked condition, both the signals applied to the multiplier are in same phase.
- Therefore, the output of the multiplier contains both the sum and the difference signals. The low pass filter connected at the output of the multiplier rejects high frequency components gives demodulated output.
- As PLL follows the input frequencies with high accuracy, a PLL AM detector exhibits a high degree of selectivity and noise immunity which is not possible with conventional peak detector type AM modulators.

## **2.4 DSB-SC SIGNAL AND SSB SIGNAL**

### **DSB-SC**

For 100% modulation about 67% of the total power is required for transmitting the carrier which does not contain any information. Hence, if the carrier is suppressed, only the sidebands remain and in this way a saving of two-third power may be achieved at 100% modulation. This type of suppression of carriers does not affect baseband signal. The resulting signal is DSB-SC signal.

As we know,

$$P_t = \left(1 + \frac{m_a^2}{2}\right)P_c$$

$$\text{Put } m_a = 1$$

$$P_t = \left(1 + \frac{1}{2}\right)P_c$$

$$\Rightarrow P_t = \frac{3}{2}P_c$$

$$\Rightarrow P_c = \frac{2}{3}P_t$$

$$\Rightarrow P_c = 0.67P_t$$

So,  $P_c$  is 67% of the transmitted power.

## **2.5 METHODS OF GENERATING & DETECTION OF SSB-SC SIGNAL**

### **SSB-SC**

- Amplitude modulation and double-sideband suppressed carrier modulation are wasteful of bandwidth. Since then both need a transmission bandwidth equal to twice the message signal bandwidth.
- In either case one half of the transmission bandwidth is occupied by the upper sideband of the modulated signal whereas the other half is occupied by the lower sideband. As far as the transmission of information is concerned, only one sideband is necessary.
- Thus if the carrier and one of the two side bands are suppressed at the transmitter, no information is lost. Modulation of this type which provides a single sideband with suppressed carrier is known as single sideband suppressed carrier system. Thus, SSB-SC system reduces the transmission bandwidth by half.

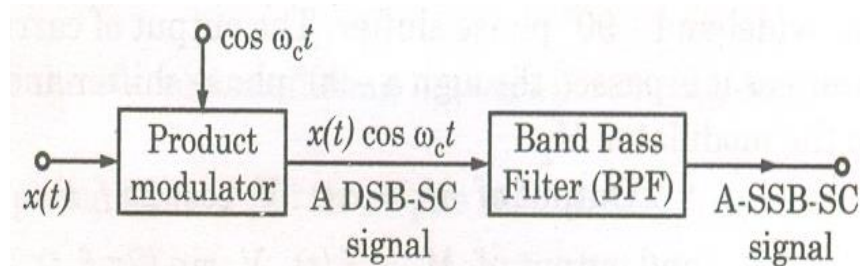
#### **Generation-**

SSB-SC signals may be generated by two methods

- (i) Frequency discrimination
- (ii) Phase discrimination

#### **FREQUENCY DISCRIMINATION METHOD-**

In a frequency discrimination method, a DSB-SC signal is generated by using an ordinary product modulator or balance modulator. After this, from the DSB-SC signal one of the two sidebands is filtered out by a suitable band pass filter.



**Frequency Discrimination Method for SSB SC Generation**

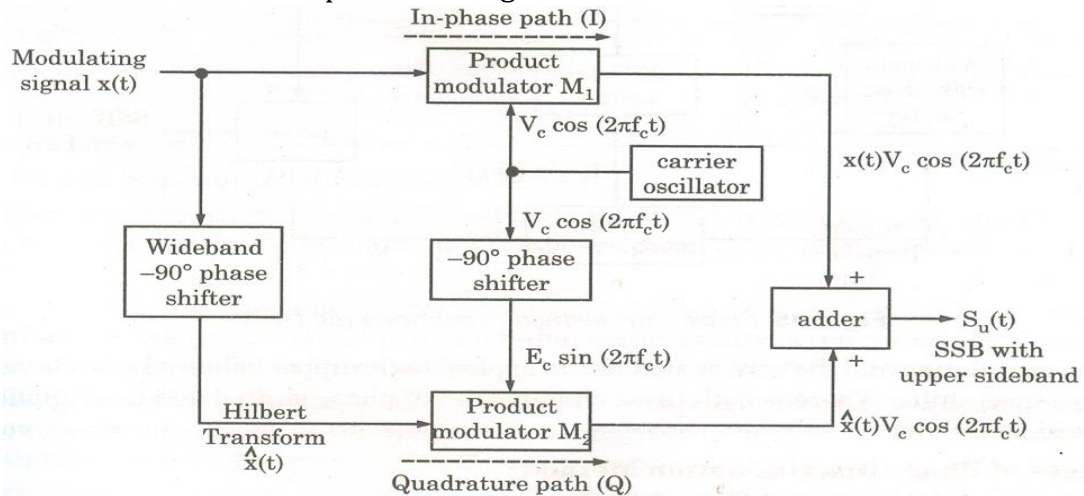
#### **Limitations-**

- The frequency discrimination method is useful only if the base band signal is restricted at its lower edge due to which the upper and lower sidebands are non-overlapping.

- The design of the band pass filter becomes difficult if the carrier frequency is quite higher than the bandwidth of the baseband signal.

### PHASE-SHIFT METHOD-

The phase shift method avoids filter. This method makes use of the two balanced modulators and two phase shifting networks.



### **Phase Discrimination Method for SSB- SC signal**

One of the modulators  $M_1$  receives the carrier voltage shifted by  $90^\circ$  and the modulating voltage, whereas another balanced modulator  $M_2$  receives the modulating voltage shifted by  $90^\circ$  and the carrier voltage. Both balanced modulators produce an output consisting only of sidebands. The two lower sidebands are out of phase and when combined together in the adder, they cancel each other. The upper sidebands are in phase and they added in the adder producing SSB in which the lower sideband has been cancelled.

### DEMODULATION-

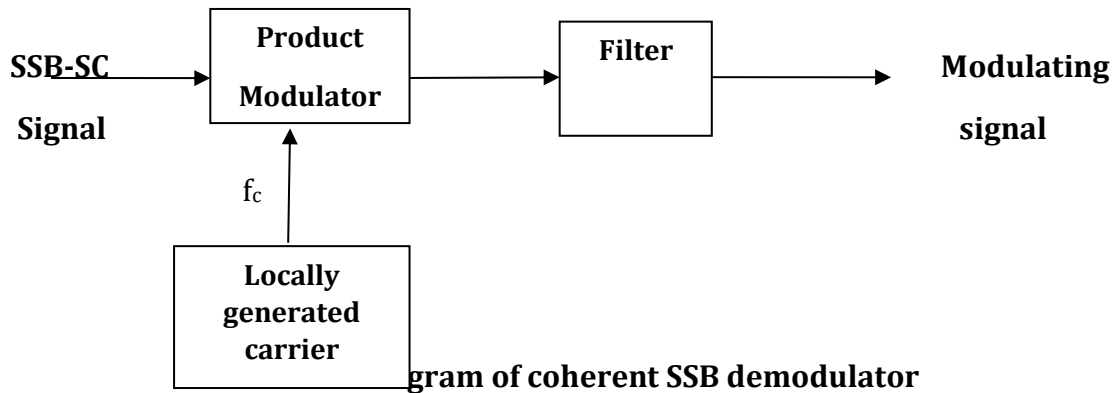
The baseband signal  $x(t)$  can be recovered from the SSB-SC signal by using the synchronous detection technique. With the help of synchronous detection method the spectrum of an SSB-SC signal centred about  $\omega = \pm\omega_c$ , is retranslated to the baseband spectrum which is centered about  $\omega = 0$ . The process of synchronous detection involves multiplication of the received SSB-SC signal with locally generated carrier. The generated carrier should have exactly the same frequency as that of the suppressed carrier. The product modulator multiplies the two signals at its input and the product signal is passed through a low pass filter with a bandwidth equal to  $f_m$ . At the output of the filter, we get the modulating signal back.

$$\begin{aligned}
 e_d(t) &= S(t)_{SSB} \times \cos\omega_c t \\
 &= [x(t) \cos\omega_c t \pm x_n(t) \sin\omega_c t] \cos\omega_c t
 \end{aligned}$$

$$= 1/2 x(t) + 1/2 [x(t) \cos 2\omega_c t \pm x_n(t) \sin 2\omega_c t]$$

When  $e_d(t)$  is passed through a low pass filter, then the terms centered about  $\pm 2\omega_c$  are filtered out and we get, at the output of detector, signal  $e_o$  which is given as

$$e_o(t) = 1/2 x(t)$$



## **2.6 METHODS OF GENERATION OF DSB-SC SIGNAL**

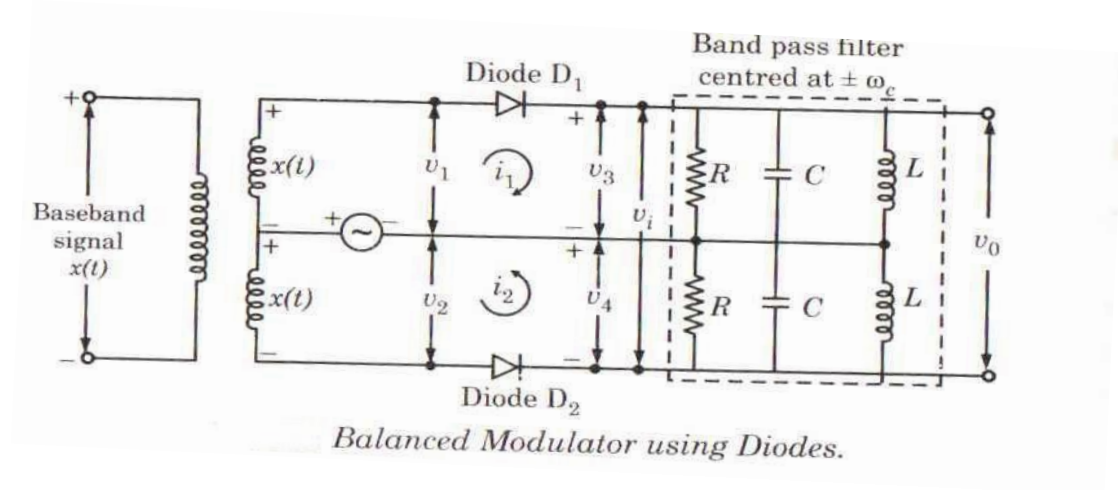
### **GENERATION OF DSB-SC SIGNAL-**

A circuit used to achieve the generation of a DSB-SC signal is called a product modulator. There are two types of product modulator.

1. Balanced Modulator
2. Ring Modulator

#### **Balance Modulator :-**

A non-linear resistance or a non-linear device may be used to produce amplitude modulation i.e, one carrier and two sidebands. However a DSB-SC signal contains only two sidebands. Thus if two non-linear devices such as diodes, transistors etc. are connected in a balanced mode so as to suppress the carriers of each other, then only sidebands are left i.e. a DSB-SC signal is generated.



Therefore a Balanced Modulator may be defined as a circuit in which two nonlinear devices are connected in a balanced mode to produce a DSB-SC signal. A modulating signal  $x(t)$  is applied to the diodes through a center-tapped transformer with the carrier signal  $\cos \omega_c t$ .

A non-linear VI relationship is given as,

$i = av + bv^2$  where  $v$  is the input voltage applied across a non-linear device and  $i$  is the current through the non-linear device.

For diode  $D_1$ ,  $i_1 = av_1 + bv_1^2$

Similarly, For diode  $D_2$ ,  $i_2 = av_2 + bv_2^2$

$$v_1 = \cos \omega_c t + x(t)$$

$$v_2 = \cos \omega_c t - x(t)$$

Due to currents  $i_1$  and  $i_2$  the net voltage  $v_i$  at the input of band pass filter expressed as  $v_i = i_1 R - i_2 R$ .

After substituting the values of  $i_1$  &  $i_2$  we get

$$v_i = 2R[ax(t) + 2bx(t) \cos \omega_c t]$$

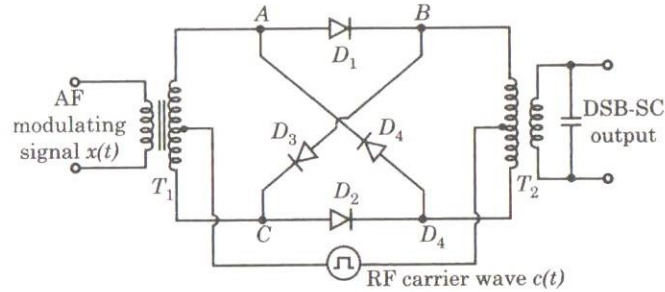
A band pass filter is that type of filter which allows to pass a band of frequencies. Here the band pass filter is centred around  $\pm \omega_c$ , it will pass a narrow band of frequencies centered at  $\pm \omega_c$ .

The output of the BPF is

$$v_o = 4bR x(t) \cos \omega_c t$$

### Ring Modulator-

Ring Modulator is another product Modulator, which is used to generate DSB-SC Signal. In a ring modulator circuit, four diodes are connected in the form of ring in which all four diodes point in same manner. All the four diodes in ring are controlled by a square wave carrier signal  $c(t)$  of frequency  $f_c$  applied through a centre tapped transformer.



*A diode ring modulator.*

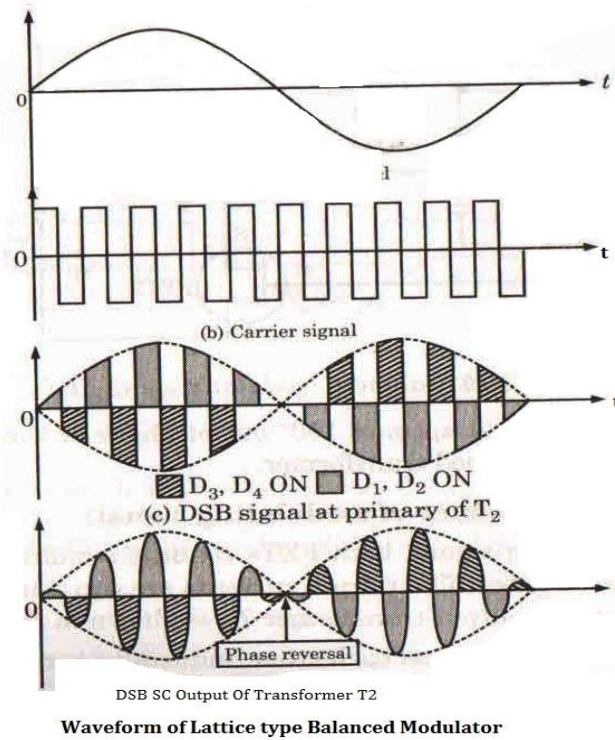
In case, when diodes are ideal and transformer are perfectly balanced, the two outer diodes are switched on if the carrier signal is positive whereas the two inner diodes are switched off and thus presenting very high impedance. Under this condition, the modulator multiplies the modulating signal  $x(t)$  by +1.

When carrier signal is -ve, the situation becomes reversed. In this case the modulator multiplies the modulating signal by -1.

$$C(t) = \frac{4}{\pi} \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{2n-1} \{\cos[2\pi f_c t(2n-1)]\}$$

We have  $S(t) = x(t) C(t)$





A Ring modulator is also known as a double balanced modulator. The modulating signal is band limited to  $-f_m \leq f \leq f_m$ . The desired sideband around the carrier frequency  $f_c$  may be selected using band pass filter having centre frequency  $\omega_c$  and bandwidth  $2f_m$ . To avoid overlapping of side bands  $f_c$  is greater than  $f_m$ .

## **2.7 DETECTION OF DSB-SC SIGNAL-**

The DSB-SC signal may be demodulated by following two methods.

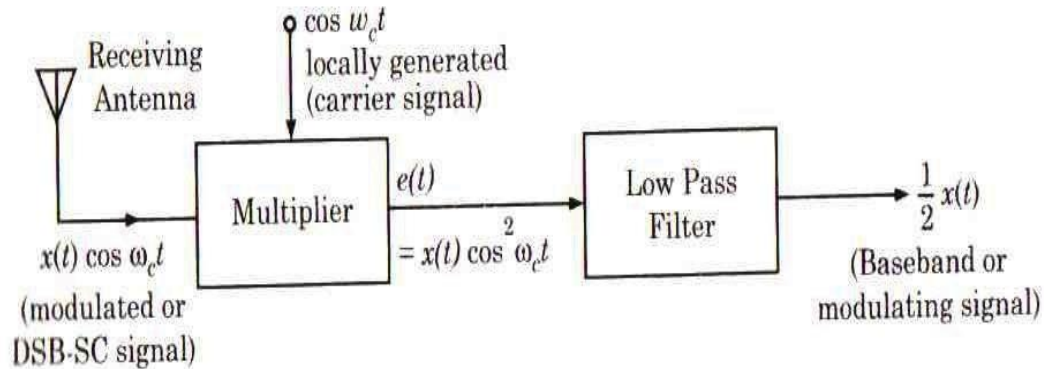
1. Synchronous detection method
2. Using envelope detector after carrier reinsertion.

### **Synchronous detection Method-**

DSB-SC signal is transmitted from the transmitter and it reaches the receiver through a transmission medium. At the receiver end, the original modulating signal  $x(t)$  is recovered from the modulated signal. This can be achieved by simply retranslating the baseband or modulating signal from a higher spectrum, cantered at  $\pm\omega_c$ , to the original

spectrum. This process is called demodulation or detection. Hence, the original or baseband signal is recovered from the modulated signal by the detection process.

A method of DSB-SC detection is known as synchronous detection.



*Synchronous detection method.*

### **Working principle-**

In synchronous detection method, the received modulated or DSB-SC signal is first multiplied with a locally generated carrier signal  $\cos \omega_c t$  and then passed through a low pass filter. At the output of a low pass filter, the original modulating signal is recovered.

### **2.8 VESTIGIAL SIDE BAND MODULATION:**

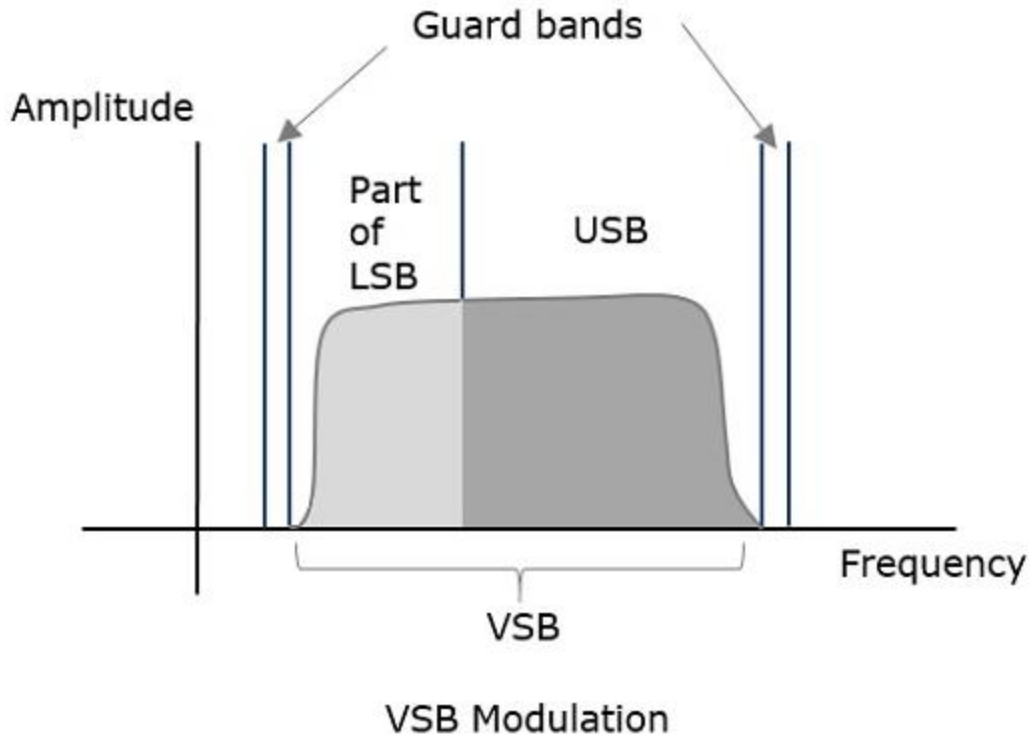
In case of SSB modulation, when a sideband is passed through the filters, the band pass filter may not work perfectly in practice. As a result of which, some of the information may get lost.

Hence to avoid this loss, a technique is chosen, which is a compromise between **DSB-SC** and **SSB**, called as **Vestigial Sideband (VSB)** technique. The word vestige which means “a part” from which the name is derived.

#### **Vestigial Sideband**

Both of the sidebands are not required for the transmission, as it is a waste. But a single band if transmitted, leads to loss of information. Hence, this technique has evolved.

**Vestigial Sideband Modulation** or **VSB Modulation** is the process where a part of the signal called as **vestige** is modulated, along with one sideband. A VSB signal can be plotted as shown in the following figure.



Along with the upper sideband, a part of the lower sideband is also being transmitted in this technique. A guard band of very small width is laid on either side of VSB in order to avoid the interferences. VSB modulation is mostly used in television transmissions.

#### VSB Modulation – Advantages

Following are the advantages of VSB –

- Highly efficient.
- Reduction in bandwidth.
- Filter design is easy as high accuracy is not needed.
- The transmission of low frequency components is possible, without difficulty.
- Possesses good phase characteristics.

#### VSB Modulation – Disadvantages

Following are the disadvantages of VSB –

- Bandwidth when compared to SSB is greater.
- Demodulation is complex.

## **UNIT-3: ANGLE MODULATION SYSTEMS**

### **3.1 CONCEPT OF ANGLE MODULATION & ITS TYPES**

Angle modulation is the process in which the frequency or the phase of the carrier signal varies according to the message signal.

The standard equation of the angle modulated wave is

$$S(t) = A_c \cos \theta_i(t)$$

Where  $A_c$  is the amplitude of the modulated wave, which is the same as the amplitude of the carrier signal.

$\theta_i(t)$  is the angle of the modulated wave

### **TYPES**

Angle modulation is further divided into frequency modulation and phase modulation.

**Frequency Modulation-** it is the process of varying the frequency of the carrier signal linearly with the message signal.

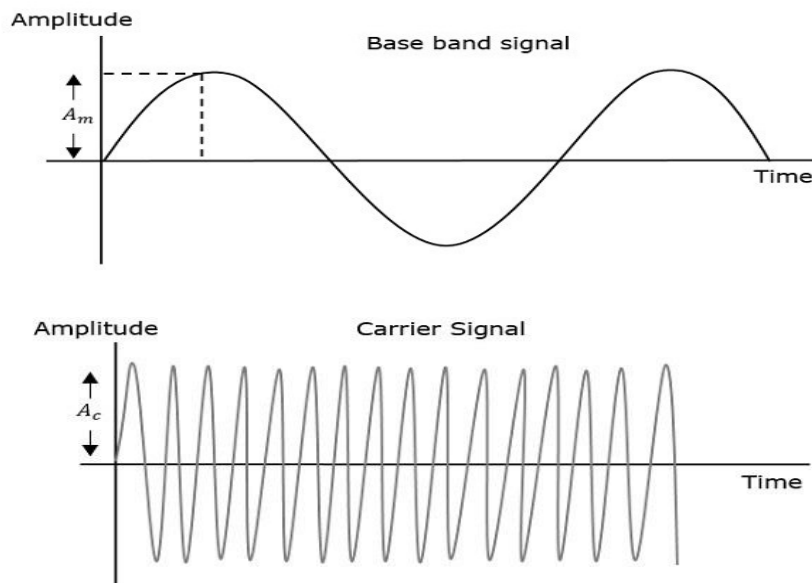
**Phase Modulation-** It is the process of varying the phase of the carrier signal linearly with the message signal.

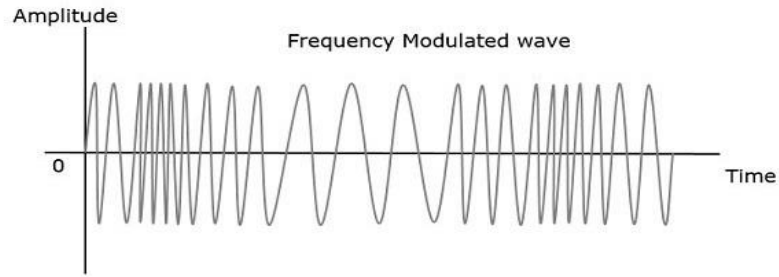
### **3.2 BASIC PRINCIPLE OF FREQUENCY MODULATION & FREQUENCY SPECTRUM OF FM SIGNAL**

#### **FREQUENCY MODULATION**

In frequency modulation, the frequency of the carrier signal varies in accordance with the instantaneous amplitude of the modulating signal. Here amplitude and phase of the carrier signal remains constant.

The frequency of the modulated wave increases, when the amplitude of the modulating signal increases and the frequency of the modulated wave decreases, when the amplitude of the modulating signal decreases.





## **FREQUENCY SPECTRUM OF FM SIGNAL-**

The frequency spectrum of the signal

$$v(t) = \cos(\omega_c t + \beta \sin \omega_m t) \quad \dots\dots(1)$$

which is the signal with the amplitude arbitrarily set at unity.

We have

$$\cos(\omega_c t + \beta \sin \omega_m t) = \cos \omega_c t \cos (\beta \sin \omega_m t) - \sin \omega_c t \sin (\beta \sin \omega_m t) \quad \dots\dots\dots(2)$$

Consider now the expression  $\cos (\beta \sin \omega_m t)$  which appears as a factor on the right hand side. It is an even, periodic function having an angular frequency  $\omega_m$ . Therefore, it is possible to expand this expression in a Fourier series in which  $\omega_m/2\pi$  is the fundamental frequency. The coefficients are functions of  $\beta$ , and, since function is even, the coefficients of the odd harmonics are zero. The result is

$$\cos \omega_c t \cos (\beta \sin \omega_m t) = J_0(\beta) + 2J_2(\beta) \cos 2\omega_m t + 2J_4(\beta) \cos 4\omega_m t + \dots \dots \dots + 2J_{2n}(\beta) \cos 2n\omega_m t + \dots \dots$$

While for  $\sin \omega_m t$ , which is an odd function, we find the expansion contains only odd harmonics and is given by

$$\sin (\beta \sin \omega_m t) = 2J_1(\beta) \sin \omega_m t + 2J_3(\beta) \sin 3\omega_m t + \dots \dots \dots + 2J_{2n-1}(\beta) \sin (2n-1)\omega_m t + \dots \dots$$

The functions  $J_n(\beta)$  occur often in the solution of engineering problem. They are known as Bessel functions of the first kind and of order n.

Putting the results given and using the identities

$$\cos A \cdot \cos B = \frac{1}{2} \cos (A - B) + \frac{1}{2} \cos (A + B)$$

$$\sin A \cdot \sin B = \frac{1}{2} \cos (A - B) - \frac{1}{2} \cos (A + B)$$

We find  $v(t)$  becomes

$$v(t) = J_0(\beta) \cos \omega_c - J_1(\beta)[\cos(\omega_c - \omega_m)t - \cos(\omega_c + \omega_m)t] \\ + J_2(\beta)[\cos(\omega_c - 2\omega_m)t + \cos(\omega_c + 2\omega_m)t] \\ - J_3(\beta)[\cos(\omega_c - 3\omega_m)t - \cos(\omega_c + 3\omega_m)t] + \dots$$

Observe that the spectrum is composed of a carrier with an amplitude and a set of sidebands spaced symmetrically on either side of the carrier at frequency separations of  $\omega_m, 2\omega_m, 3\omega_m$ , etc.

### **3.3 EXPRESSION FOR FREQUENCY MODULATED SIGNAL & MODULATION INDEX**

#### **EXPRESSION FOR FREQUENCY MODULATED SIGNAL-**

The equation for instantaneous frequency  $f_i$  in FM modulation is:

$$f_i = f_c + K_f m(t)$$

Where  $f_c$  is the carrier frequency

$K_f$  is the frequency sensitivity

$m(t)$  is the message signal

The relationship between angular frequency  $w_i$  and angle  $\theta_i(t)$  is

$$w_i = \frac{d\theta_i(t)}{dt} \\ \Rightarrow 2\pi f_i = \frac{d\theta_i(t)}{dt} \\ \Rightarrow \theta_i(t) = 2\pi \int f_i dt$$

Substitute  $f_i$  value in the equation

$$\theta_i(t) = 2\pi \int (f_c + K_f m(t)) dt \\ \Rightarrow \theta_i(t) = 2\pi f_c t + 2\pi K_f \int m(t) dt$$

Substitute the  $\theta_i(t)$  value in the standard equation of angle modulated wave.

$$S(t) = A_c \cos(2\pi f_c t + 2\pi K_f \int m(t) dt)$$

If the modulating signal is  $m(t) = A_m \cos(2\pi f_m t)$ , then the equation of FM wave will be

$$S(t) = A_c \cos(2\pi f_c t + 2\pi K_f \int A_m \cos(2\pi f_m t) dt) \\ \Rightarrow S(t) = A_c \cos(2\pi f_c t + 2\pi K_f \frac{1}{2\pi f_m} A_m \sin(2\pi f_m t)) \\ \Rightarrow S(t) = A_c \cos(2\pi f_c t + \beta \sin(2\pi f_m t))$$

Where  $\beta$  = modulation index

$$= \frac{k_f A_m}{f_m} = \frac{\Delta f}{f_m}$$

The difference between FM modulated frequency and normal carrier frequency is termed as frequency deviation. It is denoted by  $\Delta f$ .

$$\Delta f = k_f A_m$$

### **MODULATION INDEX-**

The modulation index is defined as the ratio of frequency deviation to the modulating frequency.

Modulation index,  $\beta$  = frequency deviation/modulation frequency

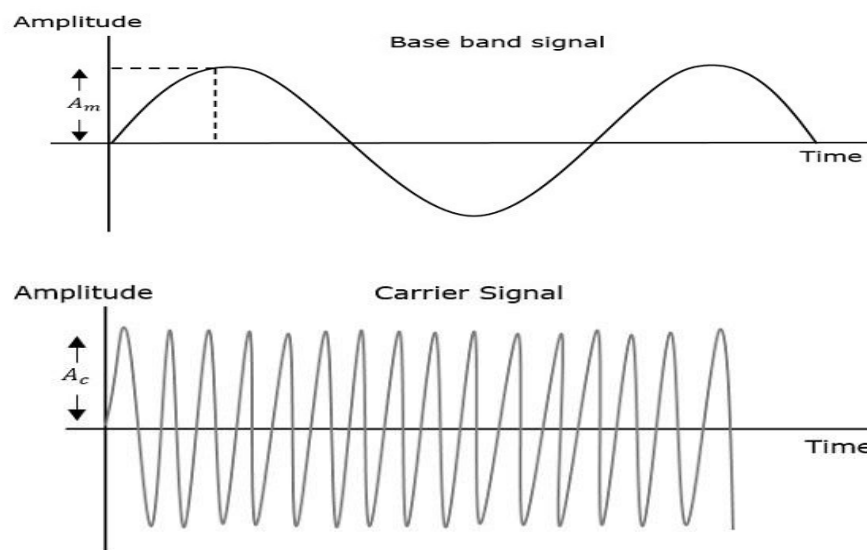
Or 
$$\beta = \frac{\Delta f}{f_m}$$

This modulation index may be greater than unity.

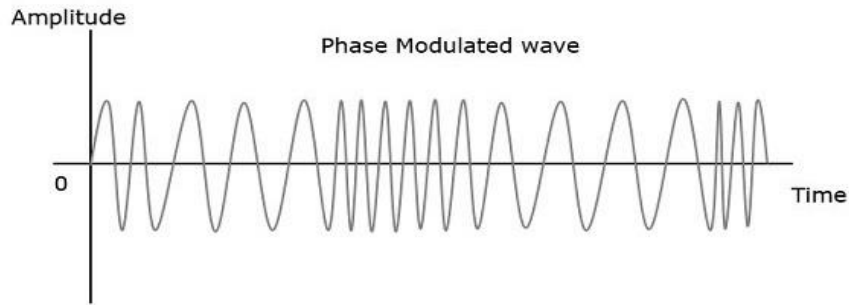
### **3.4 PHASE MODULATION & DIFFERENCE OF FM & PM-**

#### **PHASE MODULATION-**

In phase modulation, the phase of the carrier signal varies in accordance with the instantaneous amplitude of the modulating signal. Here with the change in phase, the frequency of the signal also shows variation. Thus it can be said that while phase modulating any signal, the phase as well as the frequency of the carrier signal shows variation.







The figure shows a sinusoidal message signal that is to be transmitted from one end to another, a carrier signal which is to be phase modulated and the last figure represents the phase modulated signal. Here it is clear from the above figure that when the amplitude of the sinusoidal signal starts to increase and reaches the maximum value then the phase lead of the carrier signal gets increased. Due to this a compression in the carrier signal is noticed.

However, when the amplitude of the modulating signal starts falling and attains a minimum value, then the phase lag of the carrier wave occurs. Due to this, the frequency of the signal gets increased.

The equation for instantaneous phase  $\Phi_i$  in phase modulation is

$$\Phi_i = K_p m(t)$$

Where,  $K_p$  is the phase sensitivity

$m(t)$  is the modulating signal

The standard equation of angle modulated wave is

$$S(t) = A_c \cos(2\pi f_c t + \Phi_i)$$

Substitute,  $\Phi_i$  value in the above equation

$$S(t) = A_c \cos(2\pi f_c t + K_p m(t))$$

If the modulating signal,  $m(t) = A_m \cos(2\pi f_m t)$  then the equation of PM wave will be

$$S(t) = A_c \cos(2\pi f_c t + K_p A_m \cos(2\pi f_m t))$$

$$\Rightarrow S(t) = A_c \cos(2\pi f_c t + \beta \cos(2\pi f_m t))$$

Where,  $\beta$  = modulation index

### **DIFFERENCE OF FM & PM-**

S.No.	FM	PM
1.	$s(t) = V_c \sin [\omega_c t + m_f \sin \omega_m t]$	$s(t) = V_c \sin[\omega_c t + m_p \sin \omega_m t]$
2.	Frequency deviation is proportional to modulating voltage.	Phase deviation is proportional to the modulating voltage.
3.	Associated with the change in $f_c$ , there is some phase change.	Associated with the changes in phase, there is some change in $f_c$ .
4.	$m_f$ is proportional to the modulating voltage as well as the modulating frequency $f_m$ .	$m_p$ is proportional only to the modulating voltage.
5.	It is possible to receive FM on a PM receiver.	It is possible to receive PM on a FM receiver.
6.	Noise immunity is better than AM and PM.	Noise immunity is better than AM but worse than FM.
7.	Amplitude of the FM wave is constant.	Amplitude of the PM wave is constant.
8.	Signal to noise ratio is better than that of PM.	Signal to noise ratio is inferior to that in FM.
9.	FM is widely used.	PM is used in some mobile systems.
10.	In FM, the frequency deviation is proportional to the modulating voltage only.	In PM, the frequency deviation is proportional to both the modulating voltage and modulating frequency.

### **3.5 COMPARE BETWEEN AM AND FM MODULATION-**

#### **AM-**

- (i) Amplitude of AM wave will change with the modulating voltage.
- (ii) Transmitted power is dependent on the modulation index.
- (iii) Carrier power and one sideband power are useless.
- (iv) AM receivers are not immune to noise.
- (v) Frequency deviation feature is absent in AM.
- (vi) Bandwidth =  $2f_m$ . It is not dependent on the modulation index.
- (vii) Bandwidth is much less than FM.
- (viii) Ground wave and sky wave propagation is used. Therefore larger area is covered than FM.
- (ix) Not possible to operate more channels on the same frequency.
- (x) AM equipment are less complex.
- (xi) Number of sidebands in AM will be constant and equal to 2.
- (xii) The information is contained in the amplitude variation of the carrier.

#### **FM-**

- (i) Amplitude of FM wave is constant. It is independent of the modulation index.
- (ii) Transmitted power remains constant. It is independent of mf.
- (iii) All the transmitted power is useful.
- (iv) FM receivers are immune to noise.
- (v) It is possible to decrease noise further by increasing deviation.
- (vi) Bandwidth =  $2[\Delta_f + f_m]$ . The bandwidth depends on modulation index.
- (vii) Bandwidth is large. Hence, wide channel is required.
- (viii) Space wave is used for propagation. So, radius of transmission is limited to line of sight.
- (ix) It is possible to operate several transmitters on same frequency.
- (x) FM transmission and reception equipment are more complex.
- (xi) The number of sidebands having significant amplitudes depends on modulation index mf.
- (xii) The information is contained in the frequency variation of the carrier.

### **3.6 FM GENERATION-**

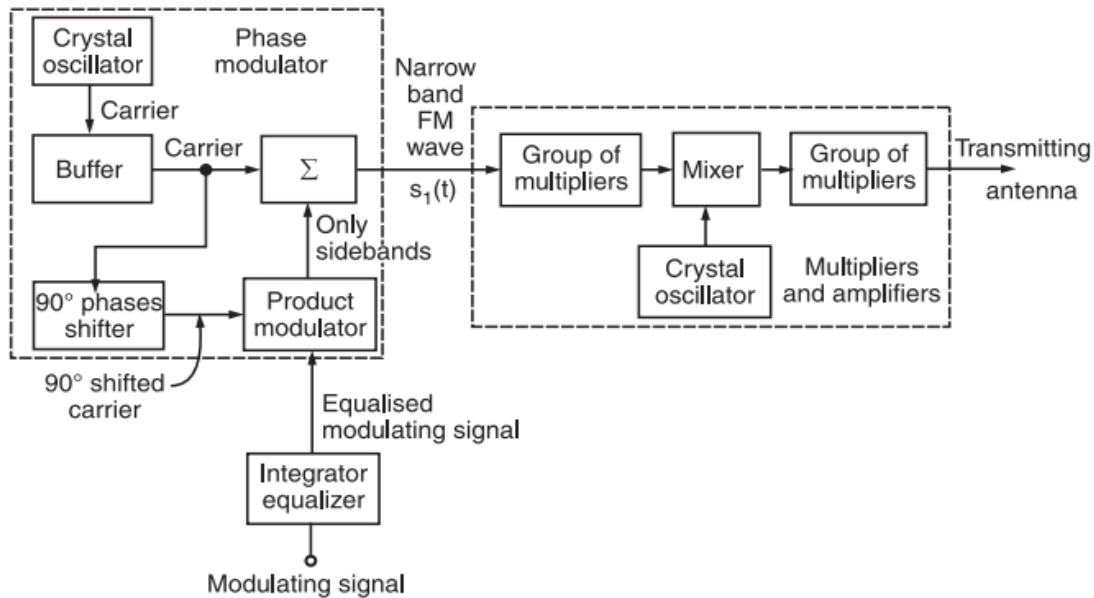
The FM modulator circuits used for generating FM signals may be put into two categories as under.

- (i) The direct method or parameter variation method
- (ii) The indirect method or the Armstrong method

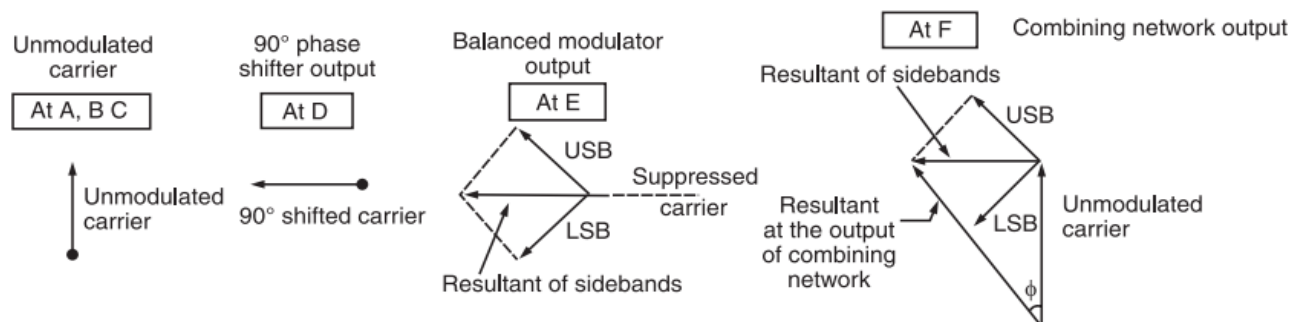
#### **INDIRECT METHOD OR THE ARMSTRONG METHOD:**

In direct methods of generation of FM, LC oscillators are used. The crystal oscillator cannot be used. The LC oscillators are not stable enough for the broadcast purpose. Thus, the direct methods cannot be used for the broadcast application. In order to overcome the limitation of direct method, we use indirect method of FM generation called as the Armstrong method.

In this method, the FM is obtained through phase modulation. A crystal oscillator can be used hence the frequency stability is very high and this method is widely used in practice. The Armstrong method uses the phase modulator to generate a frequency modulated wave. Crystal oscillator produce stable frequency upto 1MHz.



- The modulating signal  $x(t)$  is passed through an integrator before applying it to the phase modulator.
- The crystal oscillator produces a stable unmodulated carrier which is applied to the  $90^\circ$  phase shifter as well as the combining network through a buffer.
- The  $90^\circ$  phase shifter produces a  $90^\circ$  phase shifted carrier. It is applied to the balanced modulator along with the modulating signal. Thus, the carrier used for modulation is  $90^\circ$  shifted with respect to the original carrier.
- At the output of the product modulator, we get DSB SC signal i.e., AM signal without carrier. This signal consists of only two sidebands with their resultant in phase with the  $90^\circ$  shifted carrier.
- The two sidebands and the original carrier without any phase shift are applied to a combining network ( $\Sigma$ ). At the output of the combining network, we get the resultant of vector addition of the carrier and two sidebands



- As the amplitude of modulating signal increases the modulation index will increase and the amplitude of sidebands will also increase. Hence the amplitude of their resultant increases.
- This will increase the angle  $\phi$  made by the resultant with unmodulated carrier. The angle  $\phi$  decreases with reduction in modulation index. Thus the resultant at the output of the combining network is phase modulated.
- The FM signal produced at the output of phase modulator has a low carrier frequency and low modulation index. They are increased to an high value with the help of frequency multiplies, mixer and amplifier.
- For low modulation index,  $\phi$  is small and for high modulation index,  $\phi$  increases.

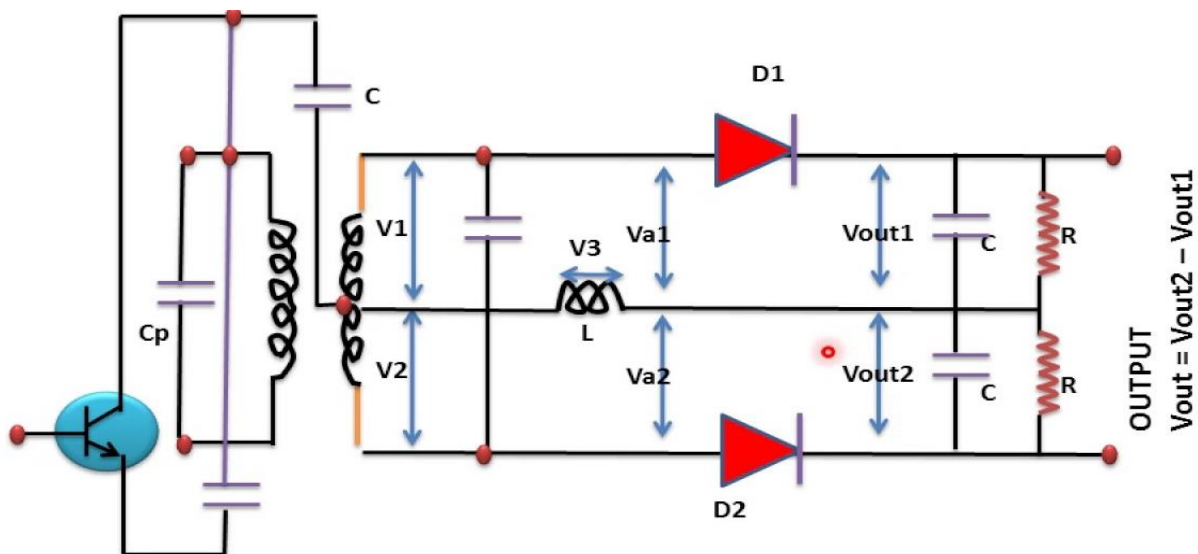
### **3.7 FM DEMODULATOR-**

The demodulation process of FM waves is exactly opposite to that of the frequency modulation. After demodulation, we get the original modulating signal at the demodulation output.

#### **METHODS OF FM DEMODULATION-**

##### **FORSTER SEELEY DETECTOR-**

The circuit diagram of phase discriminator or Foster Seeley Discriminator is given below



This circuit consists of an inductively coupled double tuned circuit in which both primary and secondary coils are tuned to the same frequency. The center of the secondary coil is connected to the top of the primary through a capacitor  $C$ . this capacitor performs the functions are:

- It blocks the D.C. from primary to secondary.

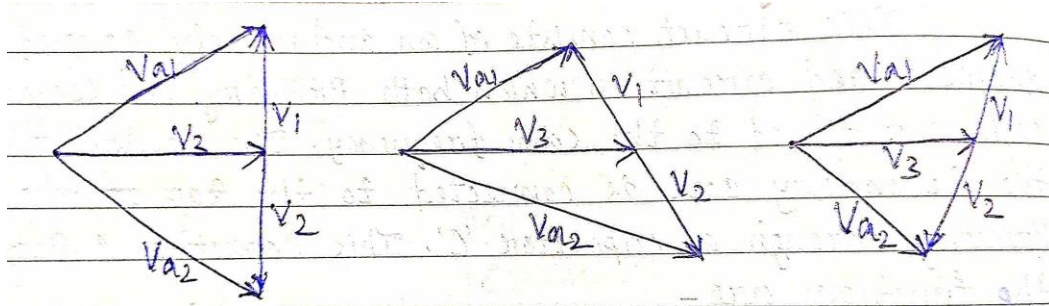
- (ii) It couples the signal frequency from primary to center tapping of the secondary.

The primary voltage  $V_3$  appears across the inductor in primary side. Nearly entire voltage  $V_3$  appears across inductor L except a small drop across the capacitor C.

The center tapping of the secondary coil has an equal and opposite voltage across each half winding. Hence  $V_1$  and  $V_2$  are equal in magnitude but opposite in phase. The radio frequency voltages  $V_{a1}$  and  $V_{a2}$  applied to the diodes  $D_1$  and  $D_2$  are expressed as

$$V_{a1} = V_3 + V_1$$

$$V_{a2} = V_3 + V_2$$



Voltages  $V_{a1}$  and  $V_{a2}$  depend upon the phasor relations between  $V_1$ ,  $V_2$  and  $V_3$ . The phase position of  $V_1$  and  $V_2$  relative to  $V_3$  would depend upon the tuned secondary coil at the resonance or off the resonance.

- At resonance- when an input voltage has a frequency equal to the resonant frequency of the tuned secondary,  $V_3$  is in phase quadrature with  $V_1$  and  $V_2$ . The resultant voltage  $V_{a1}$  and  $V_{a2}$  are equal in magnitude.
- Off resonance- when an input signal frequency is above the resonant frequency the phase difference between  $V_3$  and  $V_1$  is  $45^\circ$ . Because  $V_2$  is in phase opposition of  $V_1$  the phase difference between  $V_3$  and  $V_2$  is  $135^\circ$ . The phasor diagram reveals that  $V_{a1}$  is reduced where as  $V_{a2}$  is increased. The situation is reversed when the input voltage has a frequency below the resonant frequency. Hence the amplitude of the voltage  $V_{a1}$  and  $V_{a2}$  will vary.

The voltage  $V_{a1}$  and  $V_{a2}$  are separately rectified by diodes  $D_1$  and  $D_2$  respectively to produce  $V_{out1}$  and  $V_{out2}$ . The output voltage  $V_o$  is

$$V_o = |V_{out2}| - |V_{out1}|$$

**Advantages:**

1. It is more easy to align than the balanced slope detector as there are only two tuned circuits and both are to be tuned at the same frequency  $f_c$ .
2. Linearity is better. This is because the operation of the circuit is dependent more on the primary to secondary relationship which is very much linear.

### **Drawbacks**

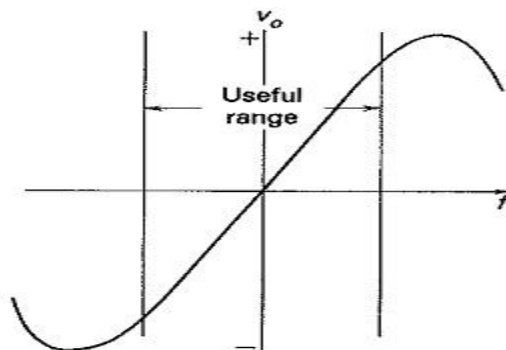
It does not provide amplitude limiting. So in the presence of noise or any other spurious amplitude variations, the demodulator output responds to them and produce errors.

### **RATIO DETECTOR-**

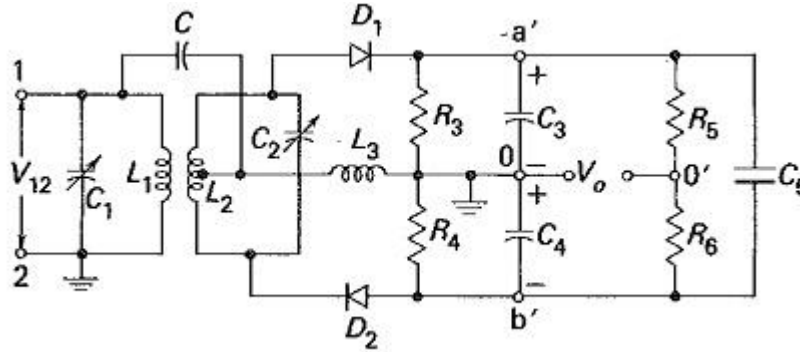
The RATIO DETECTOR uses a double-tuned transformer to convert the instantaneous frequency variations of the fm input signal to instantaneous amplitude variations. These amplitude variations are then rectified to provide a dc output voltage which varies in amplitude and polarity with the input signal frequency. This detector demodulates fm signals and suppresses amplitude noise without the need of limiter stages.

In the Foster-Seeley discriminator, changes in the magnitude of the input signal will give rise to amplitude changes in the resulting output voltage. This makes prior limiting necessary. It is possible to modify the discriminator circuit to provide limiting, so that the amplitude limiter may be dispensed with. A circuit so modified is called a Ratio Detector Circuit.

As we now, the sum  $V_{a0} + V_{b0}$  remains constant, although the difference varies because of changes in input frequency. This assumption is not completely true. Deviation from this ideal does not result in undue distortion in the Ratio Detector Circuit, although some distortion is undoubtedly introduced. It follows that any variations in the magnitude of this sum voltage can be considered spurious here. Their suppression will lead to a discriminator which is unaffected by the amplitude of the incoming signal. It will therefore not react to noise amplitude or spurious amplitude modulation.



It now remains to ensure that the sum voltage is kept constant. Unfortunately, this cannot be accomplished in the phase discriminator, and the circuit must be modified.. This is used to show how the circuit is derived from the discriminator and to explain its operation. It is seen that three important changes have been made: one of the diodes has been reversed, a large capacitor ( $C_5$ ) has been placed across what used to be the output, and the output now is taken from elsewhere.



### **Operation:**

With diode  $D_2$  reversed,  $o$  is now positive with respect to  $b'$ , so that  $V_{a'b'}$  is now a sum voltage, rather than the difference it was in the discriminator. It is now possible to connect a large capacitor between  $a'$  and  $b'$  to keep this sum voltage constant. Once  $C_5$  has been connected, it is obvious that  $V_{a'b'}$  is no longer the output voltage; thus the output voltage is now taken between  $o$  and  $o'$ . It is now necessary to ground one of these two points, and  $o$  happens to be the more convenient, as will be seen when dealing with practical Ratio Detector Circuit. Bearing in mind that in practice  $R_5 = R_6$ ,  $V_o$  is calculated as follows:

$$V_o = V_{b'o'} - V_{b'o} = \frac{V_{a'b'}}{2} - V_{b'o} = \frac{V_{a'o} + V_{b'o}}{2} - V_{b'o}$$

$$= \frac{V_{a'o} - V_{b'o}}{2}$$

The above equation shows the ratio detector output voltage is equal to half the difference between the output voltages from the individual diodes. Thus (as in the phase discriminator) the output voltage is proportional to the difference between the individual output voltages. The Ratio Detector Circuit therefore behaves identically to the discriminator for input frequency changes.



## **MODULE-2**

### **UNDERSTAND THE WORKING OF CONVERTERS, AC REGULATORS AND CHOPPERS**

#### **2.1 CONTROLLED RECTIFIER**

Rectifier are used to convert A.C to D.C supply. Rectifiers can be classified as single phase rectifier and three phase rectifier. Single phase rectifier are classified as 1- $\Phi$  half wave and 1- $\Phi$  full wave rectifier. Three phase rectifier are classified as 3- $\Phi$  half wave rectifier and 3- $\Phi$  full wave rectifier. 1- $\Phi$  Full wave rectifier are classified as 1- $\Phi$  mid point type and 1- $\Phi$  bridge type rectifier. 1- $\Phi$  bridge type rectifier are classified as 1- $\Phi$  half controlled and 1- $\Phi$  full controlled rectifier. 3- $\Phi$  full wave rectifier are again classified as 3- $\Phi$  mid point type and 3- $\Phi$  bridge type rectifier. 3- $\Phi$  bridge type rectifier are again divided as 3- $\Phi$  half controlled rectifier and 3- $\Phi$  full controlled rectifier

#### **2.2 Single phase half wave circuit with R load:**

## 6.1. PRINCIPLE OF PHASE CONTROL

The simplest form of controlled rectifier circuits consist of a single thyristor feeding dc power to a resistive load  $R$  as shown in Fig. 6.1 (a). The source voltage is  $v_s = V_m \sin \omega t$ , Fig. 6.1 (b). An SCR can conduct only when anode voltage is positive and a gating signal is applied. As such, a thyristor blocks the flow of load current  $i_o$  until it is triggered. At some delay angle  $\alpha$ , a positive gate signal applied between gate and cathode turns on the SCR. Immediately, full supply voltage is applied to the load as  $v_o$ , Fig. 6.1 (b). At the instant of delay angle  $\alpha$ ,  $v_o$  rises from zero to  $V_m \sin \alpha$  as shown. For resistive load, current  $i_o$  is in phase with  $v_o$ . Firing angle of a thyristor is measured from the instant it would start conducting if it were replaced by a diode. In Fig. 6.1, if thyristor is replaced by diode, it would begin conduction at  $\omega t = 0, 2\pi, 4\pi$  etc.; firing angle is therefore measured from these instants. A *firing angle* may thus be defined as the angle between the instant thyristor would conduct if it were a diode and the instant it is triggered.

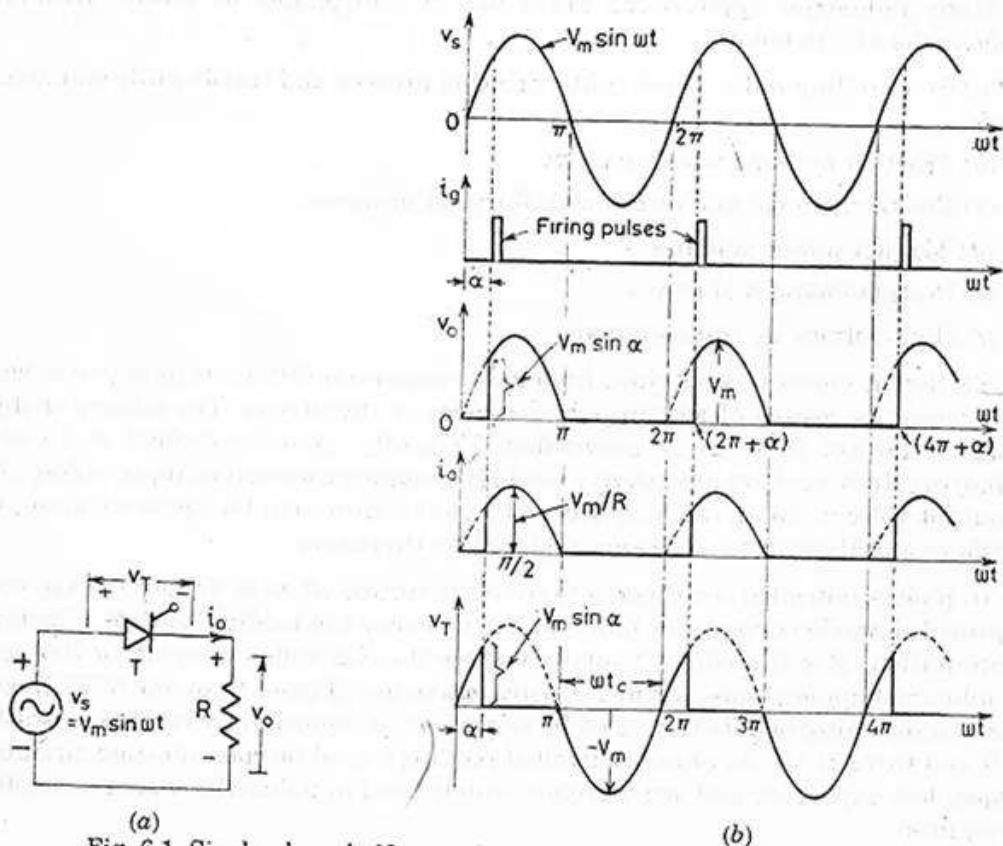


Fig. 6.1. Single-phase half-wave thyristor circuit with  $R$  load  
(a) circuit diagram and (b) voltage and current waveforms.

A firing angle may also be defined as follows: A *firing angle* is measured from the angle that gives the largest average output voltage, or the highest load voltage. If thyristor in Fig. 6.1 is fired at  $\omega t = 0, 2\pi, 4\pi$  etc., the average load voltage is the highest; the firing angle should thus be measured from these instants. A *firing angle* may thus be defined as the angle measured from the instant that gives the largest average output voltage to the instant it is triggered.

Once the SCR is on, load current flows, until it is turned-off by reversal of voltage at  $\omega t = \pi, 3\pi$  etc. At these angles of  $\pi, 3\pi, 5\pi$  etc. load current falls to zero and soon after the supply voltage reverse biases the SCR, the device is therefore turned off. It is seen from Fig. 6.1 (b) that by varying the firing angle  $\alpha$ , the *phase* relationship between the start of the load current and the supply voltage can be *controlled*; hence the term *phase control* is used for such a method of controlling the load currents [3].

A single-phase half-wave circuit is one which produces only *one* pulse of load current during one cycle of source voltage. As the circuit shown in Fig. 6.1 (a) produces only one load current pulse for one cycle of sinusoidal source voltage, this circuit represents a single-phase half-wave thyristor circuit.

In Fig. 6.1 (b), thyristor conducts from  $\omega t = \alpha$  to  $\pi, (2\pi + \alpha)$  to  $3\pi$  and so on. Over the firing angle delay  $\alpha$ , load voltage  $v_o = 0$  but during conduction angle  $(\pi - \alpha)$ ,  $v_o = v_s$ . As firing angle is increased from zero to  $\pi$ , the average load voltage decreases from the largest value to zero.

The variation of voltage across thyristor is also shown as  $v_T$  in Fig. 6.1 (b). Thyristor remains on from  $\omega t = \alpha$  to  $\pi, (2\pi + \alpha)$  to  $3\pi$  etc., during these intervals  $v_T = 0$  (strictly speaking 1 to 1.5 V). It is off from  $\pi$  to  $(2\pi + \alpha)$ ,  $3\pi$  to  $(4\pi + \alpha)$  etc., during these off intervals  $v_T$  has the waveshape of supply voltage  $v_s$ . It may be observed that  $v_s = v_o + v_T$ . As the thyristor is reverse biased for  $\pi$  radians, the circuit turn-off time is given by

$$t_c = \frac{\pi}{\omega} \text{ sec}$$

where  $\omega = 2\pi f$  and  $f$  is the supply frequency in Hz.

The circuit turn-off time  $t_c$  must be than the SCR turn-off time  $t_q$  as specified by the manufacturers.

Average voltage  $V_o$  across load  $R$  in Fig. 6.1 for the single-phase half-wave circuit in terms of firing angle  $\alpha$  is given by

$$V_o = \frac{1}{2\pi} \int_{\alpha}^{\pi} V_m \sin \omega t \cdot d(\omega t) = \frac{V_m}{2\pi} (1 + \cos \alpha) \quad \dots(6.1)$$

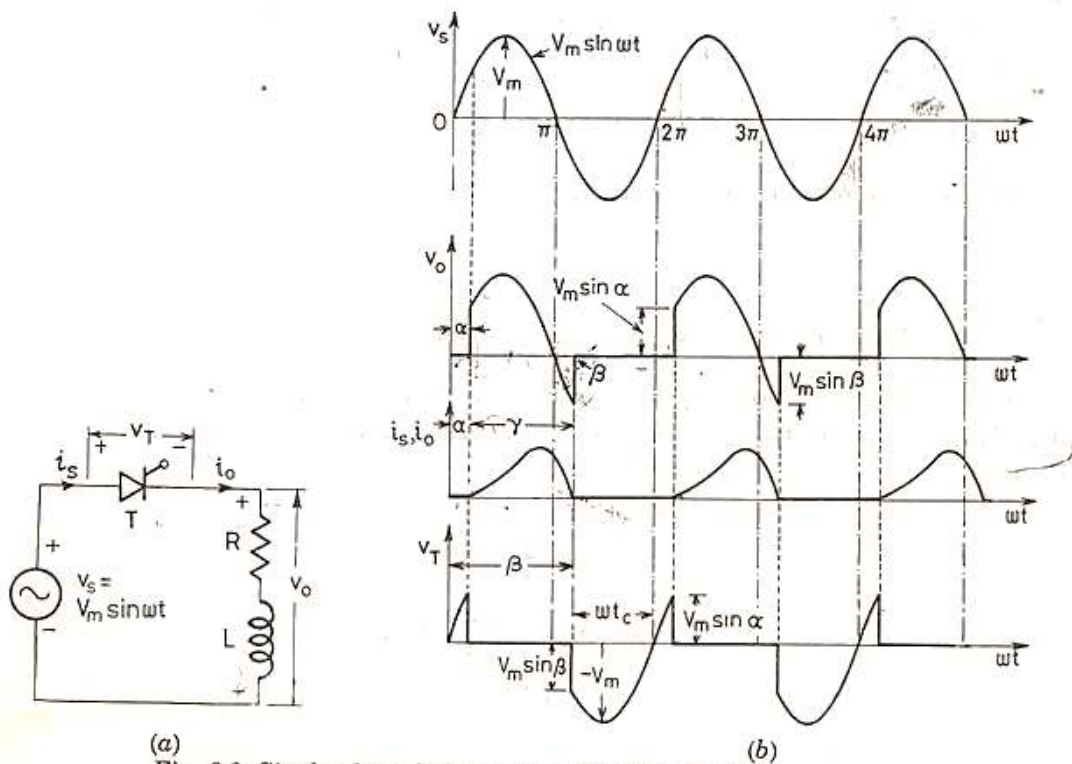
The maximum value of  $V_o$  occurs at  $\alpha = 0^\circ$ .

$$\therefore V_{o-m} = \frac{V_m}{2\pi} \cdot 2 = \frac{V_m}{\pi}$$

$$\text{Average load current, } I_o = \frac{V_o}{R} = \frac{V_m}{2\pi R} (1 + \cos \alpha) \quad \dots(6.2)$$

## Single phase half wave circuit with R-L load

A single-phase half-wave thyristor circuit with  $RL$  load is shown in Fig. 6.2 (a). Line voltage  $v_s$  is sketched in the top of Fig. 6.2 (b). At  $\omega t = \alpha$ , thyristor is turned on by gating signal. The load voltage  $v_o$  at once becomes equal to source voltage  $v_s$  as shown. But the inductance  $L$  forces the load, or output, current  $i_o$  to rise gradually. After some time,  $i_o$  reaches maximum value and then begins to decrease. At  $\omega t = \pi$ ,  $v_o$  is zero but  $i_o$  is not zero because of the load inductance  $L$ . After  $\omega t = \pi$ , SCR is subjected to reverse anode voltage but it will not be turned off as load current  $i_o$  is not less than the holding current. At some angle  $\beta > \pi$ ,  $i_o$  reduces to zero and SCR is turned off as it is already reverse biased. After  $\omega t = \beta$ ,  $v_o = 0$  and  $i_o = 0$ . At  $\omega t = 2\pi + \alpha$ , SCR is triggered again,  $v_o$  is applied to the load and load



(a) (b)  
Fig. 6.2. Single-phase half-wave circuit with  $RL$  load  
(a) circuit diagram and (b) voltage and current waveforms.

current develops as before. Angle  $\beta$  is called the *extinction angle* and  $(\beta - \alpha) = \gamma$  is called the *conduction angle*.

The waveform of voltage  $v_T$  across thyristor  $T$  in Fig. 6.2 (b) reveals that when  $\omega t = \alpha$ ,  $v_T = V_m \sin \alpha$ ; from  $\omega t = \alpha$  to  $\beta$ ,  $v_T = 0$  and at  $\omega t = \beta$ ,  $v_T = V_m \sin \beta$ . As  $\beta > \pi$ ,  $v_T$  is negative at  $\omega t = \beta$ . Thyristor is therefore reverse biased from  $\omega t = \beta$  to  $2\pi$ . Thus, circuit turn-off time  $t_C = \frac{2\pi - \beta}{\omega}$  sec. For satisfactory commutation,  $t_C$  should be more than  $t_q$  the thyristor turn-off time.

The voltage equation for the circuit of Fig. 6.2 (a) is

$$V_m \sin \omega t = R i_0 + L \frac{di_0}{dt}$$

The load current  $i_0$  consists of two components, one steady-state component  $i_s$  and the other transient component  $i_t$ . Here  $i_s$  is given by

$$i_s = \frac{V_m}{\sqrt{R^2 + X^2}} \sin (\omega t - \phi)$$

where  $\phi = \tan^{-1} \frac{X}{R}$  and  $X = \omega L$ . Here  $\phi$  is the angle by which rms current  $I_s$  lags  $V_s$ .

The transient component  $i_t$  can be obtained from force-free equation

$$R i_t + L \frac{di_t}{dt} = 0$$

Its solution gives,

$$i_t = A e^{-(R/L)t}$$

$\therefore$

$$i_o = i_s + i_t = \frac{V_m}{Z} \sin (\omega t - \phi) + A e^{-(R/L)t} \quad \dots(6.6)$$

where

$$Z = \sqrt{R^2 + X^2}$$



$$V_0 = \frac{1}{2\pi} \int_{\alpha}^{\beta} V_m \sin \omega t \, d(\omega t) = \frac{V_m}{2\pi} (\cos \alpha - \cos \beta) \quad \dots(6.8)$$

$$\text{Average load current, } I_0 = \frac{V_m}{2\pi R} (\cos \alpha - \cos \beta) \quad \dots(6.9)$$

$$\begin{aligned} \text{Rms load voltage, } V_{or} &= \left[ \frac{1}{2\pi} \int_{\alpha}^{\beta} V_m^2 \sin^2 \omega t \cdot d(\omega t) \right]^{1/2} \\ &= \frac{V_m}{2\sqrt{\pi}} \left[ (\beta - \alpha) - \frac{1}{2} (\sin 2\beta - \sin 2\alpha) \right]^{1/2} \quad \dots(6.10) \end{aligned}$$

Rms load current can be obtained from Eq. (6.7) if required.

### 6.1.2. Single-phase Half-wave Circuit with RL Load and Freewheeling Diode

The waveform of load current  $i_0$  in Fig. 6.2 (b) can be improved by connecting a freewheeling ( or flywheeling ) diode across load as shown in Fig. 6.3 (a). A freewheeling diode is also called by-pass or commutating diode. At  $\omega t = 0$ , source voltage is becoming positive. At some delay angle  $\alpha$ , forward biased SCR is triggered and source voltage  $v_s$  appears across load as  $v_0$ . At  $\omega t = \pi$ , source voltage  $v_s$  is zero and just after this instant, as  $v_s$  tends to reverse, freewheeling diode FD is forward biased through the conducting SCR. As a result, load current  $i_0$  is immediately transferred from SCR to FD as  $v_s$  tends to reverse. At the same time, SCR

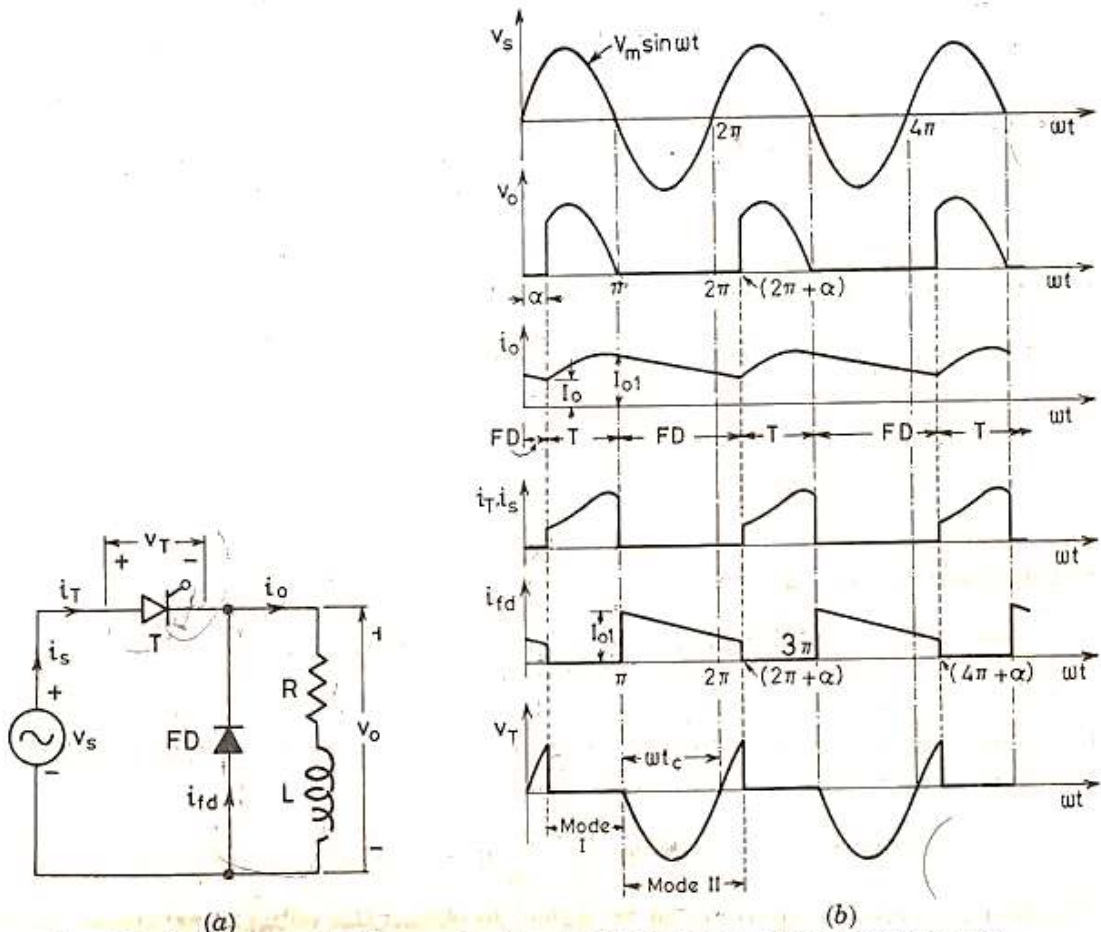


Fig. 6.3. Single-phase half-wave circuit with RL load and a freewheeling diode, (a) circuit diagram and (b) voltage and current waveforms.

is subjected to reverse voltage and zero current, it is therefore turned off at  $\omega t = \pi$ . It is assumed that during freewheeling period load current does not decay to zero until the SCR is triggered again at  $(2\pi + \alpha)$ . Voltage drop across FD is taken as almost zero, the load voltage  $v_0$  is, therefore, zero during the freewheeling period. The voltage variation across SCR is shown as  $v_T$  in Fig. 6.3 (b). It is seen from this wave-form that SCR is reverse biased from  $\omega t = \pi$  to  $\omega t = 2\pi$ . Therefore, circuit turn-off time is

$$t_C = \frac{\pi}{\omega} \text{ sec}$$

The source current  $i_s$  and thyristor current  $i_T$  have the same waveform as shown.

Operation of the circuit of Fig. 6.3 (a) can be explained in two modes. In the first mode, called *conduction mode*, SCR conducts from  $\alpha$  to  $\pi$ ,  $2\pi + \alpha$  to  $3\pi$  and so on and FD is reverse biased. The duration of this mode is for  $[(\pi - \alpha)/\omega]$  sec. Let the load current at the beginning of mode I be  $I_0$ . The expression for current  $i_0$  in mode I can be obtained as follows :

*Mode I* : For conduction mode, the voltage equation is

$$V_m \sin \omega t = Ri_0 + L \frac{di_0}{dt}$$

Its solution, already obtained in the previous section, is repeated here from Eq. (6.6) as

$$i_0 = \frac{V_m}{Z} \sin (\omega t - \phi) + A e^{-1(R/L)t}$$

At  $\omega t = \alpha$ ,  $i_0 = I_0$ , i.e. at  $t = \frac{\alpha}{\omega}$ ,  $i_0 = I_0$

Note that for mode I,  $\alpha \leq \omega t \leq \pi$

*Mode II* : This mode, called freewheeling mode, extends from  $\pi$  to  $2\pi + \alpha$ ,  $3\pi$  to  $4\pi + \alpha$  and so on. In this mode, SCR is reverse biased from  $\pi$  to  $2\pi$ ,  $3\pi$  to  $4\pi$ ... as shown by voltage waveform  $v_T$  in Fig 6.3 (b). As the load current is assumed continuous, FD conducts from  $\pi$  to  $(2\pi + \alpha)$ ,  $3\pi$  to  $(4\pi + \alpha)$  and so on. Let the current at the beginning of mode II be  $I_{01}$  as shown. As load current is passing through FD, the voltage equation for mode II is

$$0 = Ri_0 + L \frac{di_0}{dt}$$

Its solution is

$$i_0 = A e^{-(R/L)t}$$

At  $\omega t = \pi$ ,

$$i_0 = I_{01}$$

It gives

$$A = I_{01} e^{R\pi/\omega L}$$

$\therefore$

$$i_0 = I_{01} \cdot \exp \left[ -\frac{R}{L} \left( t - \frac{\pi}{\omega} \right) \right] \quad \dots(6.12)$$

Note that for mode II,

$$\pi < \omega t \leq (2\pi + \alpha)$$

Average load voltage  $V_0$  from Fig. 6.3 (b) is given by

$$V_0 = \frac{1}{2\pi} \int_{\alpha}^{\pi} V_m \sin \omega t d(\omega t) = \frac{V_m}{2\pi} (1 + \cos \alpha) \quad \dots(6.13)$$



## 2,3 Understand need of freewheeling diode

$$\text{Average load current, } I_0 = \frac{V_0}{R} = \frac{V_m}{2\pi R} (1 + \cos \alpha) \quad \dots(6.14)$$

Note that load current  $i_0$  is contributed by SCR from  $\alpha$  to  $\pi$ ,  $(2\pi + \alpha)$  to  $3\pi$  and so on and by FD from  $0$  to  $\alpha$ ,  $\pi$  to  $(2\pi + \alpha)$  and so on. Thus the waveshape of thyristor current  $i_T$  is identical with the waveshape of  $i_0$  for  $\omega t = \alpha$  to  $\pi$ ,  $(2\pi + \alpha)$  to  $3\pi$  and so on. Similarly, the waveshape of FD current  $i_{fd}$  is identical with the waveform of  $i_0$  for  $\omega t = 0^\circ$  to  $\alpha$ ,  $\pi$  to  $(2\pi + \alpha)$  and so on.

In Fig. 6.2, load consumes power  $p_1$  from source for  $\alpha$  to  $\pi$  (both  $v_0$  and  $i_0$  are positive) whereas energy stored in inductance  $L$  is returned to the source as power  $p_2$  for  $\pi$  to  $\beta$  ( $v_0$  is negative and  $i_0$  is positive). As a result, net power consumed by the load is the difference of these two powers  $p_1$  and  $p_2$ . In Fig. 6.3, load absorbs power for  $\alpha$  to  $\pi$ , but for  $\pi$  to  $(2\pi + \alpha)$ , energy stored in  $L$  is delivered to load resistance  $R$  through the FD. As a consequence, power consumed by load is more in Fig. 6.3. It can, therefore, be concluded that power delivered to load, for the same firing angle, is more when FD is used. As volt-ampere input is almost the same in both Figs. 6.2 and 6.3, the input  $pf$  (= power delivered to load/input volt-ampere) with the use of FD is improved.

It is also seen from Figs. 6.2 (b) and 6.3 (b) that load current waveform is improved with FD in Fig. 6.3 (b). Thus the advantages of using freewheeling diode are

- (i) input  $pf$  is improved
- (ii) load current waveform is improved and
- (iii) as a result of (ii), load performance is better.

It may be seen from Fig. 6.3 (b) that freewheeling diode prevents the load voltage  $v_0$  from becoming negative. Whenever load voltage tends to go negative, FD comes into play. As a result, load current is transferred from main thyristor to FD, allowing the thyristor to regain its forward blocking capability.

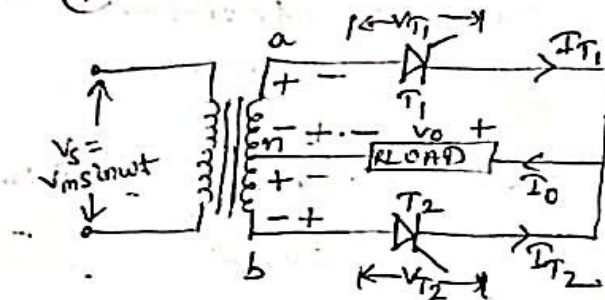
It is seen from Figs. 6.2 (b) and 6.3 (b) that supply current  $i_s$  taken from the source is unidirectional and is in the form of dc pulses. Single phase half-wave converter thus introduces a dc component into the supply line. This is undesirable as it leads to saturation of the supply transformer and other difficulties (harmonics etc.).

These shortcomings can be overcome to some extent by the use of single-phase fullwave circuits discussed in Art. 6.2.



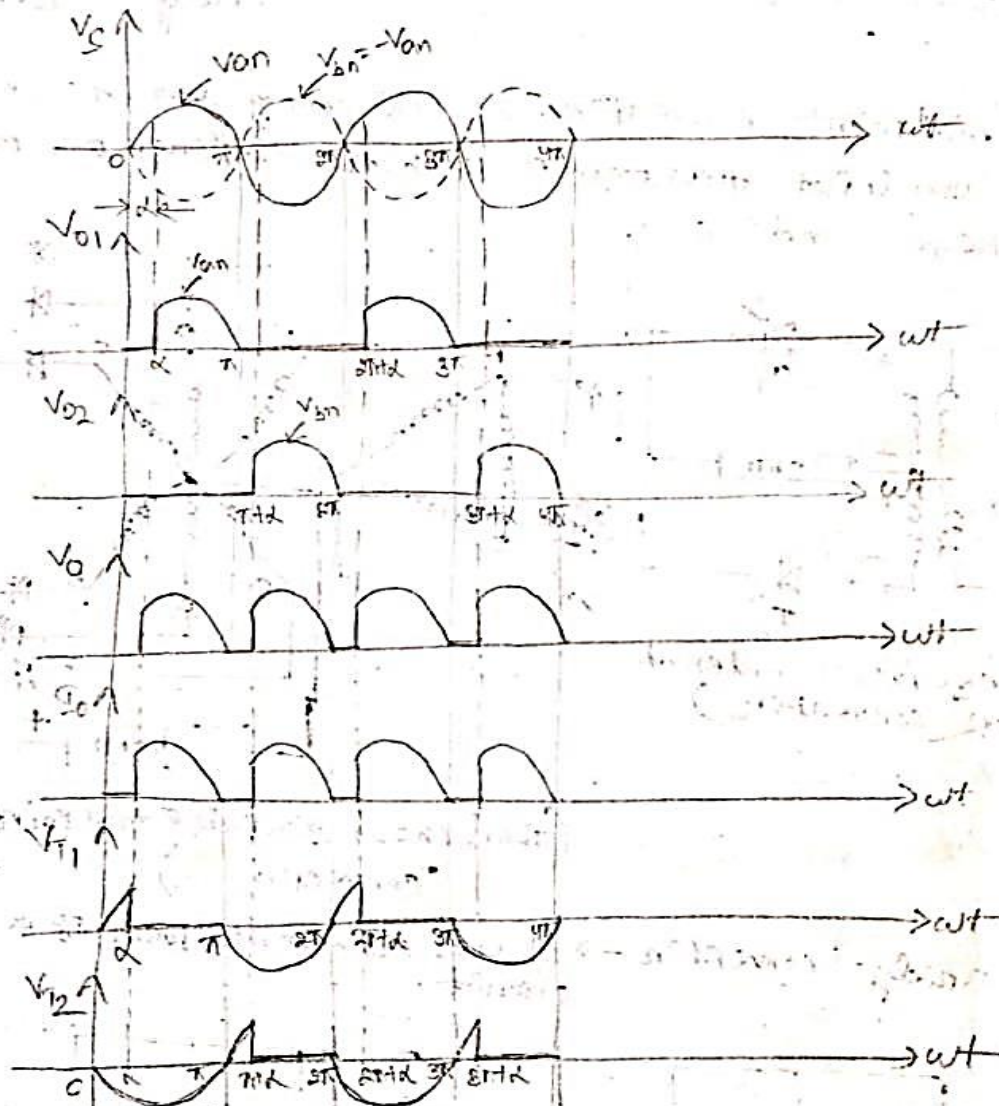
## 2.4 Single phase Fully Controlled Converter

① midraht type with R load  $\rightarrow$



$$V_{an} = V_{nb}$$

$$V_{an} = -V_{on}$$



operation  $\rightarrow$

During positive half cycle,

a tie w.r.t b,  $V_{an}$  is in forward path

$V_{bn}$  is in reverse path

anode of  $T_1$  is tie, cathode is -ve.

At  $\omega t = \alpha$ ,  $T_1$  is turned ON

$T_2$  remains OFF

$I_0 = I_{T1}$ , flows in the tie direction

$V_0 = V_{01}$ , forwards in the tie direction

Here  $T_1$  is called incoming SCR and

$T_2$  is outgoing SCR.

During -ve half cycle,

a -ve w.r.t b,  $V_{an}$  is in reverse path

$V_{bn}$  is in forward path

anode of  $T_1$  is -ve and cathode is tie.

$\omega t = \pi$  to  $(\pi + \alpha)$ ,  $I_0 = 0$ ,  $V_0 = 0$

$\omega t = (\pi + \alpha)$ ,  $T_1$  is OFF and  $T_2$  is ON

$I_0 = I_{T2}$  flows in the tie direction

$V_0 = V_{02}$  forwards in the tie direction

$t_c = \frac{\pi}{\omega}$  sec.

$$V_0 = \frac{1}{2\pi} \int_{\alpha}^{\pi} V_m \sin \omega t d\omega t$$

$$V_0 = \frac{V_m}{\pi} (1 + \cos \alpha)$$

$$I_0 = \frac{V_0}{R} = \frac{V_m}{\pi R} (1 + \cos \alpha)$$

## Single Phase Full wave bridge converter →

3 types ① uncontrolled converters:- uses only diodes and the level of dc o/p voltage cannot be controlled.

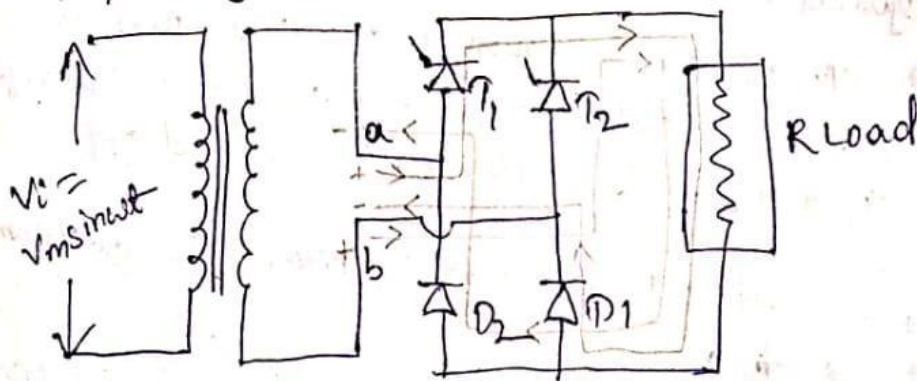
② half controlled converters:- uses mixture of diodes and thyristors or semi converters

and there is a limited control over the level of dc o/p voltage.

③ A fully controlled converter or full converter :- uses thyristors

only and there is wider control over the level of dc o/p voltage.

## Half controlled bridge rectifier with R Load → 1 $\phi$ bridge type semi converter (R load)



$$V_o = \frac{V_m}{\pi} (1 + \cos \alpha)$$

$$I_o = \frac{V_o}{R} = \frac{V_m}{\pi R} (1 + \cos \alpha)$$

During 1st half cycle,

a +ve w.r.t b,  $T_1, D_1$  are forward biased

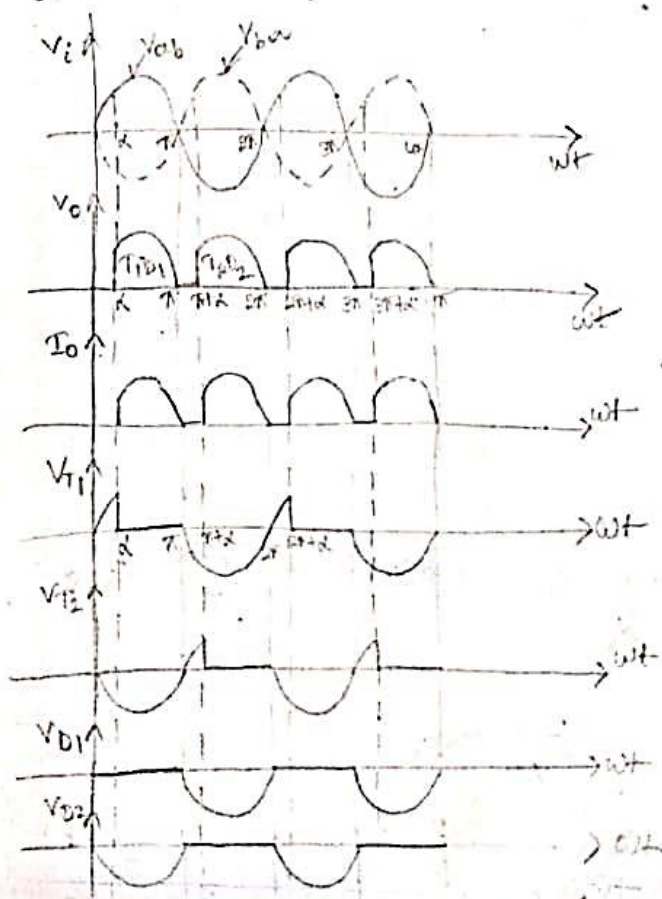
At  $\omega t = \alpha$ ,  $T_1$  is fired,  $v_o$  follows the i/p. Here  $T_1$  is called the incoming SCR and  $D_1$  is called incoming diode. During  $\alpha \rightarrow \pi$ ,  $T_1, D_1$  conducts load current. At  $\omega t = \pi$ , due to line commutation  $T_1$  stops conducting.

During 2nd half cycle,

a -ve w.r.t b,  $T_2, D_2$  are forward biased

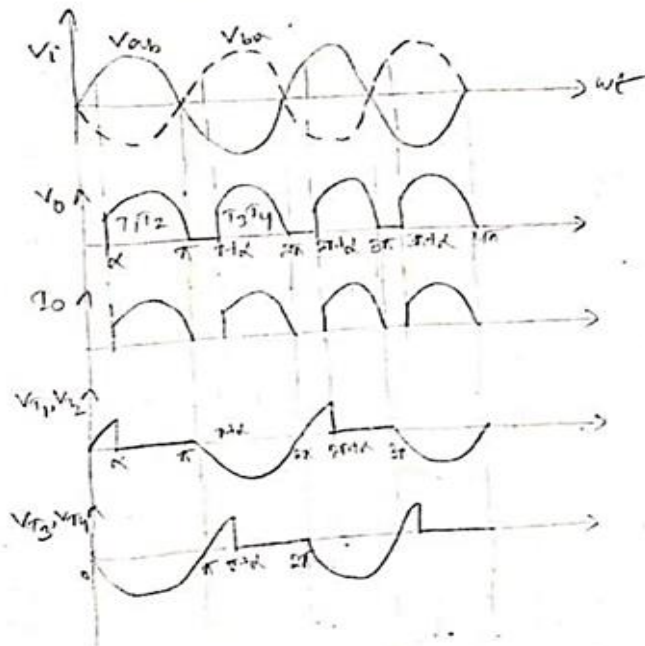
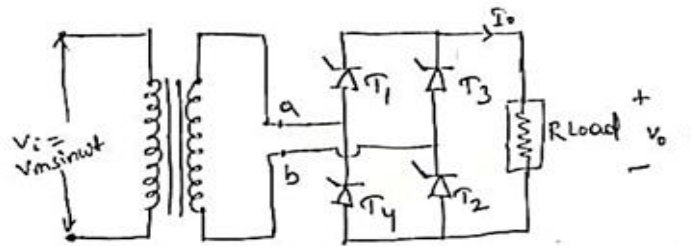
At  $\omega t = \pi + \alpha$ ,  $T_2$  is fired & starts conducting. Here  $T_1, D_1$  are outgoing SCR and diode and  $T_2, D_2$  are incoming SCR and diode respectively.

During  $(\pi + \alpha) \rightarrow 2\pi$ ,  $T_2, D_2$  conducts the load current.





Fully controlled bridge rectifier with R-load  $\rightarrow$



$$V_o = \frac{V_m}{\pi} (1 + \cos \alpha)$$

$$I_o = \frac{V_o}{R} = \frac{V_m}{\pi R} (1 + \cos \alpha)$$

$$t_c = \frac{\pi}{\omega} \text{ sec.}$$

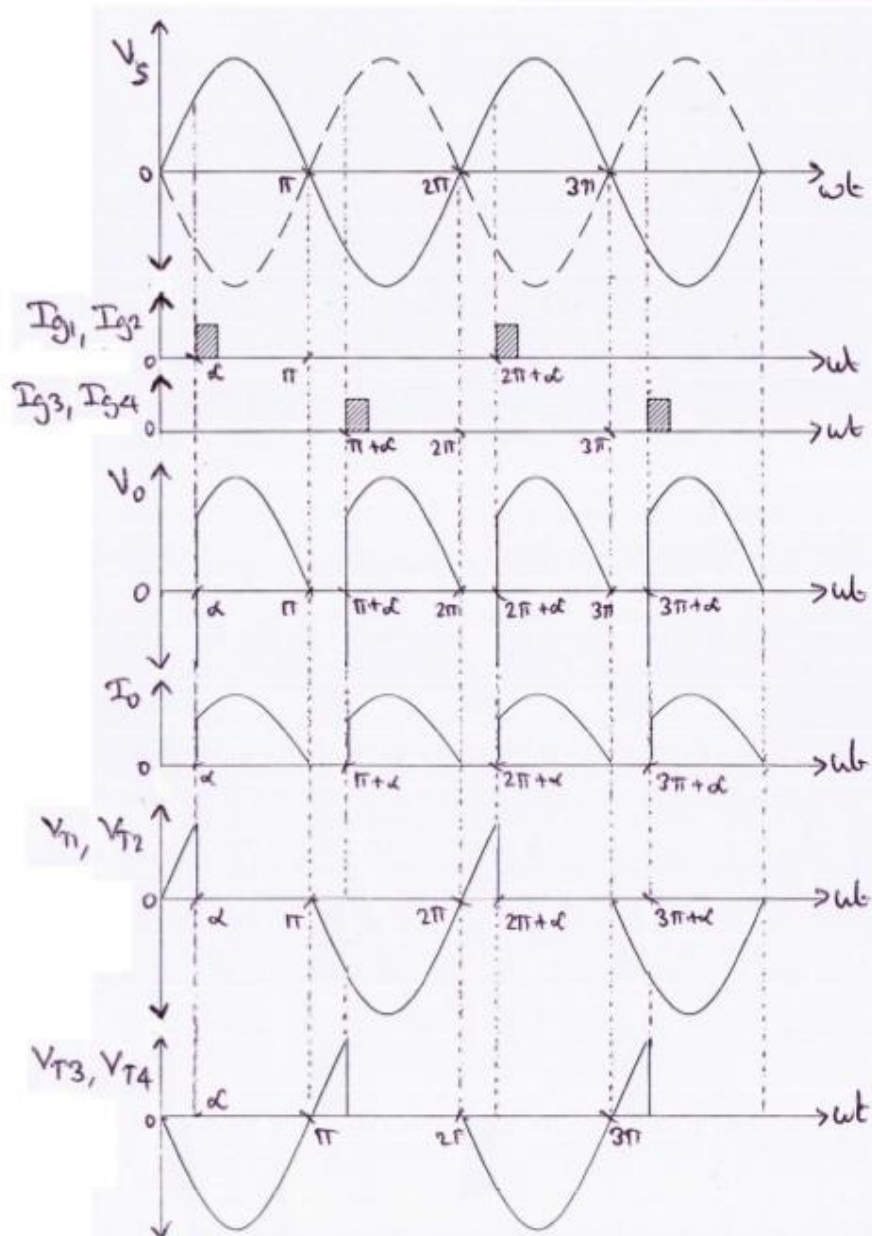
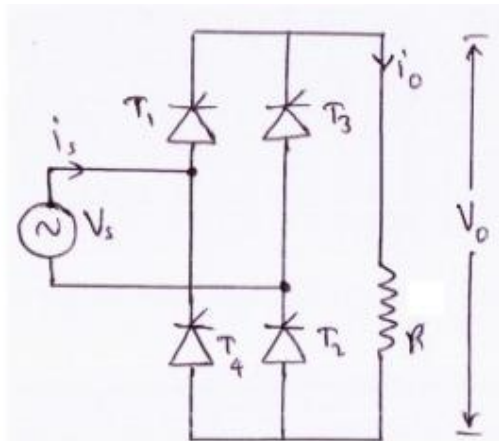
Operation  $\rightarrow$

During first half cycle, a is the w.r.t b.  
 From  $\omega t = 0 \rightarrow \alpha$ ,  $T_1, T_2$  are forward biased but not conduct.  $V_o = 0$ . At  $\omega t = \alpha$ ,  $T_1, T_2$  are triggered.  
 $T_1$  and  $T_2$  starts conducting,  $T_3, T_4$  will be off.

# 1 $\phi$ full wave bridge converter

(bulky controlled)

R - LOAD



during second half cycle,

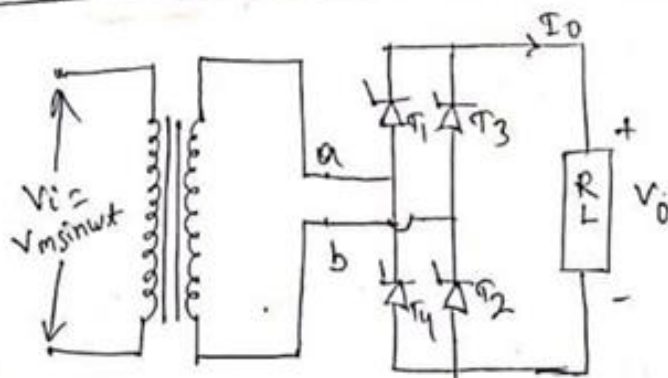
b is +ve w.r.t a,  $T_3, T_4$  forward biased but not conducts  
 $T_1, T_2$  stop conducting due to line commutation.

→ Line commutation technique called as natural commutation uses reverse voltage for turning off a thyristor i.e. in this type of rectifier by applying reverse bias across the thyristor and by reducing the anode current level below the holding current level we can turn off the thyristor.

from  $\omega t = \pi \rightarrow (\pi + \alpha)$ ,  $T_1, T_2$  will be OFF.  $T_3, T_4$  not conduct due to absence of gate signal

from  $\omega t = (\pi + \alpha) \rightarrow 2\pi$ ,  $T_3$  and  $T_4$  are triggered,  $T_1, T_2$  will be OFF.  $T_3$  and  $T_4$  conduct due to gate signal. In this way the process goes on.

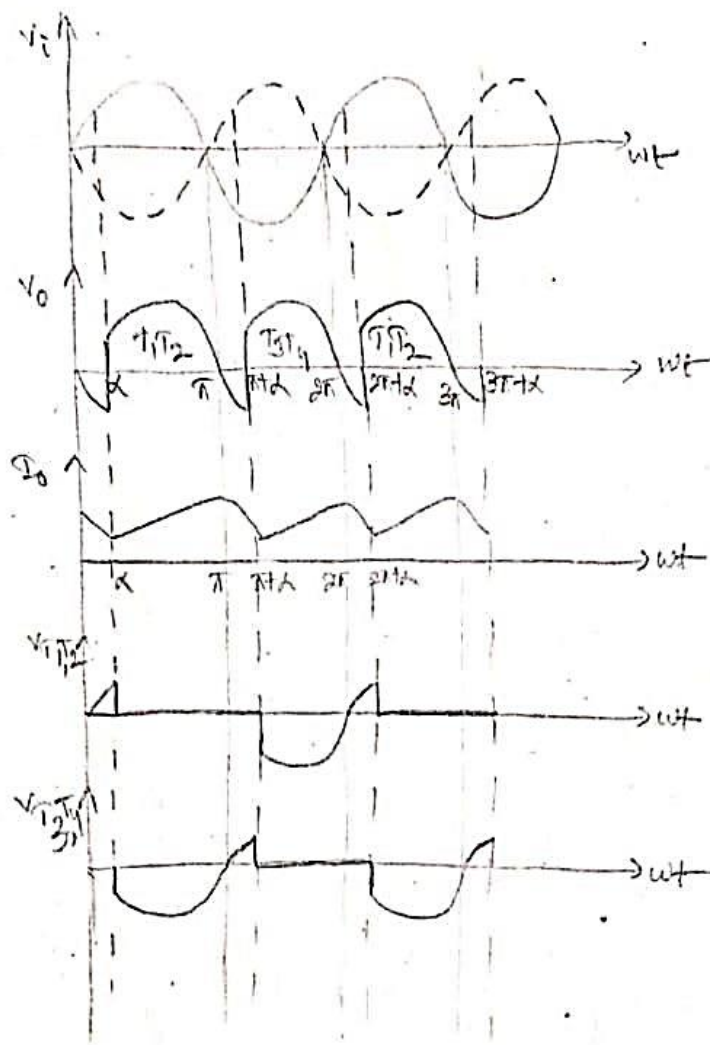
Fully controlled bridge rectifier with RL load →



operation →

During first half cycle, a is +ve w.r.t b,

from  $\omega t = 0 \rightarrow \alpha$ ,  $T_1$  and  $T_2$  are forward biased but not



During second half cycle, b +ve w.r.t a,

At  $\omega t = \pi \rightarrow (\pi + \alpha)$ ,  $v_o$  follows  $v_i$  in reverse path.  $T_3$  and  $T_4$  are forward biased but not conducting.  $T_1$  and  $T_2$  still conduct due to load inductance.

At  $\omega t = \pi + \alpha$ ,  $T_3$  and  $T_4$  are triggered,  $T_1$  and  $T_2$  will be off.  $T_3$  and  $T_4$  starts conducting.

From  $\omega t = \pi + \alpha \rightarrow 2\pi$ ,  $T_3$  and  $T_4$  conduct.

During second first half cycle, a +ve w.r.t b,

$\omega t = 2\pi \rightarrow (2\pi + \alpha)$ ,  $T_3$  and  $T_4$  still conduct due to load inductance and here  $v_o$  follows  $v_i$  in reverse path.



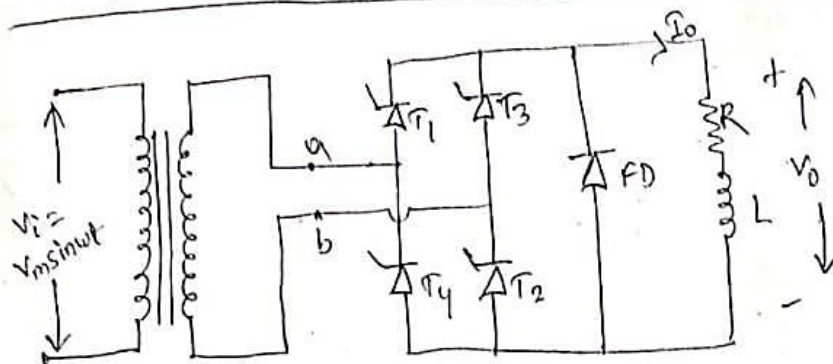
At  $\omega t = (2\pi k) \rightarrow 3\pi$ , again  $T_1$  and  $T_2$  are triggered and  $T_3$  and  $T_4$  conduct due to gate signal. Here  $T_3$  and  $T_4$  will be off, and the process continues.

$$V_0 = \frac{2V_m}{\pi} \cos \alpha$$

$$I_0 = \frac{V_0}{R} = \frac{2V_m}{\pi R} \cos \alpha$$

$$t_c = \frac{\pi - \alpha}{\omega} \text{ sec.}$$

Fully controlled bridge rectifier with RL and flywheel diode  $\rightarrow$



$$V_0 = \frac{V_m}{\pi} (1 + \cos \alpha)$$

$$I_0 = \frac{V_m}{\pi R} (1 + \cos \alpha)$$

$$t_c = \frac{\pi}{\omega} \text{ sec.}$$

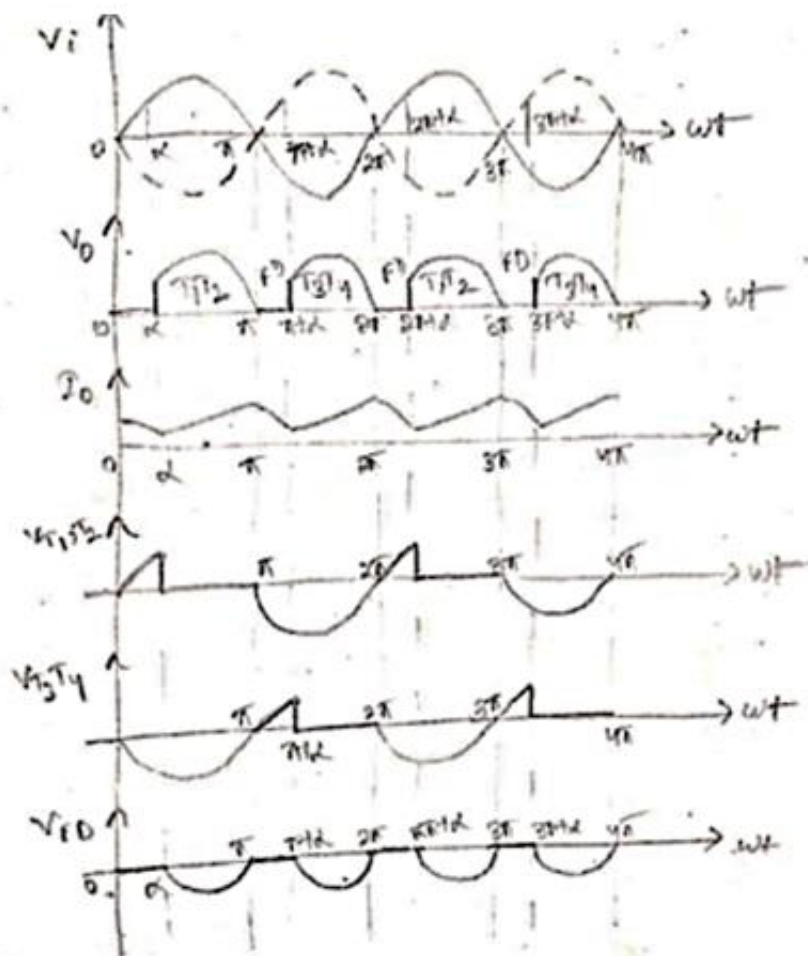
operation  $\rightarrow$

$V_i =$  i/p voltage

$V_o =$  o/p voltage

$I_0 =$  current flowing through load

$V_{T1}, V_{T2}, V_{T3}, V_{T4}$  are voltages across thyristors  $T_1, T_2, T_3, T_4$ .  
FD flywheel diode.



### operation $\rightarrow$

The operation of 1 $\phi$  fully controlled bridge rectifier with  $RL$  load and  $FD$  is similar to that of half controlled bridge rectifier feeding  $RL$  load with  $FD$ .

$\omega t = 0 \rightarrow \alpha$   $V_o = 0$ ,  $I_o$  falls from its peak value,  
 $V_{FD} = 0$

$\omega t = \alpha \rightarrow \pi$   $V_o$  follows  $V_i$  in forward path,  $I_o$  rises towards the peak.  $V_{FD}$  follows  $V_i$  in reverse path.

$\omega t = \pi \rightarrow \pi + \alpha$   $V_o = 0$ ,  $I_o$  falls from its peak value.  
 $V_{FD} = 0$

$\omega t = \pi + \alpha \rightarrow 2\pi$   $V_o$  follows  $V_i$  in forward path,  $I_o$  rises towards the peak.  $V_{FD}$  follows  $V_i$  in reverse path.

now  $\omega t = 2\pi \rightarrow (2\pi + \alpha)$  and

$\omega t = (2\pi + \alpha) \rightarrow 3\pi$  the process continues.

## 2.5 Three phase half wave Controlled Converter with resistive load

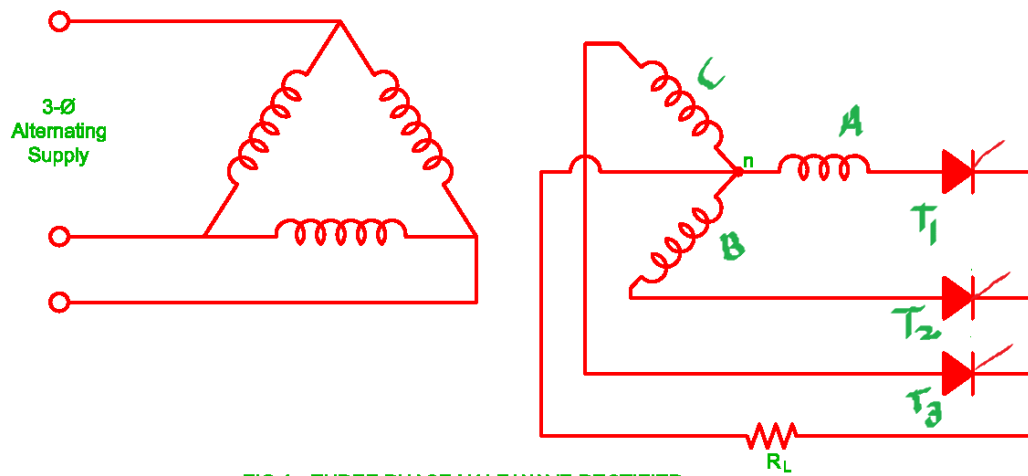


FIG A : THREE PHASE HALF WAVE RECTIFIER

For a 3 - phase half-wave controlled rectifier shown in Fig. A, the input phase voltages  $V_a$ ,  $V_b$ ,  $V_c$  have same amplitude and frequency with  $120^\circ$  phase shift as shown in Fig.2.

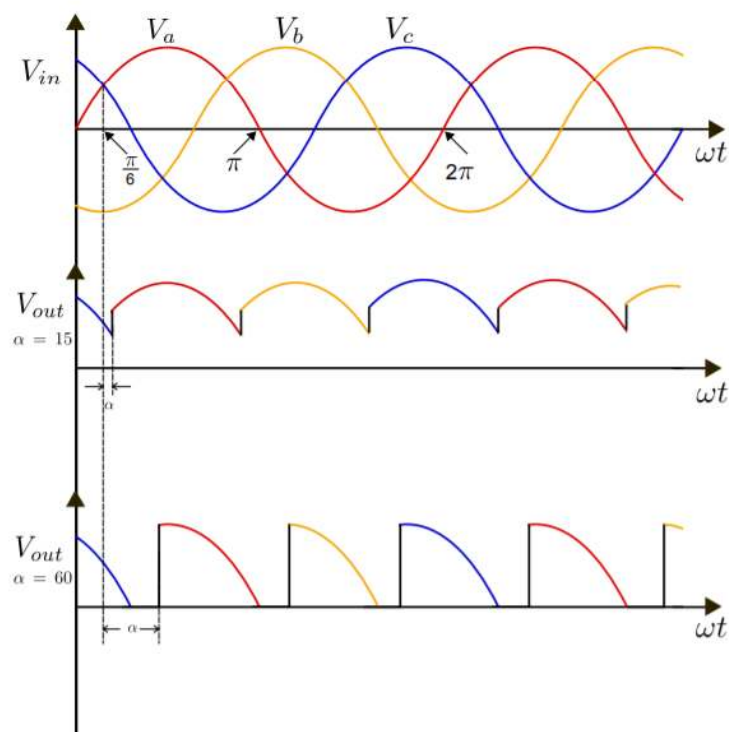
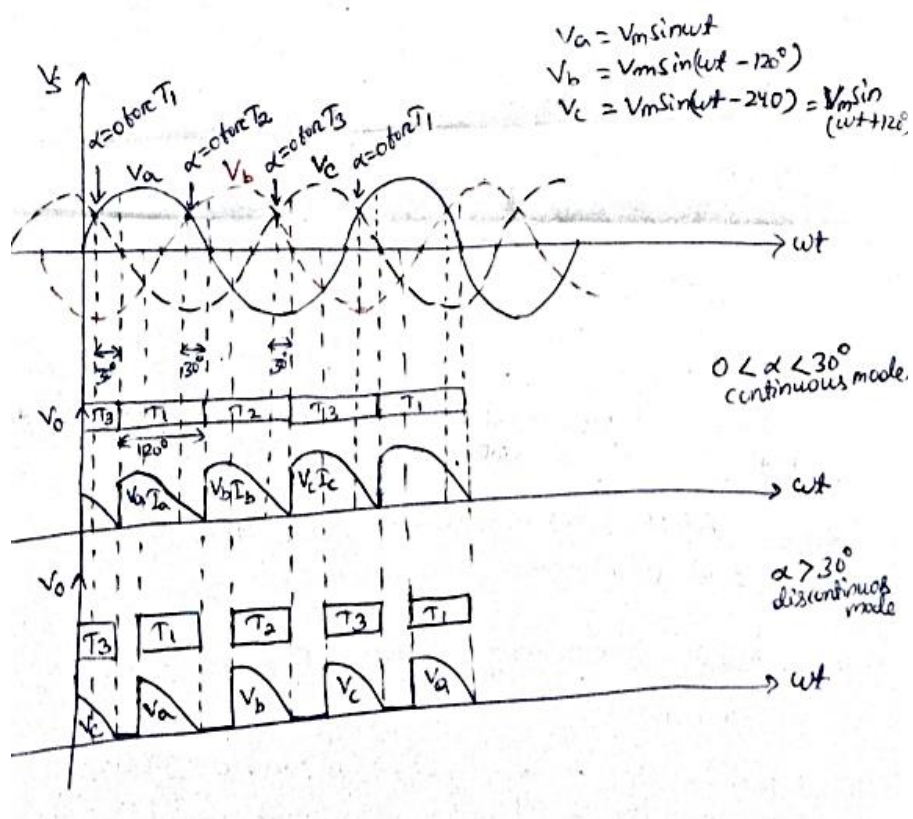
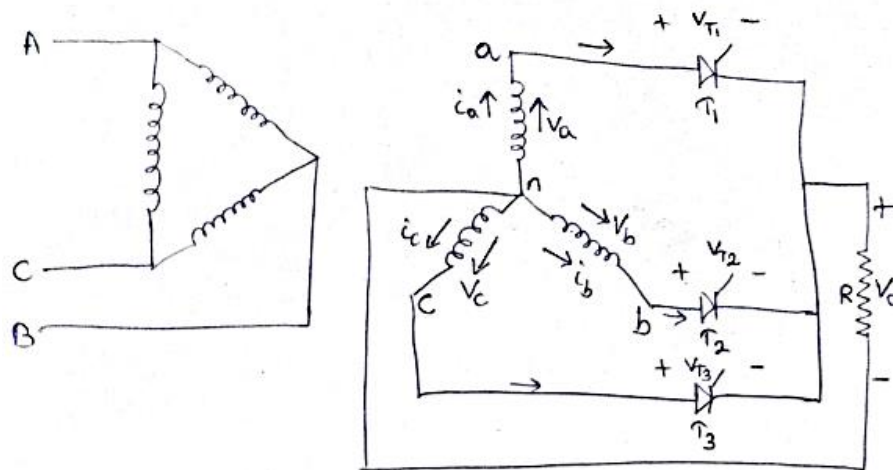


Figure 2: Output voltage waveform of 3 phase half-wave controlled rectifier



This converter is called 3-phase 3-pulse converter or 3-phase M-3 converter.

With reference to the above circuit diagram and waveforms, if firing angle is zero-degree, SCR T1 would begin conducting from  $\omega t = 30^\circ$  to  $150^\circ$ , T2 from  $\omega t = 150^\circ$  to  $270^\circ$  and T3 from  $\omega t = 270^\circ$  to  $390^\circ$  and so on. In other words, firing angle for this controlled converter would be measured from  $\omega t = 30^\circ$  for T1, from  $\omega t = 150^\circ$  for T2 and from  $\omega t = 270^\circ$  for T3. For zero degree firing

angle delay thyristor behaves as a diode. The operation of this converter is now described for  $\alpha < 30^\circ$  and for  $\alpha > 30^\circ$ .

Firing angle  $< 30^\circ$ ,

The output voltage waveform for firing angle less than  $30^\circ$  (say around  $30^\circ$ ) is sketched, where T1 conducts from  $\omega t = 30^\circ + \alpha$  to  $\omega t = 150^\circ + \alpha$ , T2 conducts from  $\omega t = 150^\circ + \alpha$  to  $\omega t = 270^\circ + \alpha$ , T3 conducts from  $\omega t = 270^\circ + \alpha$  to  $\omega t = 390^\circ + \alpha$  and so on. Each SCR conducts for 120 degrees. The waveform of load current would be identical with voltage waveform.

Average value of output voltage

$$V_0 = \frac{3\sqrt{3}}{2\pi} V_{mp} \cos \alpha$$

$$V_0 = \frac{3}{2\pi} V_{ml} \cos \alpha$$

Where  $V_{mp}$  = maximum value of phase voltage

$V_{ml}$  = maximum value of line voltage =  $\sqrt{3} V_{mp}$

$\alpha$  = firing angle

$$I_0 = \frac{V_0}{R} = \frac{3}{2\pi R} V_{ml} \cos \alpha$$

Firing angle  $> 30^\circ$ ,

When firing angle is more than  $30^\circ$ , T1 conducts from  $\omega t = 30^\circ + \alpha$  to  $\omega t = 180^\circ$ , T2 conducts from  $\omega t = 150^\circ + \alpha$  to  $\omega t = 300^\circ$ , T3 conducts from  $\omega t = 270^\circ + \alpha$  to  $\omega t = 420^\circ$  and so on. For R load when phase voltage  $V_0$  reaches zero at  $\omega t = 180^\circ$ , current  $i_0 = 0$ , T1 is therefore turned off. Thus, T1 would conduct from  $\omega t = 30^\circ + \alpha$  to  $\omega t = 180^\circ$ . Same is true for other SCRs. This shows that each SCR for Firing angle  $> 30^\circ$  conducts for  $(150^\circ - \alpha)$  only. This also implies that for R load maximum possible value of firing angle is  $150^\circ$ . The waveform of load current would be identical with voltage waveform.

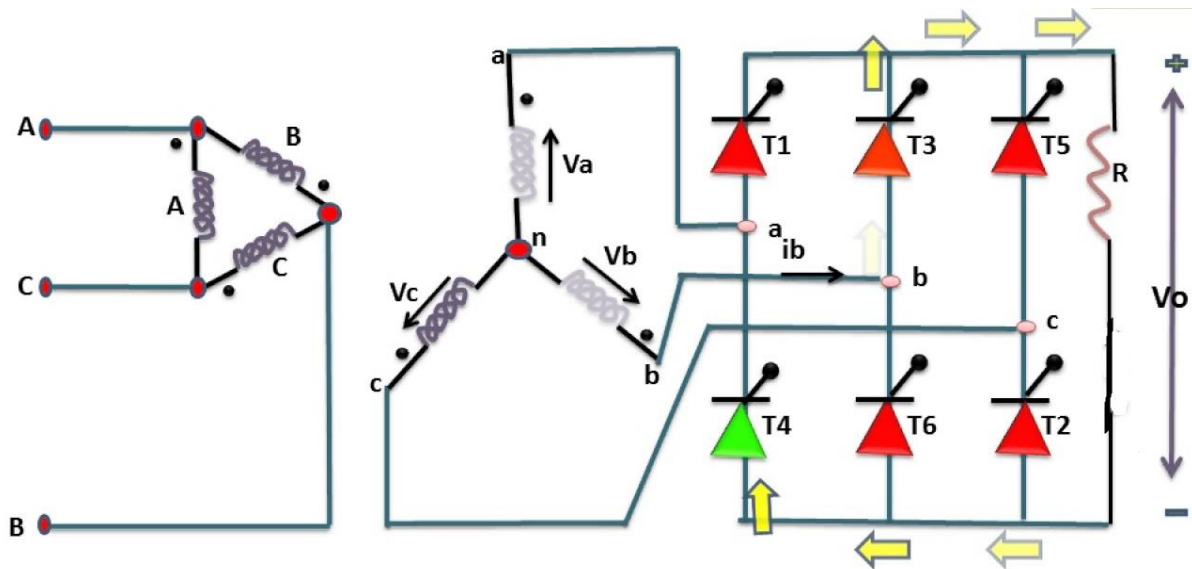
Average value of output voltage

$$V_0 = \frac{3}{2\pi} V_{mp} [1 + \cos(\alpha + 30^\circ)]$$

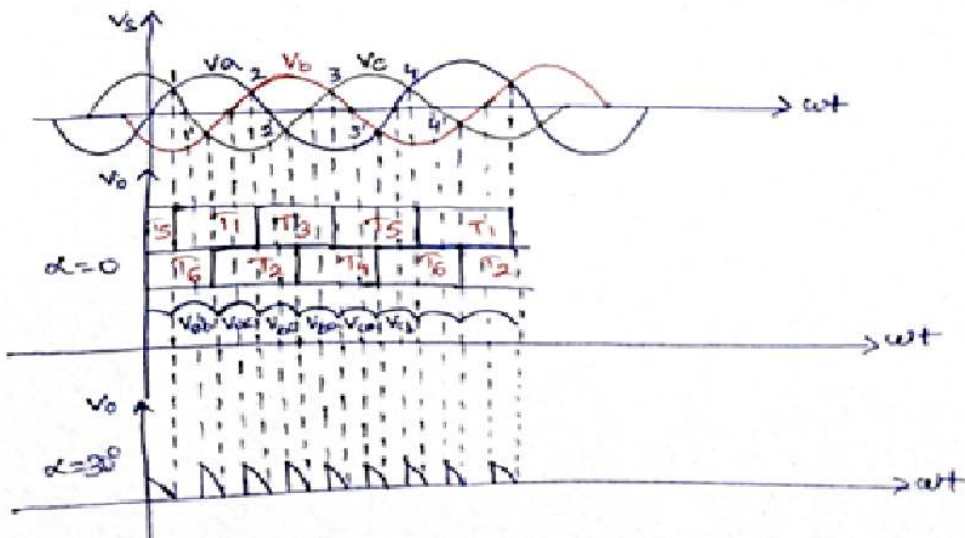
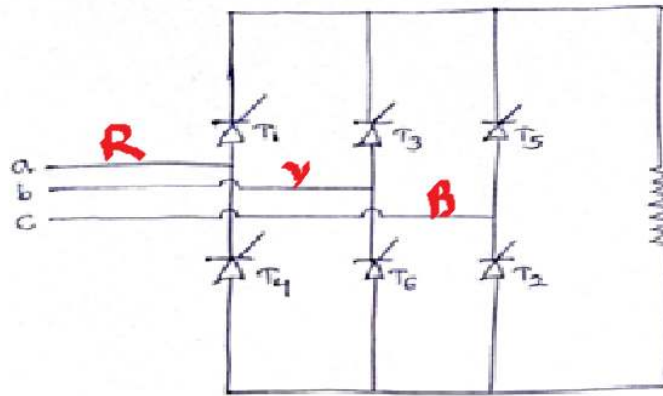
Where  $V_{mp}$  = maximum value of phase voltage

$\alpha$  = firing angle

## 2.6 Three phase fully Controlled Converter with resistive load







**(3-phase 6-pulse)**

The three-phase bridge rectifier circuit has three-legs, each phase connected to one of the three phase voltages. Alternatively, it can be seen that the bridge circuit has two halves, the positive half consisting of the SCRs  $S_1$ ,  $S_3$  and  $S_5$  and the negative half consisting of the SCRs  $S_2$ ,  $S_4$  and  $S_6$ . At any time when there is current flow, one SCR from each half conducts. If the phase sequence of the source be RYB, the SCRs are triggered in the sequence  $S_1$ ,  $S_2$ ,  $S_3$ ,  $S_4$ ,  $S_5$ ,  $S_6$  and  $S_1$  and so on.

The operation of the circuit is first explained with the assumption that diodes are used in place of the SCRs. The three-phase voltages vary as shown below.

Let the three-phase voltages be defined as shown below.

$$v_R(\theta) = E^* \sin(\theta), \quad v_Y(\theta) = E^* \sin(\theta - 120^\circ), \quad \text{and} \quad v_B(\theta) = E^* \sin(\theta + 120^\circ).$$

It can be seen that the R-phase voltage is the highest of the three-phase voltages when  $q$  is in the range from  $30^\circ$  to  $150^\circ$ . It can also be seen that Y-phase voltage is the highest of the three-phase voltages when  $q$  is in the range from  $150^\circ$  to  $270^\circ$  and that B-phase voltage is the highest of the three-phase voltages when  $q$  is in the range from  $270^\circ$  to  $390^\circ$  or  $30^\circ$  in the next cycle. We also find that R-phase voltage is the lowest of the three-phase voltages when  $q$  is in the range from  $210^\circ$  to  $330^\circ$ . It can also be seen that Y-phase voltage is the lowest of the three-phase voltages when  $q$  is in the range from  $330^\circ$  to  $450^\circ$  or  $90^\circ$  in the next cycle, and that B-phase voltage is the lowest when  $q$  is in the range from  $90^\circ$  to  $210^\circ$ . If diodes are used, diode  $D_1$  in place of  $S_1$  would conduct from  $30^\circ$  to  $150^\circ$ , diode  $D_3$  would conduct from  $150^\circ$  to  $270^\circ$  and diode  $D_5$  from  $270^\circ$  to  $390^\circ$  or  $30^\circ$  in the next cycle. In the same way, diode  $D_4$  would conduct from  $210^\circ$  to  $330^\circ$ , diode  $D_6$  from  $330^\circ$  to  $450^\circ$  or  $90^\circ$  in the next cycle, and diode  $D_2$  would conduct from  $90^\circ$  to  $210^\circ$ . The positive rail of output voltage of the bridge is connected to the topmost segments of the envelope of three-phase voltages and the negative rail of the output voltage to the lowest segments of the envelope.

Period, range of $q$	SCR Pair in conduction
$30^\circ$ to $90^\circ$	$S_1$ and $S_6$
$90^\circ$ to $150^\circ$	$S_1$ and $S_2$
$150^\circ$ to $210^\circ$	$S_2$ and $S_3$
$210^\circ$ to $270^\circ$	$S_3$ and $S_4$
$270^\circ$ to $330^\circ$	$S_4$ and $S_5$
$330^\circ$ to $360^\circ$ and $0^\circ$ to $30^\circ$	$S_5$ and $S_6$

If SCRs are used, their conduction can be delayed by choosing the desired firing angle. When the SCRs are fired at  $0^\circ$  firing angle, the output of the bridge rectifier would be the same as that of the circuit with diodes. For instance, it is seen that  $D_1$  starts conducting only after  $q = 30^\circ$ . In fact, it can start conducting only after  $q = 30^\circ$ , since it is reverse-biased before  $q = 30^\circ$ . The bias across  $D_1$  becomes zero when  $q = 30^\circ$  and diode  $D_1$  starts getting forward-biased only after  $q = 30^\circ$ . When  $v_R(q) = E \sin(q)$ , diode  $D_1$  is reverse-biased before  $q = 30^\circ$  and it is forward-biased

when  $q > 30^\circ$ . When firing angle to SCRs is zero degree,  $S_1$  is triggered when  $q = 30^\circ$ . This means that if a synchronizing signal is needed for triggering  $S_1$ , that signal voltage would lag  $v_R(q)$  by  $30^\circ$  and if the firing angle is  $\alpha$ , SCR  $S_1$  is

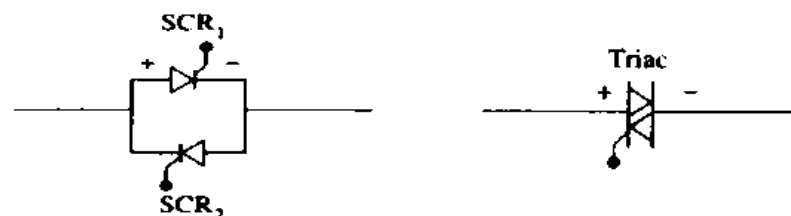


triggered when  $q = a + 30^\circ$ . Given that the conduction is continuous, the following table presents the SCR pair in conduction at any instant.

Period, range of $q$	SCR Pair in conduction
$a + 30^\circ$ to $a + 90^\circ$	$S_1$ and $S_6$
$a + 90^\circ$ to $a + 150^\circ$	$S_1$ and $S_2$
$a + 150^\circ$ to $a + 210^\circ$	$S_2$ and $S_3$
$a + 210^\circ$ to $a + 270^\circ$	$S_3$ and $S_4$
$a + 270^\circ$ to $a + 330^\circ$	$S_4$ and $S_5$
$a + 330^\circ$ to $a + 360^\circ$ and $a + 0^\circ$ to $a + 30^\circ$	$S_5$ and $S_6$

## 2.7 SINGLE PHASE AC REGULATOR OR CONTROLLER – PHASE ANGLE CONTROL

- AC voltage controllers are thyristor based devices which convert fixed alternating voltage directly to variable alternating voltage without change in frequency.
- Using these controllers, rms value of the voltage across the load is steplessly varied from a maximum value to zero.
- The simplest way to control AC voltage to the load is by using AC switch (bidirectional).
- The bi-directional conducting property can be achieved by simply connecting two unidirectional thyristors in inverse parallel to each other.



- AC voltage controllers are naturally commutated

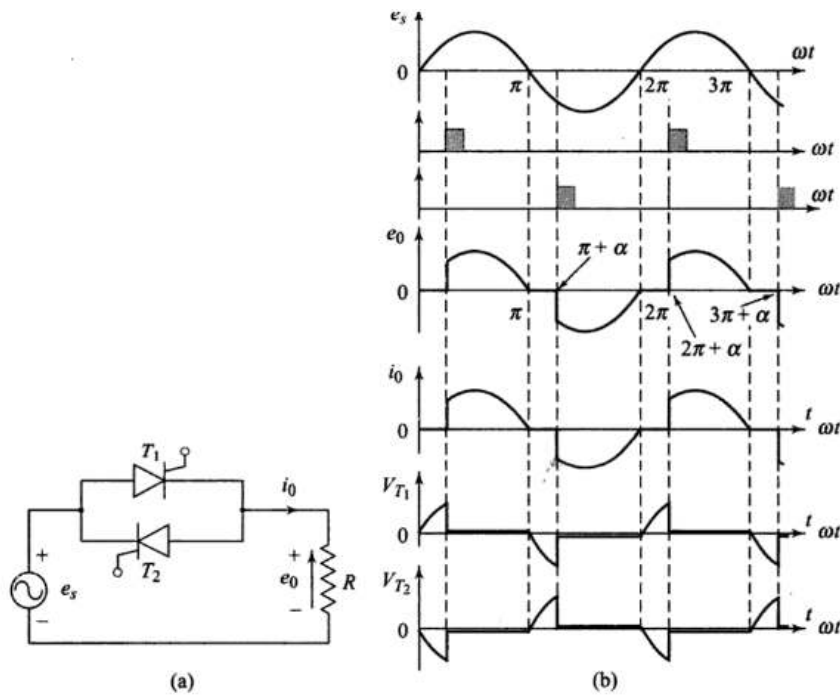
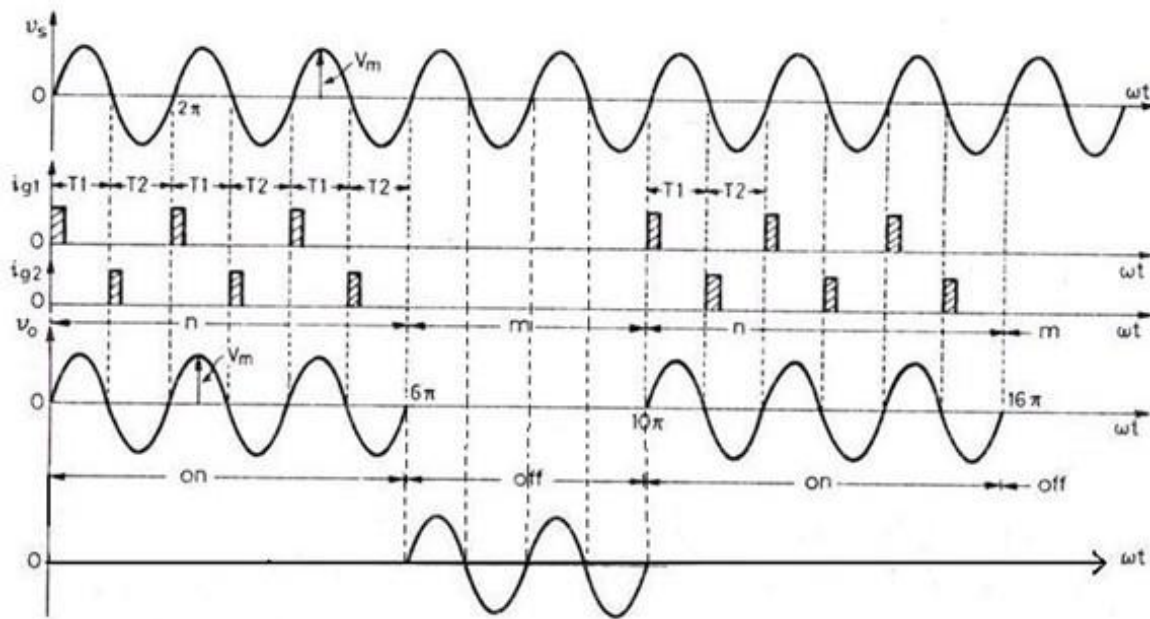


Fig.1 (a) Single-phase a.c. voltage controller with R load (b) voltage and current waveforms

Thyristors  $T_1$  and  $T_2$  are forward biased during positive and negative half-cycle, respectively. During positive half-cycle,  $T_1$  is triggered at a firing angle  $\alpha$ .  $T_1$  starts conducting and source voltage is applied to load from  $\alpha$  to  $\pi$ . At  $\pi$ , both  $e_0$ ,  $i_0$  fall to zero. Just after  $\pi$ ,  $T_1$  is subjected to reverse bias and it is, therefore, turned-off. During negative half-cycle,  $T_2$  is triggered at  $(\pi + \alpha)$ .  $T_2$  conducts from  $(\pi + \alpha)$  to  $2\pi$ . Soon after  $2\pi$ ,  $T_2$  is subjected to a reverse bias and it is, therefore, commutated. Load and source currents have the same waveform.

From zero to  $\alpha$ ,  $T_1$  is forward biased, therefore  $V_{T1} = e_s$  as shown in Fig.1.b. From  $\alpha$  to  $\pi$ ,  $T_1$  conducts,  $V_{T1}$  is therefore about 1 V. After  $\pi$ ,  $T_1$  is reverse biased by source voltage, therefore,  $V_{T1} = e_s$  from  $\pi$  to  $(\pi + \alpha)$ . The voltage variation  $V_{T1}$  across  $T_1$  is shown in Fig.1.b. Similarly, the variation of voltage  $V_{T2}$  across thyristor  $T_2$  can be drawn. In Fig.1.b, voltage drop across thyristors  $T_1$  and  $T_2$  is purposely shown just to highlight the duration of reverse bias across  $T_1$  and  $T_2$ . Examination of this figure reveals that for any value of  $\alpha$ , each thyristor is reverse biased for  $\pi/\omega$  seconds.

## SINGLE PHASE AC REGULATOR OR CONTROLLER – INTEGRAL CYCLE CONTROL



### 1- On-Off Control (Integral Cycle Control)

The load power can be controlled by connecting the source to the load for few complete cycles then disconnecting the source from the load for another number of cycles, and repeating the switching cycle.

Suitable for systems with large time constants.

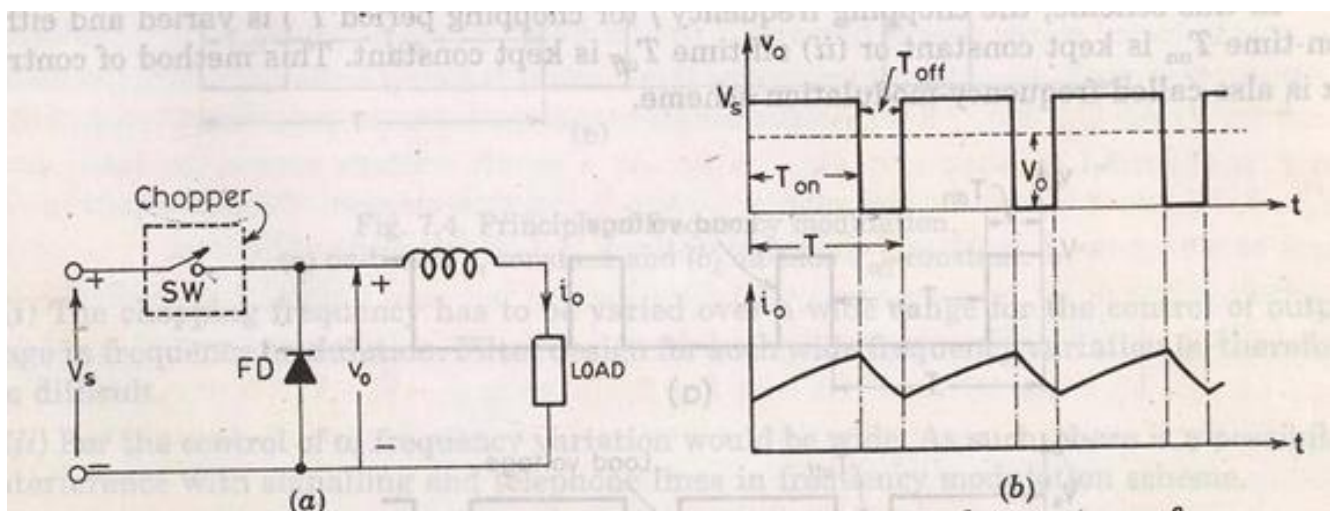
Average power to the load can be varied from 0% through 100%

Integral cycle control finds applications in heating loads and for motor speed control.

## 2.8 STEP UP & STEP-DOWN CHOPPER

### STEP DOWN CHOPPER

A chopper is a static device that converts fixed DC input voltage to variable output voltage directly. Chopper are mostly used in electric vehicle, mini haulers. Chopper are used for speed control and braking. The systems employing chopper offer smooth control, high efficiency and have fast response.



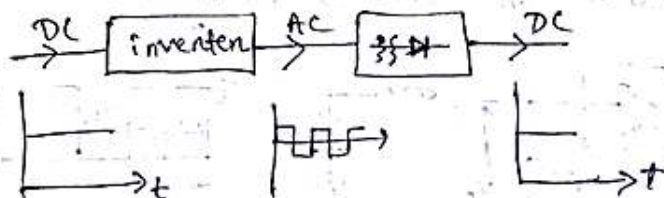
- Chopper is a static device that converts fixed dc i/p voltage to a variable dc o/p voltage directly.
- Chopper is a high speed on-off semiconductor switch that converts fixed dc input voltage to a variable dc o/p voltage by connecting source to load and disconnecting the load from source at a fast speed.

### Application

- subway cars
- trolley buses, trolley cars
- battery operated vehicles
- battery charging
- marine hoists
- forklift trucks
- mine haulers
- Electric automobiles speed control & braking

### AC link chopper

Here first dc is converted to ac by inverter. Ac is then stepped up or <sup>stepped</sup> down by a transformer which is then converted back to dc by a diode rectifier. Here conversion is in two stages (dc  $\rightarrow$  ac & ac  $\rightarrow$  dc) so this chopper is costly & less efficient.



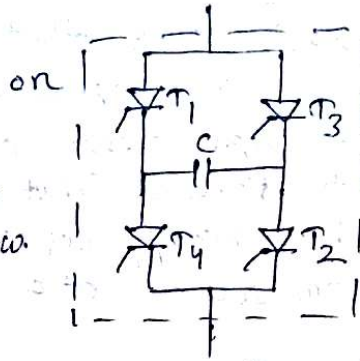
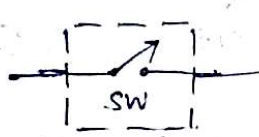
### DC chopper

A chopper is a static device that converts fixed dc i/p voltage to variable dc o/p voltage directly.





Chopper represented by

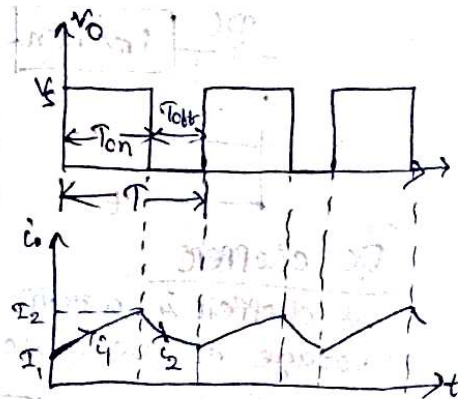
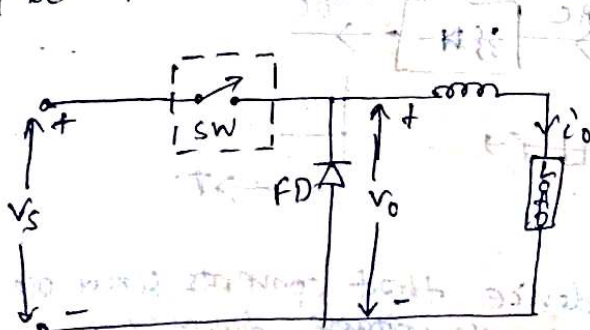


chopper can be represented by a switch  $SW$  with an arrow. when the switch is off no current can flow. when the switch is on current flows in the direction of arrow only.

- chopper is dc equivalent of an ac transformer having continuously variable turns ratio. Like a transformer chopper can be used to step down or step up the fixed dc input voltage.

### Principle of chopper operation: →

A chopper is a high speed on/off semiconductor switch. It connects source to load and disconnects the load from the source at a fast speed. In this manner a chopped load voltage is obtained from a constant dc supply of magnitude  $V_s$ . Chopper is represented by a switch  $SW$  inside a dotted rectangle, which may be turned on or turned off as desired.



During the period  $T_{on}$ , chopper is on and load voltage is equal to source voltage  $V_s$ . During the interval  $T_{off}$ , chopper is off, load current flows through the FD, so that load terminals are short circuited by FD and load voltage is zero during  $T_{off}$ . In this manner, chopped dc voltage is produced at the load terminals. The load current is continuous.

$$\text{Average load voltage, } V_0 = \frac{T_{on}}{T_{on} + T_{off}} V_s$$

$$V_0 = \frac{T_{on}}{T} V_s$$

$$V_0 = \alpha \cdot V_s$$

$T_{on}$  = on time

$T_{off}$  = off time

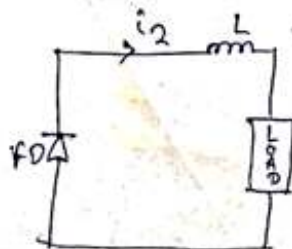
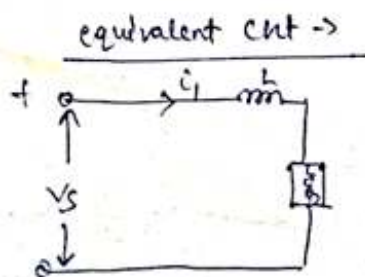
$T = T_{on} + T_{off}$  = Chopping period

$\alpha = \frac{T_{on}}{T}$  = duty cycle

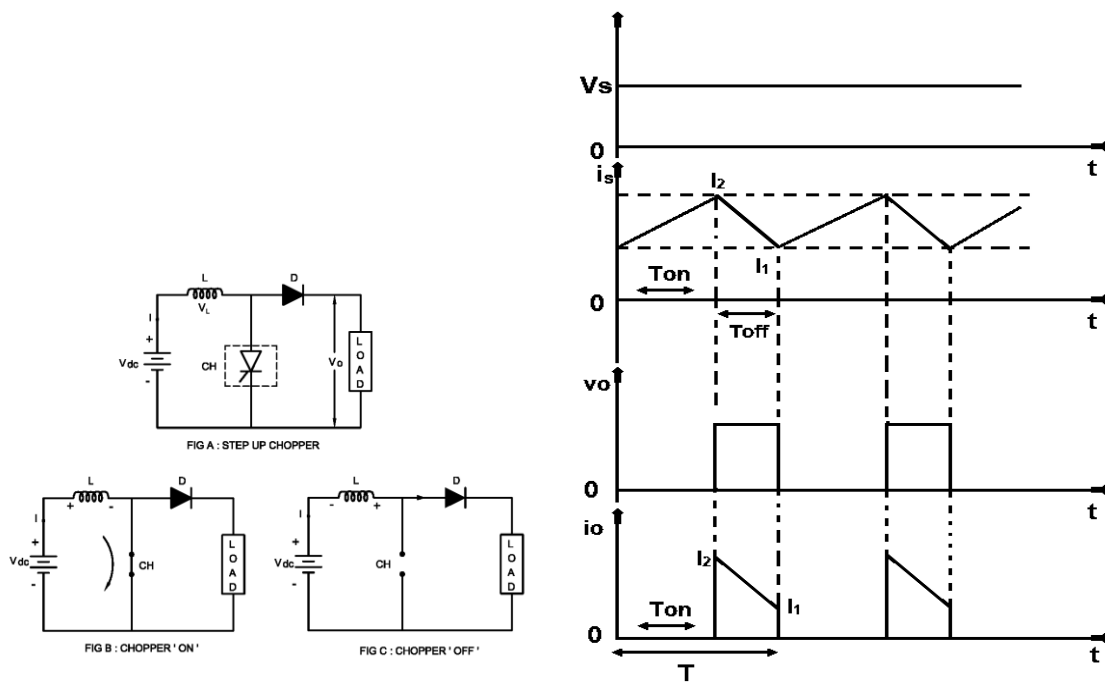
- Hence the load voltage can be controlled by varying duty cycle  $\alpha$ .
- load voltage is independent of load current.

$$V_0 = f \cdot T_{on} \cdot V_s$$

$f = \frac{1}{T}$  = chopping frequency.



## 2.8.2 STEP UP CHOPPER



### Working of Step up Chopper

#### Step up Chopper

The step up chopper is one in which output DC voltage is greater than the input DC voltage.

The basic diagram for the step up chopper is shown in the figure A.

When the chopper is switched ON during  $T_{ON}$  time, the energy stored in the inductor via path  $V_{dc} - L - CH - V_{dc}$ .

The direction of current passing through inductor is shown in the figure B when the chopper CH is switched on.

When chopper is switched OFF during  $T_{OFF}$  time, the current passing through inductor is zero and voltage across inductor is  $L (di/dt)$ .

The stored energy of inductor is transferred to the load.

The circuit diagram of step up chopper during chopper OFF time is shown in the figure C.

The load / output voltage is equal to

$$V_o = V_{dc} + V_L \\ = V_{dc} + L (di/dt)$$

When chopper is switch ON, the energy stored in the inductor is

$$W_i = V_{dc} I T_{ON} \dots \dots \dots (1)$$



When chopper is switched OFF, the energy stored in the inductor is transferred to the load.

$$W_o = (V_o - V_{dc}) I T_{OFF} \dots \dots (2)$$

If there are no losses in the system, the input energy is equal to output energy

$$V_{dc} I T_{ON} = (V_o - V_{dc}) I T_{OFF}$$

$$V_{dc} T_{ON} = V_o T_{OFF} - V_{dc} T_{OFF}$$

$$V_{dc} (T_{ON} + T_{OFF}) = V_o T_{OFF}$$

$$V_o = [(T_{ON} + T_{OFF}) / T_{OFF}] V_{dc}$$

$$V_o = [T / T_{OFF}] V_{dc}$$

**OR**

$$V_o = [T / (T - T_{ON})] V_{dc}$$

$$V_o = [1 / (1 - T_{ON} / T)] V_{dc}$$

$$V_o = [1 / (1 - K)] V_{dc}$$

When  $K = 0$  (chopper is in OFF condition)  $V_o = V_{dc}$

When  $K = 1$  (chopper is in OFF condition)  $V_o = \infty$

When the duty cycle lies in the range of  $0 < K < 1$ , the output voltage lies in the range of  $V_{dc} < V_o < \infty$ .

### **Application of DC Step up Chopper**

The application of step up chopper is in the regenerative braking of DC Motor.

The output voltage is greater than the input voltage therefore the DC Motor works as DC generator and load current flows from load to supply side.

## **2.9 CONTROL MODES OF CHOPPER**

### **Constant frequency operation:**

1) The chopping period  $T$  is kept constant and on time is varied.

The pulse width modulation, the width of the pulse is varied.

2) Variable frequency operation, the chopping frequency  $f$  is varied.

Frequency modulation, either on time or off time is kept constant.

This type of control generates harmonics at unpredictable frequency and filter design is often difficult.

Control strategies →

$$\boxed{\text{avg } V_o = \alpha \cdot V_s}$$

$$V_o = \frac{T_{on}}{T} \cdot V_s$$

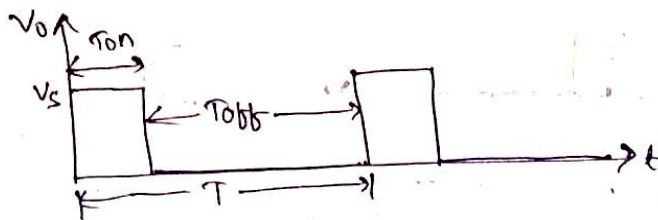
$$V_o = f \cdot T_{on} \cdot V_s$$

The average o/p voltage  $V_o$  can be controlled through  $\alpha$  by opening and closing the semiconductor switch periodically.

various control strategies of varying duty cycle  $\alpha$  :->

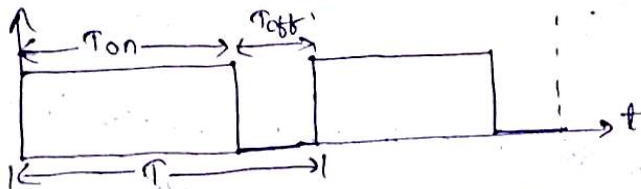
① constant frequency system / PWM / TRC system

- ontime  $T_{on}$  is varied
- chopping frequency  $f$  or chopping period  $T$  is constant.
- variation of  $T_{on}$  means adjustment of pulsewidth.
- Also known as pulse width modulation or time ratio control system.



$$T_{on} = \frac{1}{4} T$$

$$\alpha = 0.25 \text{ or } 25\%$$



$$T_{on} = \frac{3}{4} T$$

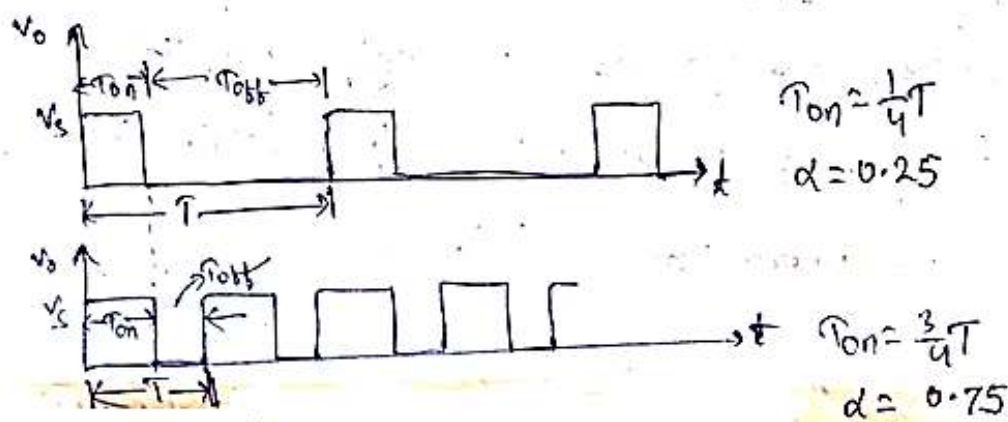
$$\alpha = 0.75 \text{ or } 75\%$$

Limitation → In PWM techniques,  $T_{on}$  cannot be reduced to near zero for most of the commutation circuits used in choppers, so that low range of  $\alpha$  control is not possible in PWM. This can be achieved by increasing the chopping period or decreasing the chopping frequency.

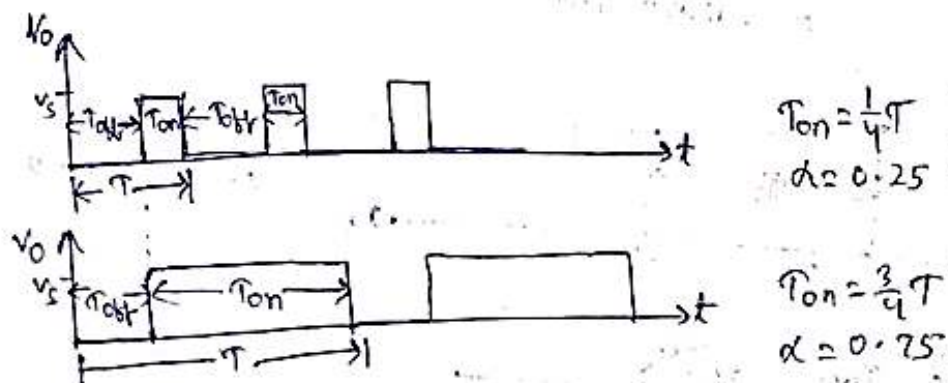
## ② variable frequency system / frequency modulation

- chopping frequency  $\neq$  one chopping period  $T$  is varied and either  $T_{on}$  is constant or  $T_{off}$  is constant.
- Also called as frequency modulation scheme.

(a)  $T_{on}$  kept constant,  $T$  varied



(b)  $T_{off}$  is kept constant and  $T$  varied

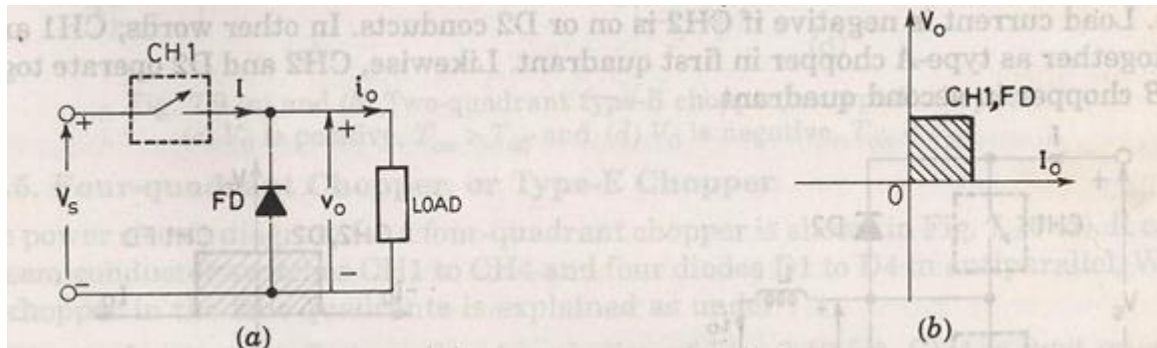


disadvantages →

- filter design for wide frequency variation is difficult.
- possibility of interference with signalling and telephone lines.
- longer off time may make the load current discontinuous.

## TYPES OF CHOPPER:

### FIRST QUADRANT OR TYPE A CHOPPER:



When switch ON

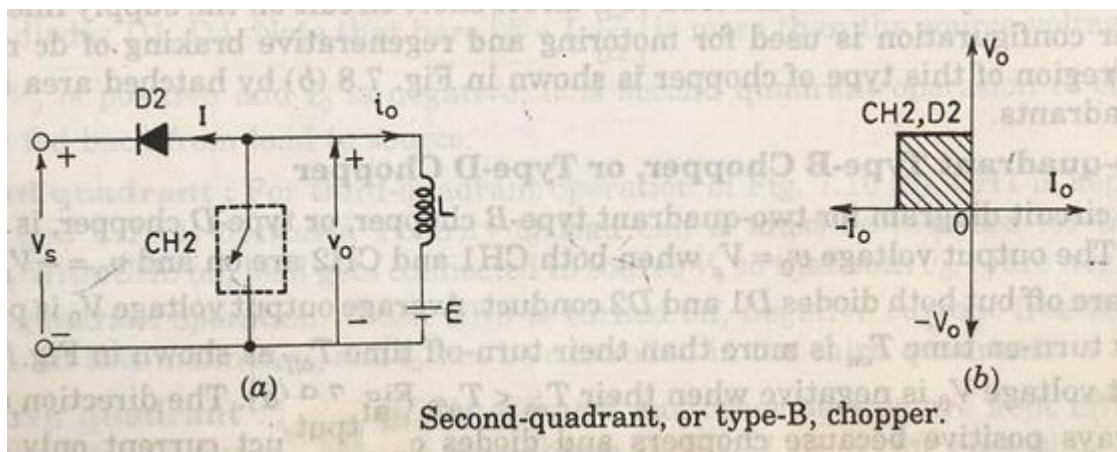
$$V_o = V_s$$

Current  $i_o$  flows in the same direction when switch off.

$$V_o = 0, i_o = 0$$

So, average value of both the load and the current are positive.

### SECOND QUADRANT OR TYPE B CHOPPER:



When switch is closed the load voltage  $E$  drives current through  $L$  and switch.

During  $T_{on}$ ,  $L$  stores energy.

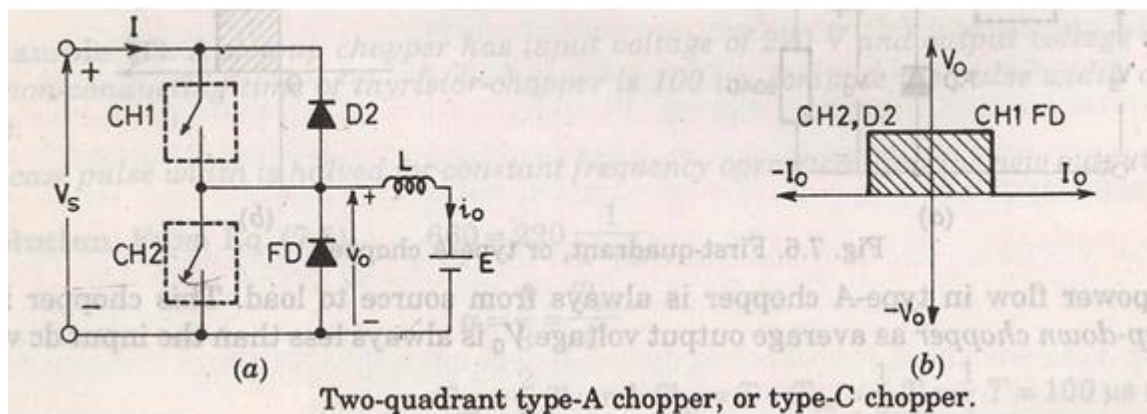
When switch off  $V_o$  exceeds source voltage  $V_s$ .

$$V_o = E + L \frac{di}{dt}$$

Diode  $D_2$  is forward biased. power is fed back to supply. As  $V_o$  is more than source voltage. So such chopper is called step up chopper.

So current is always negative and  $V_o$  is always positive.

## TWO QUADRANT TYPE A CHOPPER OR, TYPE C CHOPPER:



Both the switches never switch ON simultaneously as it lead direct short circuit of the supply.

Now when sw2 is closed or FD is on the output voltage  $V_o$  is zero.

When sw1 is ON or diode D conducts output voltage is  $V_o$  is  $+V_s'$

### CURRENT ANALYSIS:

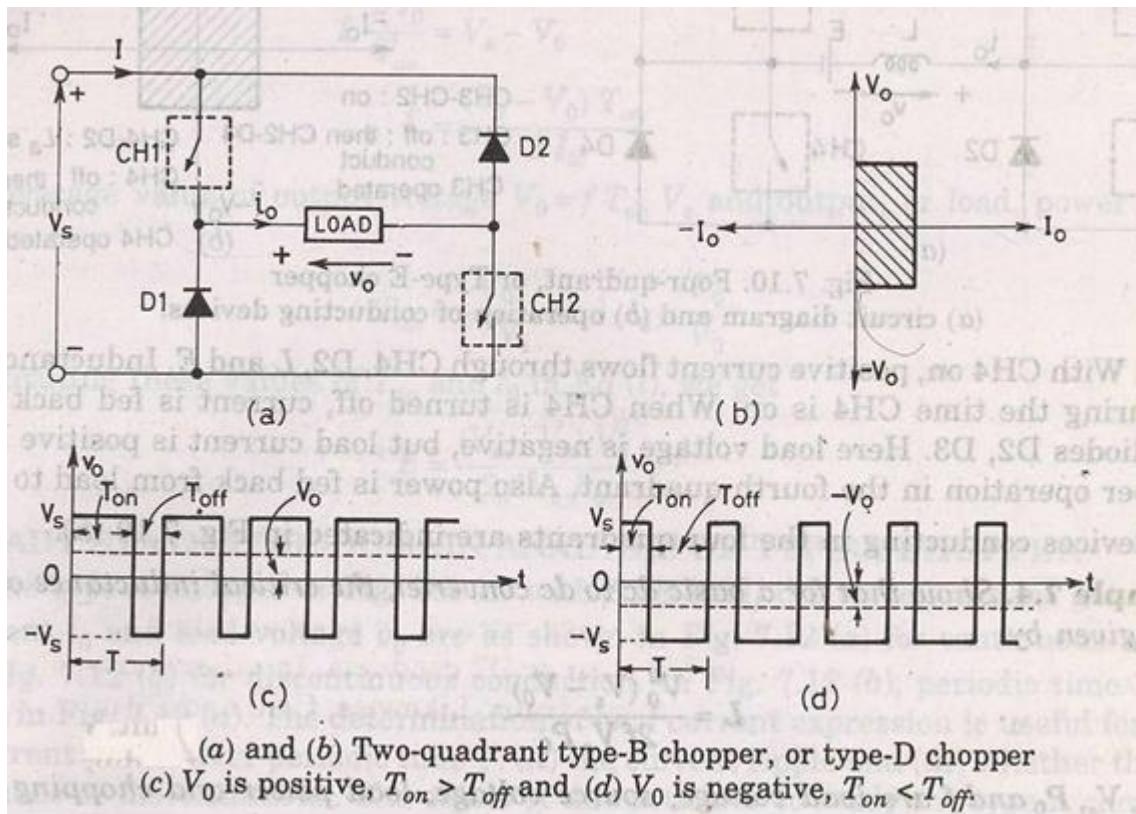
When  $CH1$  is ON current flows along  $i_o$ . When  $CH1$  is off current continues to flow along  $i_o$  as  $FD$  is forward biased. So  $i_o$  is positive.

Now when  $CH2$  is ON current direction will be opposite to  $i_o$ . When sw2 is off  $D2$  turns ON. Load current is  $-i_o$ . So average load voltage is always positive.

Average load current may be positive or negative.



## TWO QUADRANT TYPE B CHOPPER, OR TYPE D CHOPPER:

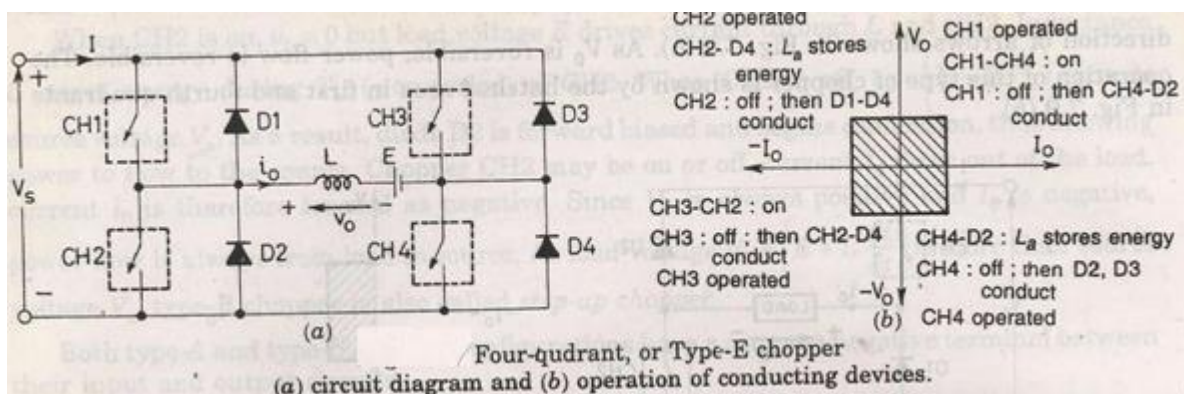


When CH1 and CH2 both are on then  $V_o = V_s$ .

When CH1 and CH2 are off and D1 and D2 are on  $V_o = -V_s$ .

The direction of current is always positive because chopper and diode can only conduct in the direction of arrow shown in fig. Average voltage is positive when  $T_{on} > T_{off}$

## 2.10 FOUR QUADRANT CHOPPER, OR TYPE E CHOPPER



FIRST QUADRANT:

CH4 is kept ON

CH3 is off

CH1 is operated

$V_0 = V_s$

$i_0$  = positive

when CH1 is off positive current free wheels through CH4, D2  
so  $V_0$  and  $I_2$  is in first quadrant.

SECOND QUADRANT:

CH1, CH3, CH4 are off.

CH2 is operated.

Reverse current flows and  $I$  is negative through L CH2 D4 and E.

When CH2 off D1 and D4 is ON and current  $i_d$  fed back to source. So

$E + L \frac{di}{dt}$  is more than source voltage  $V_s$ .

As  $i_0$  is negative and  $V_0$  is positive, so second quadrant operation.

THIRD QUADRANT:

CH1 OFF, CH2 ON

CH3 operated. So, both  $V_0$  and  $i_0$  is negative.

When CH3 turned off negative current freewheels through CH2 and D4.

FOURTH QUADRANT:

CH4 is operated other are off.

Positive current flows through CH4 E L D2.

Inductance L stores energy when current fed to source through D3 and D2.  $V_0$  is negative.

## **Unit-4: AM & FM TRANSMITTER & RECEIVER**

### **4.1. CLASSIFICATION OF RADIO RECEIVERS-**

Radio receivers are classified in two ways.

- (A) Depending upon the applications, the radio receivers are classified as:
- 1) Amplitude Modulation broadcast receivers: These receivers are used to receive the broadcast of speech or music transmitted from amplitude modulation broadcast transmitters which operate on long wave, medium wave or short wave bands
  - 2) Frequency Modulation broadcast receivers: These receivers are used to receive the broadcast programs from FM broadcast transmitters which operate in VHF or UHF bands.
  - 3) Communication receivers: Communication receivers are used for reception of telegraph and short wave telephone signals. This means that communication receivers are used for various purposes other than broadcast services.
  - 4) Television receivers: Television receivers are used to receive television broadcast in VHF or in UHF bands.
  - 5) Radar receivers: Radar receivers are used to receive radar signals.
- (B) Depending upon the fundamental aspects, the radio receivers are classified as:
- 1) Tuned Radio Frequency receivers
  - 2) Super Heterodyne receiver

### **4.2 DEFINATION-**

#### **FIDELITY-**

The fidelity of a receiver is its ability to accurately reproduce in its output, the signal that appears at its input.

#### **SENSITIVITY-**

The sensitivity of a radio receiver is its ability to amplify weak signal.

#### **SELECTIVITY-**

The ability of a device to respond to a particular frequency without interference from others. The selectivity of a receiver is its ability to reject unwanted signal and accept the desired signal.

#### **NOISE FIGURE-**

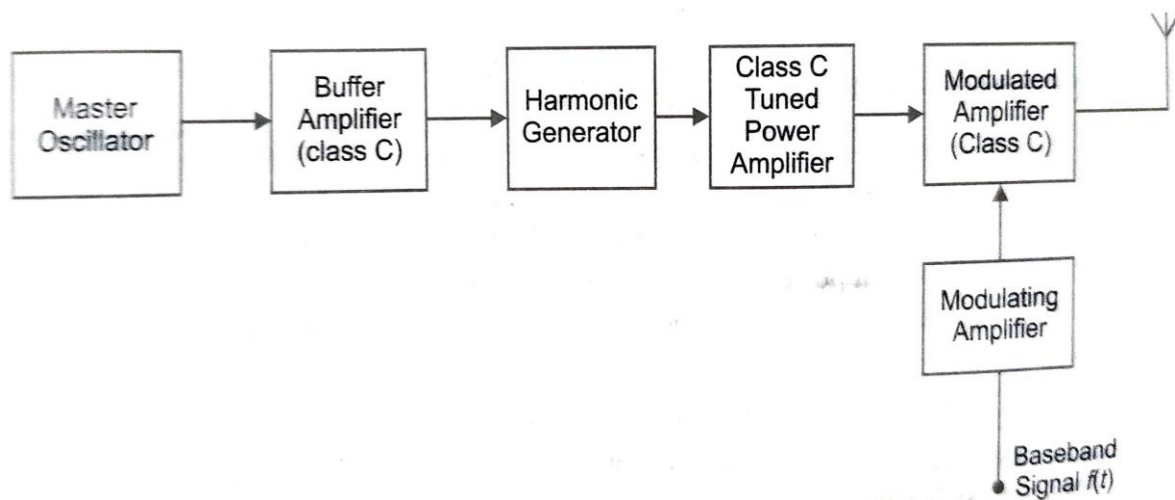
It is defined as the ratio of signal to noise ratio at the input to that at the output.

$$NF = \frac{(S/N)_i}{(S/N)_o}$$

Noise figure is the measures of degradation of the signal to noise ratio caused by components in a signal chain. It is a number by which the performance of an amplifier or a radio receiver can be specified with lower values indicating better performance.



### 4.3 AM TRANSMITTER-



#### Master Oscillator-

It generates the carrier signal, which lies in the RF range. As we know the frequency of the carrier is always very high. But it very difficult to generate high frequencies with good frequency stability. The master oscillator generates a sub multiple with the required carrier frequency.

This submultiple frequency is multiplied by the frequency multiplier stage to get the required carrier frequency. A crystal oscillator can be used in this stage to generate a low frequency carrier with the best frequency stability. The frequency multiplier stage then increase the frequency of the carrier to its required value.

#### Buffer Amplifier-

A buffer amplifier is one that provides electrical impedance transformation from one circuit to another and helps to prevent the signal source from being affected by whatever currents that the load may be produced with. The signal is buffered from load currents.

It first matches the output impedance of the carrier oscillator with the input impedance of the frequency multiplier. It then isolates the carrier oscillator and frequency multiplier. This is required so that the multiplier does not draw a large current from the carrier oscillator. If this occurs the frequency of the carrier oscillator will not remain stable.

#### Frequency Multiplier-

Frequency multiplier is an electronic circuit that generates an output signal whose output frequency is a multiple of its input frequency. The submultiple frequency of the carrier signal generated by the carrier oscillator is applied to the frequency multiplier through the buffer amplifier. This stage is also called harmonic generator.

The frequency multiplier generates high carrier frequency. The frequency multiplier is a tuned circuit that can be tuned to the required carrier frequency that is to be transmitted.

#### Class-C tuned power amplifier-

A class-C power amplifier gives high power current pulses of the carrier signal at its output.

#### Modulated Amplifier (Class-C)-

The modulating audio signal and the carrier signal after power amplification are applied to this modulating stage. The modulation takes place at this stage. This signal finally passed to the antenna.

#### Antenna-

The output of the modulated class-C power amplifier feeds the signal to the transmitting antenna. To transfer maximum power from the output stage to the antenna it is necessary that the impedance of the two sections match. For this a matching network is required. The matching network consists of L & C components.

### **4.4 CONCEPT OF FREQUENCY CONVERSION, RF AMPLIFIER & IF AMPLIFIER, TUNING, S/N RATIO-**

#### **CONCEPT OF FREQUENCY CONVERSION-**

It is the process of converting the carrier frequency of a received signal from its original value to the intermediate frequency value in a super heterodyne receiver.

In radio reception using the super heterodyne principle the incoming signal is changed in frequency by converter stage of the receiver to a new and lower frequency known as the intermediate frequency.

#### **RF AMPLIFIER-**

The antenna not only provides very low amplitude input signals but it picks up all available transmissions at the same time.

The receiver circuits generate noise signals, which are added to the wanted signals. We hear this as a 'background hiss' and are particularly noticeable if the receiver is tuned between stations or if a weak station is being received. The RF amplifier is the first stage of amplification. It has to amplify the incoming signal above the level of the internally generated noise and also to start the process of selecting the wanted station and rejecting the unwanted ones.

#### **IF AMPLIFIER-**

The IF Amplifier consists of two stages of amplification and provides the main signal amplification and selectivity. Operating at a fixed IF frequency means that the design of the amplifiers can be simplified. If it were not for the fixed frequency, all the amplifiers may need

to be tunable across the whole range of incoming RF frequencies and it would be difficult to arrange for all the amplifiers to keep in step as they are re-tuned.

The radio must select the wanted transmission and reject all the others. To do this the band pass of all the stages must be carefully controlled. Each IF stage does not necessarily have the same band pass characteristics. The overall response is important. Again, this is something which is much more easily achieved without the added complication of making them tunable. At the final output from the IF amplifiers, we have a 455 KHz wave which is amplitude modulated by the wanted audio information. The selectivity of the IF amplifiers has removed the unwanted components generated by the mixing process.

#### TUNING-

In super heterodyne receiver the front end RF tuning circuit is required to remove the image signal. LC tuned circuit is used. The tuning of this tracks that of the local oscillator, so that frequency of both sections change simultaneously.

Nowadays the tuning is normally carried out using varactor diodes that are driven by a voltage that is programmed from the microprocessor that controls the operation of the radio. This controls the frequency synthesizer used as the local oscillator.

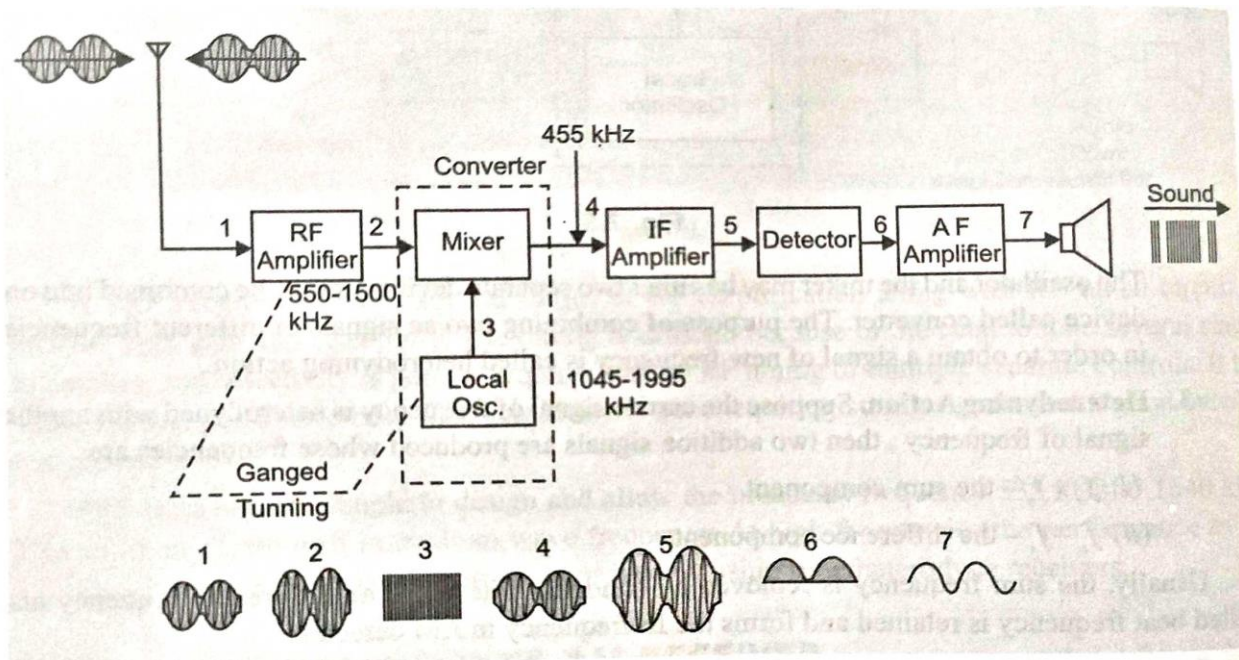
#### S/N RATIO-

### **4.5 SUPER HETERODYNE RECEIVER-**

It is difficult to design amplifiers which give uniform high gain over a wide range of radio frequencies. However it is possible to design amplifiers which can provide high gain and uniform amplification over a narrow band of lower frequencies called intermediate frequencies.

Hence it is necessary to convert the modulated RF signal into modulated IF signal by using a frequency converter. For this we use super heterodyne receiver.

The word heterodyne stands for mixing. Here we have mixed the incoming signal frequency with the local oscillator frequency. Therefore this receiver is called super heterodyne receiver.



#### RF Amplifier-

RF low noise amplifiers are designed to increase the desired RF signal amplitude without adding distortion or noise.

#### Mixer-

Mixer circuit is designed to combine two radio frequencies. It has two input one from RF amplifier and other from local oscillator.

When mixer combined the two signal we get,  $f_o + f_s$  (Sum) and  $f_o - f_s$  (Difference). The sum frequency is removed by band pass filtering. The difference frequency given to the input of IF amplifier.

The difference frequency is always maintained at 455KHz.

#### Local Oscillator-

The local oscillator is an RF oscillator whose frequency of oscillation can be controlled by varying the capacitance of its capacitor. The frequency of local oscillator always maintained higher than incoming signal.

#### IF Amplifier-

The 455 KHz output of the mixer is then passed on to IF amplifier. The IF amplifier amplify the signal and the output of IF is demodulated by a detector which provides the audio signal.

#### A.F Amplifier-

The audio signal is amplified by the audio frequency amplifier whose output is fed to a loud speaker which reproduces the original signal.

#### Ganged Tuning-

If the incoming signal changes then the local oscillator frequency also changes to maintain the difference frequency. For this purpose the tuning capacitor of the oscillator is ganged with the capacitor of the input circuit i.e, RF amplifier. So that the difference in the frequency of the incoming signal and oscillator frequency is always constant i.e, 455 KHz.

Example- if the  $f_s = 1500\text{KHz}$

$$f_o = 1955 \text{ KHz}$$

$$\text{Then } f_o - f_s = 455 \text{ KHz}$$

Or if the  $f_s = 1345 \text{ KHz}$

$$f_o = 1800 \text{ KHz}$$

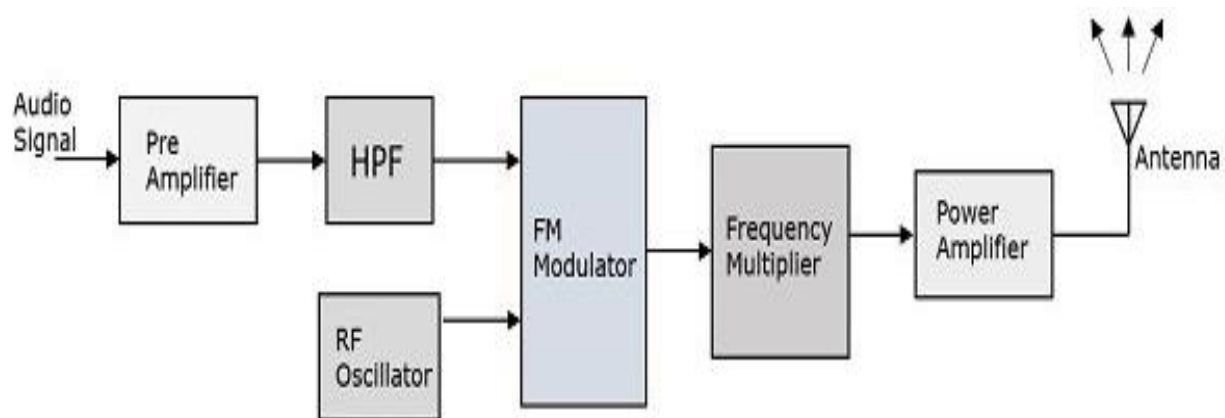
$$\text{Then } f_o - f_s = 455 \text{ KHz}$$

## **4.6 FM TRANSMITTER & RECEIVER**

### **FM TRANSMITTER-**

The FM transmitter is a low power transmitter and it uses FM waves for transmitting the sound.

FM transmitter circuit can produce the radio frequency waves which are transmitted through the antenna.



#### Audio Signal-

Here a microphone is used as a source of an audio signal. The microphone is a transducer which can convert the sound energy into an electrical energy.

#### Pre Amplifier-

The audio pre amplifier is used to amplify the audio signal coming from the microphone.

HFA-

The output of Pre Amplifier is then applied to HPF which acts as a pre emphasis network. Pre emphasis increases the magnitude of the higher signal frequency, thereby improving the signal to noise ratio.

FM Modulator-

The modulator circuit is the main part of an FM transmitter circuit. It converts the audio signal which is to be transmitted. The modulator circuit takes two signal as input, one is the signal coming from the high pass filter and another is carrier signal from RF oscillator.

The modulator circuit modulates the RF signal according to the audio signal and produces the modulated RF signal as the output.

RF Oscillator-

An RF oscillator produces signals in the radio frequency range of about 100kHz to 100Ghz.

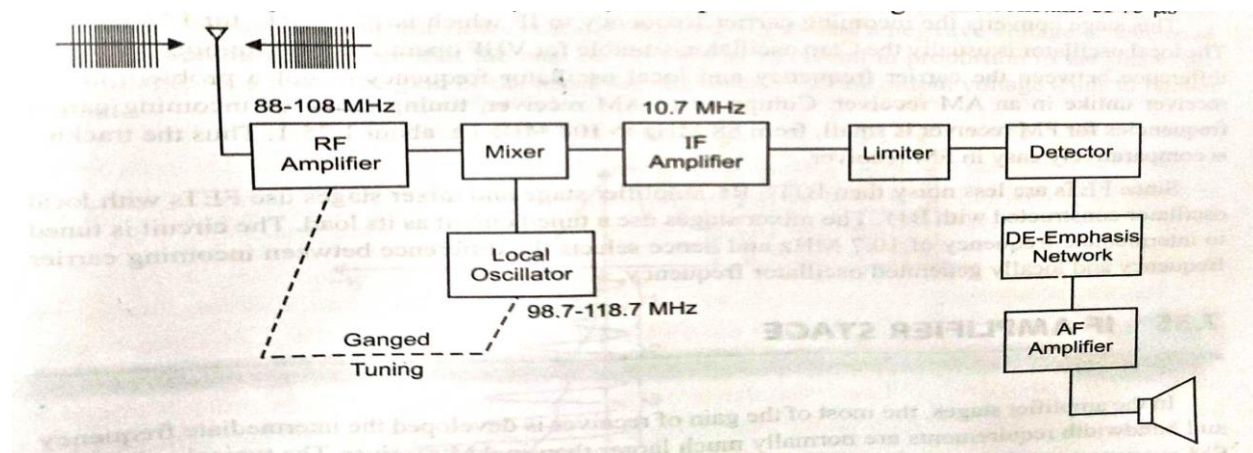
Frequency Multiplier-

Several stages of frequency multiplier are used to increase the operating frequency. Even then, the power of the signal is not enough to transmit. The RF amplifier circuit amplifies the signal coming from frequency multiplier.

RF amplifier-

RF amplifier is used to amplify the signal which can be easily transmitted for a long distance. Then the amplified radio signal is fed to the antenna for the transmission.

#### 4.6.2 FM RECEIVER-



RF amplifier-

The RF amplifier amplifies the received signal intercepted by the antenna. The amplifier is a low noise amplifier.

#### Mixer-

The amplified signal is then applied to the mixer stage. The second input of the mixer comes from the local oscillator.

#### IF Amplifier-

The output of the mixer is a difference signal of incoming signal and carrier signal i.e, known as intermediate frequency of 10.7MHz. This signal is then amplified by IF amplifier.

#### Limiter-

The output of the IF amplifier is applied to the limiter circuit. The limiter removes the noise in the received signal and gives a constant amplitude signal.

This is very important in FM receivers because at amplitude variation in the received signal will result in unfaithful reproduction of the audio signals. Limiter is a sort of clipping circuit.

#### Detector-

The output of the limiter is now applied to the detector, which recovers the modulating signal. However, this signal is still not the original modulating signal. Before applying it to the audio amplifier stage, it is applied to de-emphasized network.

The de-emphasis network reduces the amplitude of high frequencies in the audio signal to bring them back to their original amplitude as these are increased by the pre-emphasis network at the transmitting station.

#### AF Amplifier-

The output of the de-emphasized stage is the audio signal, which is then applied to the audio amplifier stages and finally to the speaker.

## **UNIT-5: ANALOG TO DIGITAL CONVERSION & PULSE MODULATION SYSTEM**

### **5.1 CONCEPT OF SAMPLING THEOREM, NYQUIST RATE & ALISING**

#### **SAMPLING THEOREM**

A continuous time signal is first converted to discrete-time signal by sampling process. The sufficient number of samples of the signal must be taken so that the original signal represented in its samples completely. Also, it should be possible to recover or reconstruct the original signal completely from its samples. The number of samples to be taken depends on maximum signal frequency present in the signal.

The statement of sampling theorem can be given in two parts as:

- (i) A band-limited signal of finite energy, which has no frequency component higher than  $f_m$  Hz, is completely described by its sample values at uniform intervals less than or equal to  $1/2f_m$  second apart.
- (ii) A band-limited signal of finite energy, which has no frequency components higher than  $f_m$  Hz, may be completely recovered from the knowledge of its samples taken at the rate of  $2f_m$  samples per second.

Combining the two parts, the sampling theorem may be stated as under:

“A continuous time signal may be completely represented in its samples and recovered back if the sampling frequency is  $f_s \geq 2f_m$ . Here  $f_s$  is the sampling frequency and  $f_m$  is the maximum frequency present in the signal”.

#### **NYQUIST RATE**

When the sampling rate becomes exactly equal to  $2f_m$  samples per sec, then it is called Nyquist rate. Nyquist rate is also called the minimum sampling rate.

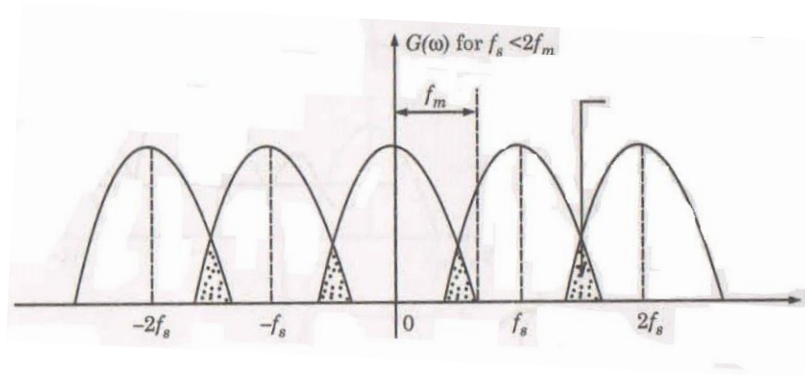
It is given by  $f_s = 2f_m$

Nyquist Interval  $T_s = 1/2 f_m \text{ sec}$

#### **ALIASING:**

When a continuous time band limited signal is sampled at a rate lower than Nyquist rate  $f_s < 2f_m$ , then the cycles of the spectrum  $G(w)$  of the sampled signal  $g(t)$  overlap with each other.





**Spectrum of the sampled signal for the case  $f_s < 2f_m$**

## **5.2 SAMPLING TECHNIQUES**

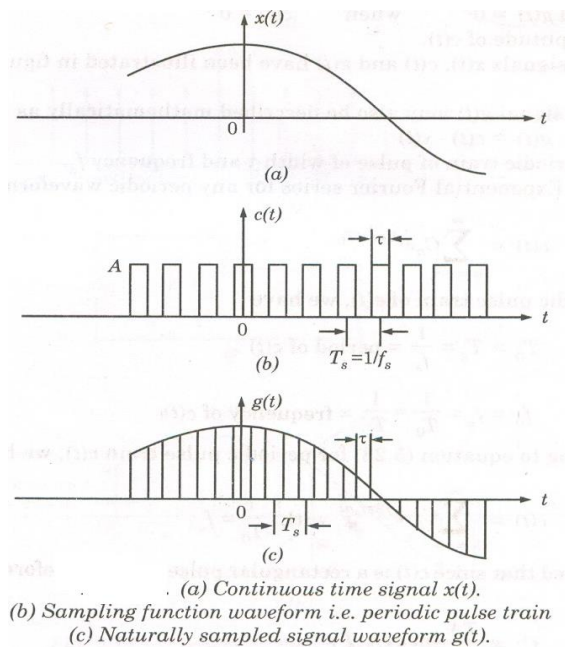
### **CLASSIFY SAMPLING**

There are 3 types of sampling techniques.

- (i) Instantaneous sampling
- (ii) Natural sampling
  - (iii) Flat top sampling

- **Natural sampling:**

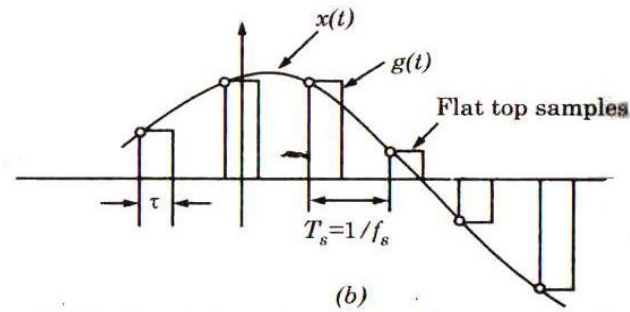
In this sampling the top of the pulses are curved according to the modulating signal.



### **Natural Sampling**

- **Flat- top Sampling:**

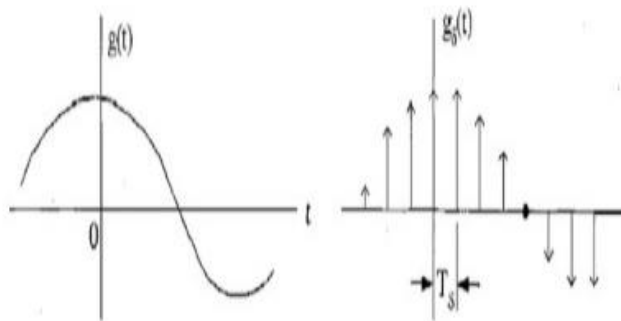
In this sampling the top of the pulses are flat.



**Flat-top sampling**

- **instantaneous sampling:**

In this sampling the modulating signal is multiplied with samples of unit strength. This form of modulation is known as impulse modulation. The main disadvantage of this modulation is very difficult to generate.



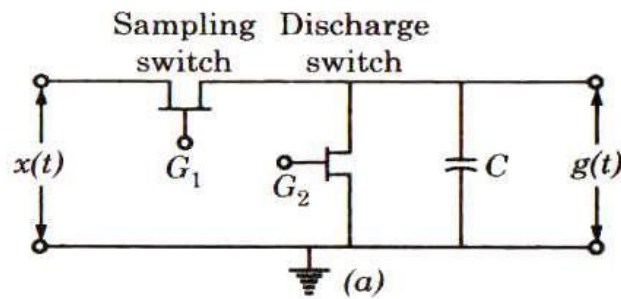
**Instantaneous sampling**

### **5.3 ANALOG PULSE MODULATION**

#### **GENERATION OF PAM-**

Pulse amplitude modulation may be defined as that type of modulation in which the amplitudes of regularly spaced rectangular pulses vary according to instantaneous value of the modulating signal. The pulses in a PAM signal may be of flat top type or natural type or ideal type. Out of these three pulse amplitude modulation methods, the flat top PAM is

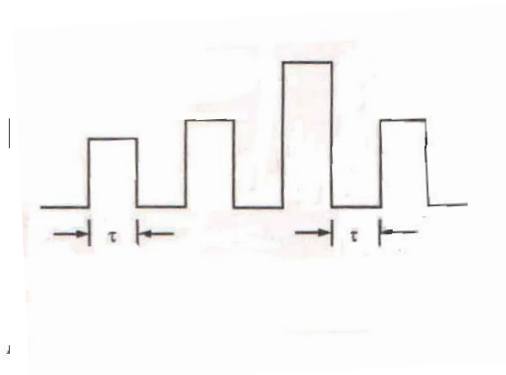
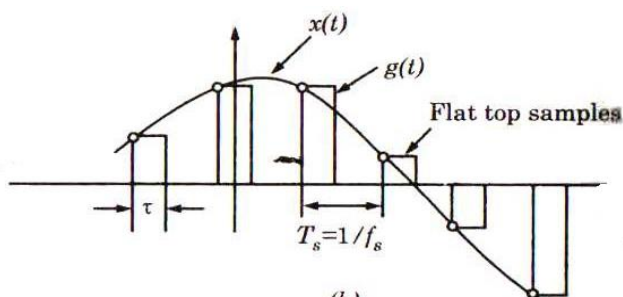
most popular and is widely used. The reason for using flat top PAM is that during the transmission, the noise interferes with the top of the transmitted pulses and this noise can be easily removed if the PAM pulses has flat top.



### Sample and hold circuit generation Flat top sampled PAM

A sample and hold circuit is used to produce flat top sampled PAM. The working principle of this circuit is quite easy. The sample and hold circuit consists of two field effect transistor switches and a capacitor. The sampling switch is closed for a short duration by a short pulse applied to the gate  $G_1$  of the transistor. During this period, the capacitor  $C$  is quickly charge up to a voltage equal to the instantaneous sample value of the incoming signal  $x(t)$ . Now the sampling switch is opened and the capacitor  $C$  holds the charge. The discharge switch is then closed by a pulse applied to gate  $G_2$  of the other transistor. Due to this, the capacitor ' $C$ ' is discharged to zero volts. The discharge switch is then opened and thus capacitor has no voltage.

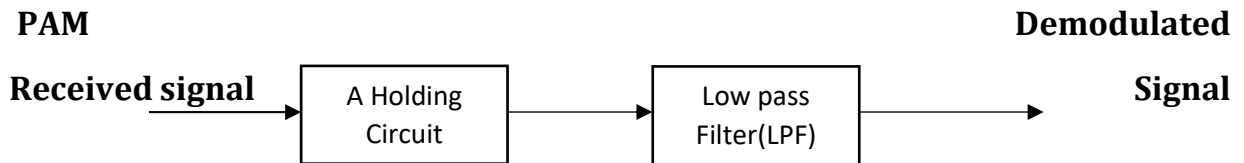
Hence, the output of the sample and hold circuit consists of a sequence of flat top samples.



(a) & (b) Illustration of maximum frequency PAM Signal

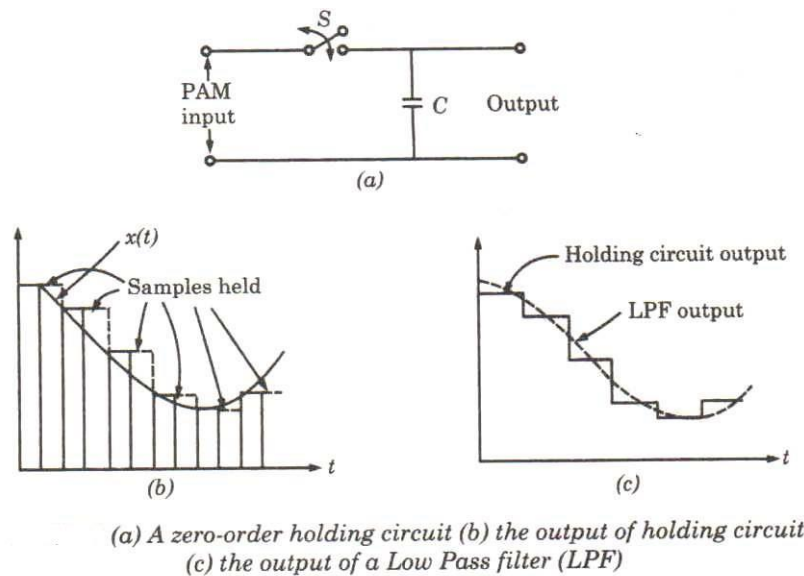
## DETECTION OF PAM-

Demodulation is the reverse process of modulation in which the modulating signal is recovered back from a modulated signal. For pulse amplitude modulated signals, the demodulation is done using a holding circuit.



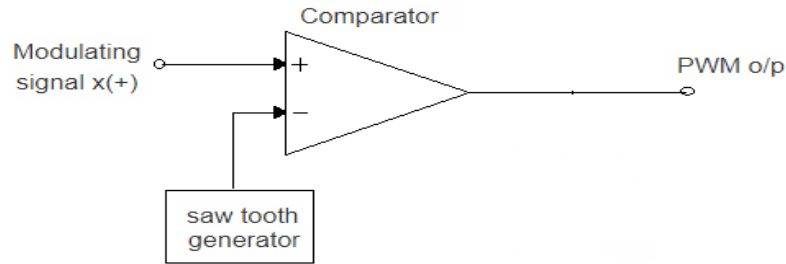
**A Block diagram of PAM Demodulator**

In this method, the received PAM signal is allowed to pass through a holding circuit and a low pass filter. In the holding circuit the switch  $s$  is closed after the arrival of the pulse and it is opened at the end of the pulses. In this way, the capacitor  $C$  is charged to the pulse amplitude value and it holds this value during the interval between the two pulses. After this the holding circuit output is smoothened in low pass filter. It may be observed that some kind of distortion is introduced due to the holding circuit. Here we use a zero order holding circuit. This zero order holding circuit considers only the previous sample to decide the value between the two pulses.



## **PAM signal generator generating modulating Signal**

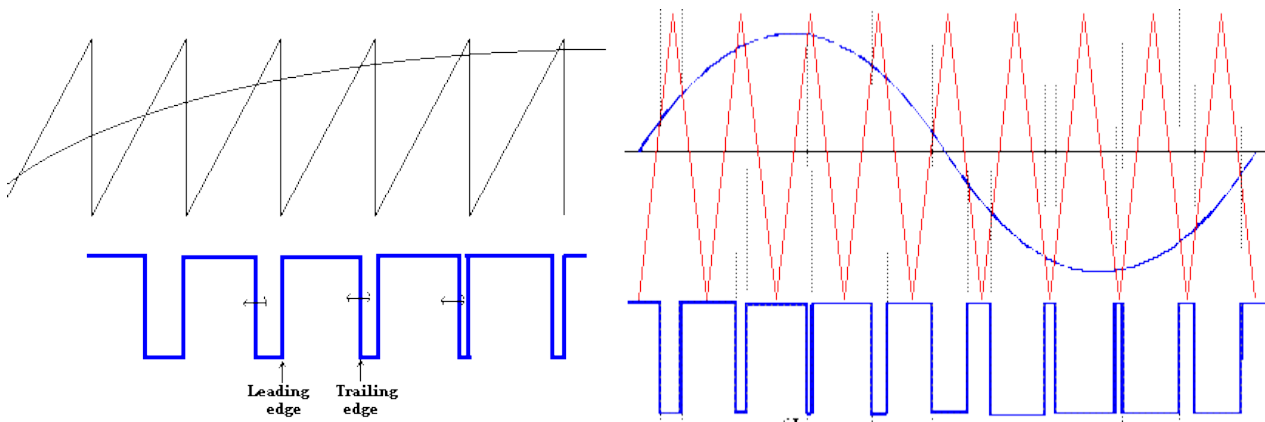
## GENERATION OF PWM-



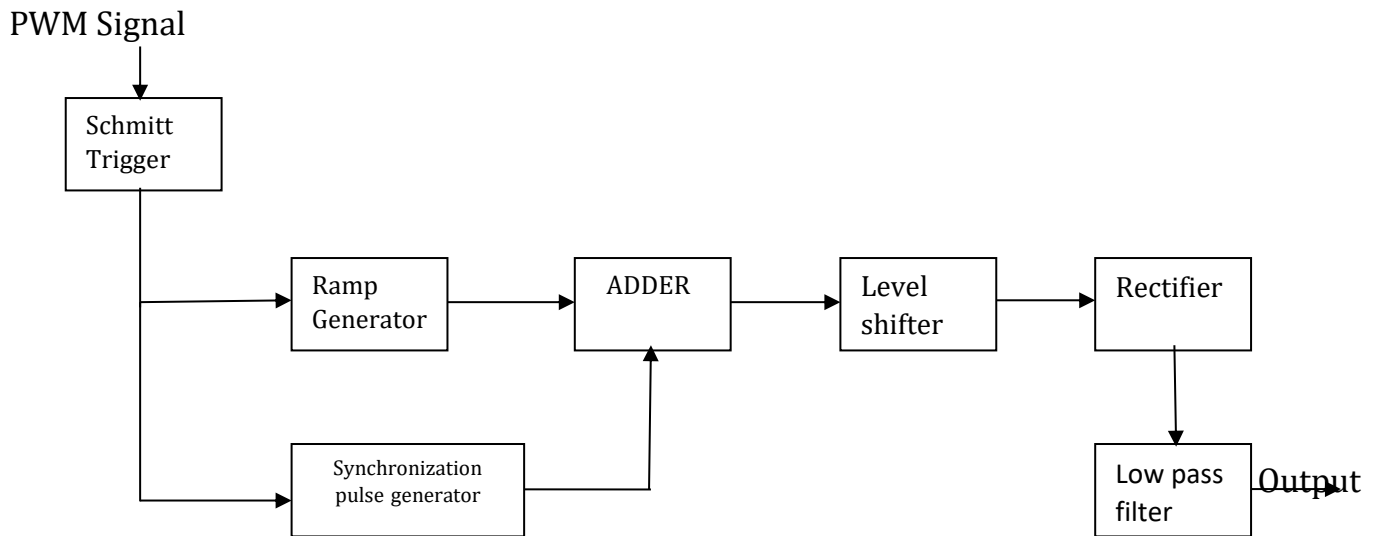
The modulating signal  $x(t)$  is applied to the non-inverting input of the comparator. The saw tooth generator generates the saw tooth signal. The saw tooth signal also known as sampling signal applied to the inverting input of comparator.

The output of the comparator is high only when instantaneous value of  $x(t)$  is higher than that of saw tooth waveform. Hence, the leading edge of PDM signal will be fixed and trailing edge will be modulated. When saw tooth waveform voltage is greater than voltage of  $x(t)$  at that instant, the output of comparator remains zero.

If the saw tooth waveform is reversed, then trailing edge will be fixed and leading edge will be modulated. If saw tooth waveform is replaced by a triangular waveform then both leading and trailing edges will be modulated. The pulse duration modulation or pulse width modulation signal is nothing but output of the comparator.



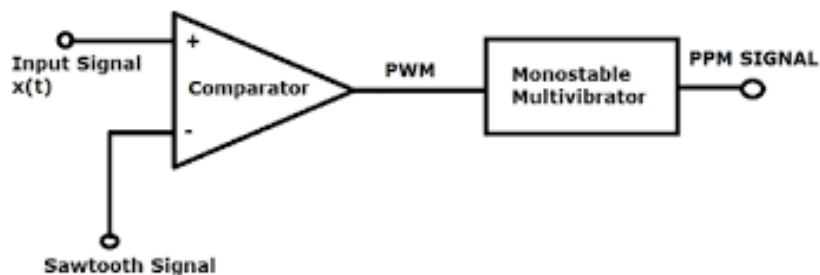
## DEMODULATION OF PWM-



### **PWM Detector**

The received PWM signal is applied to the Schmitt trigger circuit. This Schmitt trigger circuit removes the noise in the PWM waveform. The regenerated PWM is then applied to the ramp generator and the synchronization pulse detector. The ramp generator produces ramps for the duration of pulses such that height of ramps are proportional to the widths of PWM pulses. The maximum ramp voltage is retained till the next pulse. On the other hand, synchronous pulse detector produces reference pulses with constant amplitude and pulse width. These pulses are delayed by specific amount of delay. The delayed reference pulses and the output of ramp generator is added with the help of adder. The output of adder is given to the level shifter. Here negative offset shifts the waveform. Then the negative part of the waveform is clipped by rectifier. Finally, the output of rectifier is passed through low pass filter to recover the modulating signal.

## GENERATION OF PPM:-



### Generation of PPM Signal

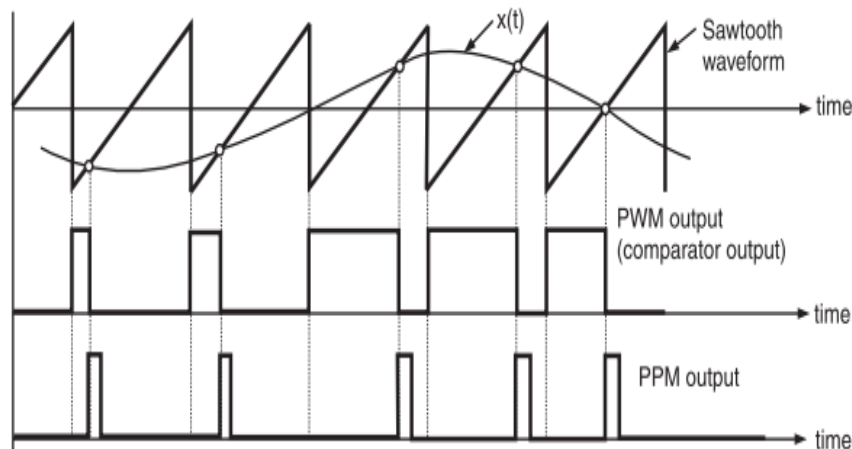
The modulating signal  $x(t)$  is applied to the non-inverting input of the comparator. The saw tooth generator generates the saw tooth signal of frequency  $f_s$ . The saw tooth signal is also known as sampling signal is applied to the inverting input of the comparator.

The output of the comparator is high only when instantaneous value of  $x(t)$  is higher than that of saw tooth waveform.

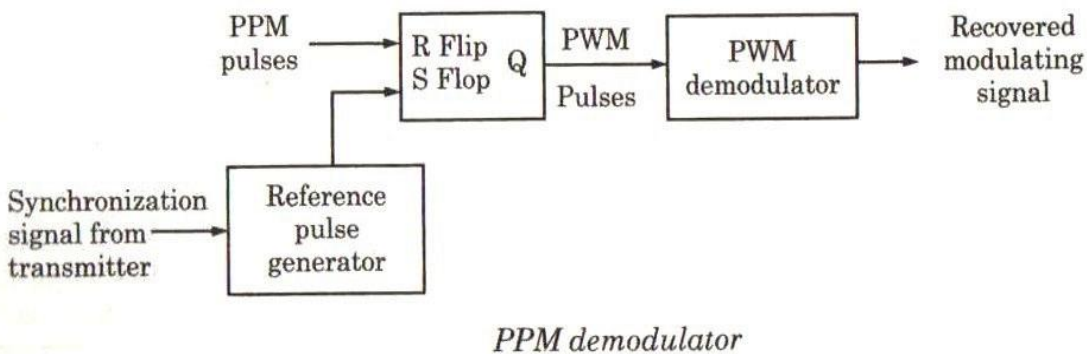
When saw tooth waveform voltage is greater than voltage of  $x(t)$  at that instant, the output of comparator remains zero. The pulse duration modulation signal is nothing but output of the comparator. To generate pulse position modulation, PDM signal is used as the trigger input to one monostable multivibrator.

The monostable output remains zero until it is triggered. The monostable is triggered on the falling edge of PDM. The output of monostable then switches to +ve saturation level 'A'. This voltage remains high for the fixed period then goes low.

The amplitude of all PPM and PDM pulses is same. Therefore nonlinear amplitude distortion as well as noise interference does not affect the detection at the receivers.



### DETECTION OF PPM:-



Flip flop is set or turned ON when the reference pulse arrives. This reference pulse is generated by reference pulse generator of the receiver with the synchronization signal from the transmitter. The flip flop circuit is reset or turned

OFF at the leading edge of position modulated pulse. This repeats and we get PWM pulses at the output of the flip flop.

#### **COMPARISON OF PAM, PWM AND PPM-**

<b>Sl. No.</b>	<b>Basis for Comparison</b>	<b>PAM</b>	<b>PWM</b>	<b>PPM</b>
1	Varying parameter	Amplitude	Width	Position
2	Immunity towards noise	Low	High	High
3	Need of synchronization pulse	Not exist	Not exist	Exist
4	Signal to noise ratio	Low	Moderate	Comparatively high
5	Transmission power	Variable	Variable	Constant
6	Bandwidth dependency	On pulse width	On rise time of pulse	On rise time of pulse
7	Synchronization between Transmitter and Receiver	Not needed	Not needed	Needed
8	Similarity of implementation	Similar to AM	Similar to FM	Similar to PM
9	Bandwidth requirement	Low	High	High

#### **5.4 QUANTIZATION OF SIGNAL & QUANTIZATION ERROR-**

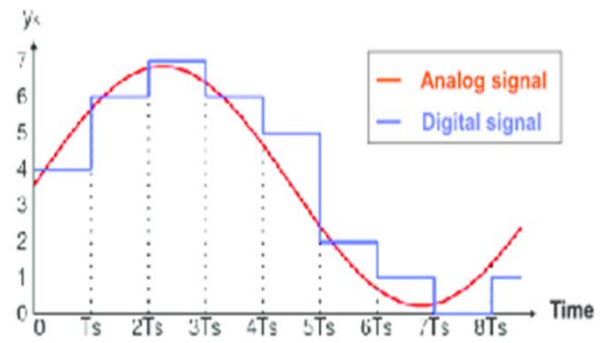
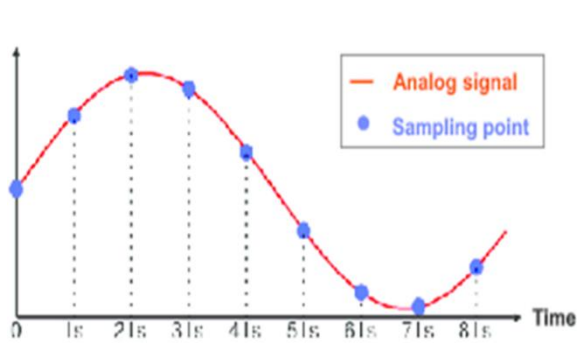
##### **QUANTIZATION-**

Quantization refers to the process of approximating the continuous set of values with a finite set of values. The input to a quantizer is the original data and the output is always one among a finite number of levels.

The analog and digital converters perform this type of function to create a series of digital values out of the analog signal. The quantizing of an analog signal is done by discretizing the signal with a number of quantization levels.

Samples taken are assigned numeric values that the digital circuit can use in a process called quantization. When a sample is quantized, the instantaneous value of its analog amplitude has to be rounded off to the nearest available digital value. This rounding off process is called approximation.





A quantizer can be specified by its input partitions and output levels. If the input range is divided into levels of equal spacing, then the quantizer is termed as a uniform quantizer and if not it is termed as a non-uniform quantizer.

A uniform quantizer can be specified easily by its lower bound and the step size. Also implementing a uniform quantizer is easier than a non-uniform quantizer. There are two types of uniform quantizer.

- 1) Mid rise type
- 2) Mid tread type

The **mid-rise type** is so called because the origin lies in the middle of a raising part of the stair case. The **mid tread type** is so called because the origin lies in the middle of a tread of stair case

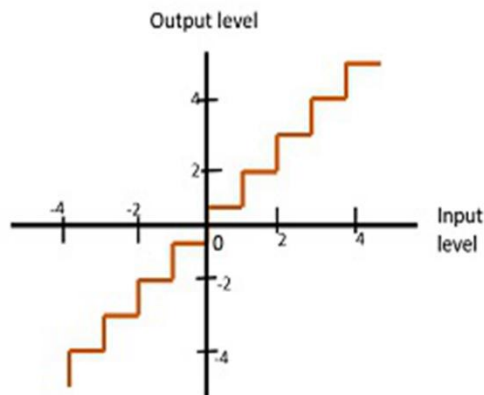


Fig 1 : Mid-Rise type Uniform Quantization

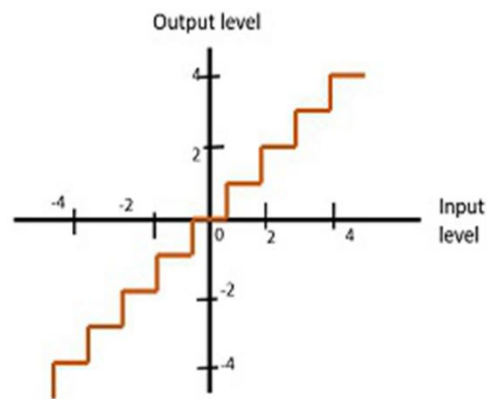


Fig 2 : Mid-Tread type Uniform Quantization

## Quantization error-

For any system, during its functioning there is always a difference in the values of its input and output. The processing of the system results in an error, which is the difference of those values. The difference between an input value and its quantized value is called a quantization error.

## Quantization Noise-

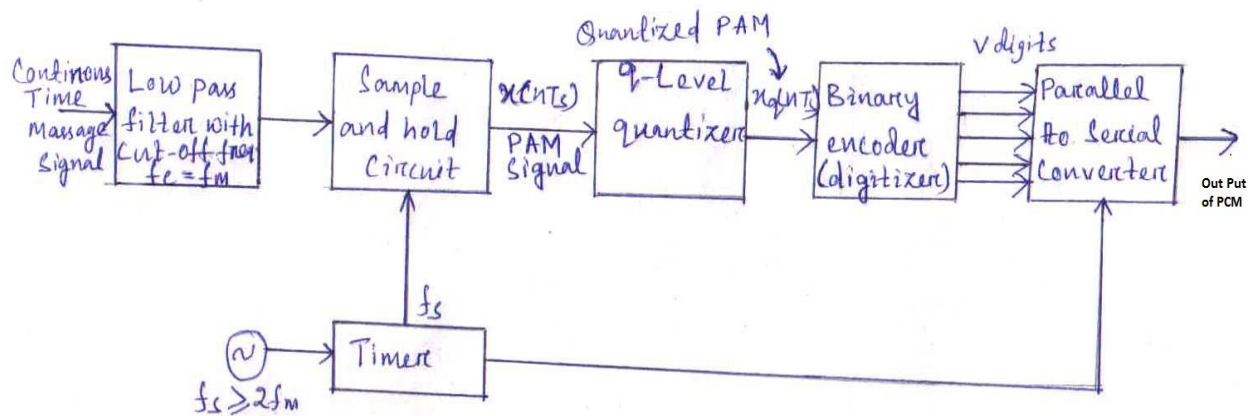
It is a type of quantization error, which usually occurs in an analog audio signal, while quantizing it to digital. For example, in music, the signals keep changing continuously where regularity is not found in errors. Such errors create a wideband noise called as quantization.

## 5.5 PULSE CODE MODULATION-

Pulse code modulation is known as a digital pulse modulation technique. The pulse code modulation is quite complex compared to the analog pulse modulation techniques.

A PCM system consists of 3 main parts i.e, transmitter, transmission path and receiver. The essential operations in the transmitter of a PCM system are sampling, quantizing and encoding. Sampling is the operation in which an analog signal is sampled according to the sampling theorem resulting in a discrete time signal. The quantizing and encoding operations are usually performed in same circuit which is known as an analog to digital converter. Also the essential operations in the receiver are regeneration of impaired signals, decoding and demodulation of the train of quantized samples.

### PCM GENERATION TRANSMITTER-



In PCM generator the signal  $x(t)$  is first passed through the low pass filter of cut off frequency  $f_m$  Hz. This low pass filter blocks all the frequency components which are lying above  $f_m$  Hz.

This means the signal  $x(t)$  is band limited to  $f_m$  Hz. The sample and hold circuit then samples this signal at the rate of  $f_s$ . Sampling frequency  $f_s$  is selected sufficiently nyquist rate to avoid aliasing i.e,

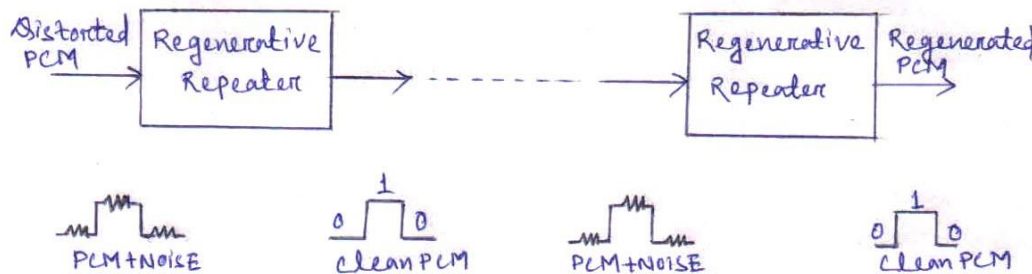
$$f_s \geq 2f_m$$

The output of sample and hold circuit is denoted by  $x(nT_s)$ . This signal  $x(nT_s)$  is discrete in time and continuous in amplitude. A Q-level quantizer compares input  $x(nT_s)$  with its fixed digital levels. It assigns any one of the digital level to  $x(nT_s)$  with its fixed digital level. It then assigns any one of the digital level to  $x(nT_s)$  which results in minimum distortion or error. This error is called quantization error. Thus output of quantizer is a digital level called  $x_q(nT_s)$ .

Now the quantized signal level  $x_q(nT_s)$  is given to binary encoder. This encoder converts input signal to 'v' digits binary word. Thus  $x_q(nT_s)$  is converted to 'v' binary bits. This encoder is also known as digitizer.

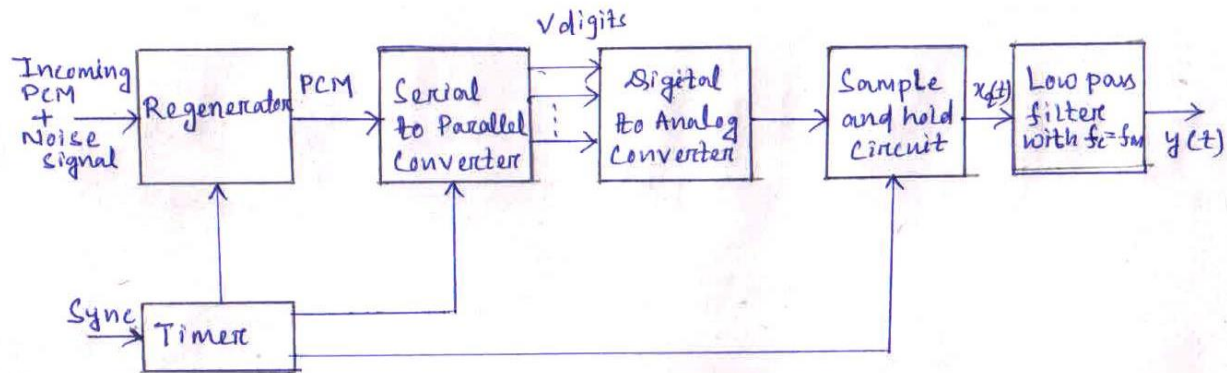
Also an oscillator generates the clocks for sample and hold circuit and parallel to serial converter. In the pulse code modulation generator, sample and hold, quantizer and encoder combinely form an analog to digital converter.

### **PCM TRANSMISSION PATH-**



The path between the PCM transmitter and PCM receiver over which the PCM signal travel, is called as PCM transmission path. The most important feature of PCM system lies in its ability to control the effects of distortion and noise when the PCM wave travels on the channel. PCM accomplishes this capacity by means of using a chain of regenerative repeaters. Such repeaters are spaced close enough to each other on the transmission path. The regenerative performs three basic operations namely equalization, timing and decision making. Hence each repeater actually reproduces the clean noise free PCM signal from the PCM signal distorted by the performance of PCM in presence of noise.

## DEMODULATION OF PCM-



In the above diagram regenerator at the start of PCM receiver reshapes the pulse and removes the noise. This signal is then converted to parallel digital words for each sample.

Now, the digital word is converted to its analog value denoted as  $x_q(t)$  with the help of a sample and hold circuit. This signal, at the output of sample and hold circuit, is allowed to pass through a low pass reconstruction filter to get the appropriate original message signal denoted as  $y(t)$ .

## 5.6 COMPANDING IN PCM & VOCODER

### COMPANDING-

Companding refers to a technique for compressing and expanding an analog or digital signal. It is a combination of the words compressing and expanding. In this process a voice signal is compressed, then changed from analog to digital in the transmitter and in receiver converted back from digital to analog before it is expanded again.

Companding helps to improve SNR of weak signals. As we know in non-uniform quantization, the step size varies according to the signal level. If the signal level is low then step size will be small. So, the step size will be low for weak signal. Thus the quantization noise will also be low.

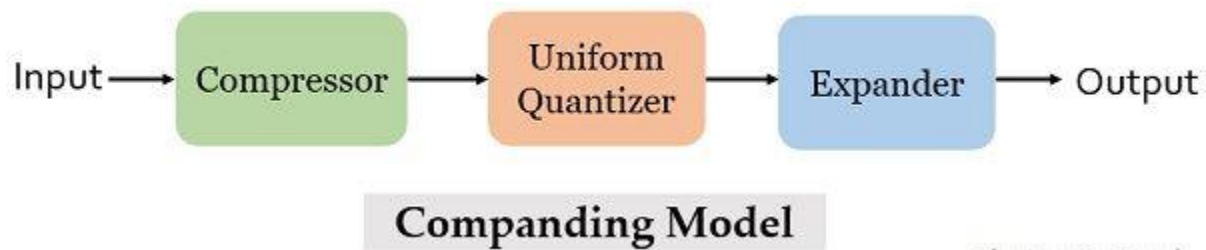
Quantization noise is given by:

$$N_q = \frac{\Delta^2}{12}$$

For uniform quantization  $\Delta$  is constant. So, for weak signal in uniform quantization the quantization noise increases. But in non-uniform quantization the step size decreases for weak signal. So, the quantization noise decreases. This will improve SNR.

## Model of Comping-

This model consists of a compressor, a uniform quantizer and an expander.



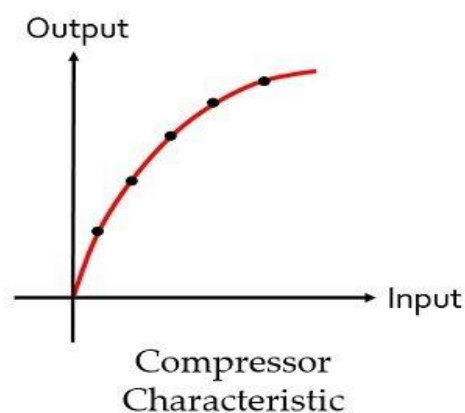
The signal is first given to the compressor. The compressor unit amplifies the weak signal in order to increase the signal level. While if the input signal is a strong signal then compressor attenuates that signal before providing it to the uniform quantizer.

This is done in order to have an appropriate signal level as the input to the uniform quantizer. High amplitude signal needs more bandwidth and also is more likely to distort. The output of the compressor is provided to uniform quantizer where the quantization of the applied signal is performed. At the receiver end the output of the uniform quantizer is fed to the expander.

It performs the reverse of the process executed by the compressor. This unit when receives a low value signal then it attenuates it, while if a strong signal is present then the expander amplifies it. This is done in order to get the originally transmitted signal at the output.

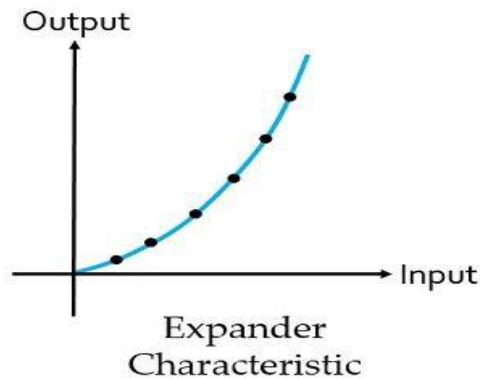
## Compressor Characteristic-

The graph clearly represent that the compressor provides amplification to weak signal and attenuates the high input signal.

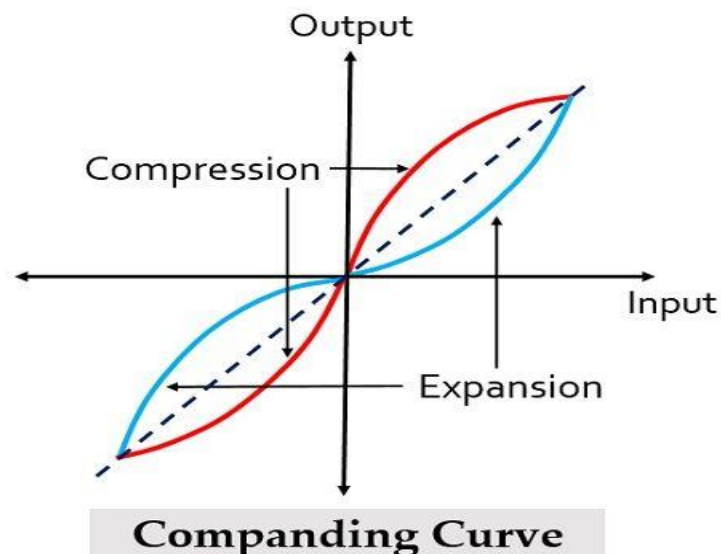


## Expander Characteristic-

Expander performs reverse operation of the compander. So, it is clear from the figure that expander provides amplification to strong signal and attenuates the low input signal.



The below one is the compander characteristics. This is the combined curve of compressor and expander. The dotted line represents the linear characteristic of the compander indicating that the originally transmitted signal is recovered at the receiver.



For digital audio signals, companding is used in pulse code modulation. The process involves decreasing the number of bits used to record the strongest signals. In the digital file format, companding improves the signal to noise ratio at reduced bit rates. For example, a 16 bit PCM signal may be converted to an eight bit signal.

### **VOCODER-**

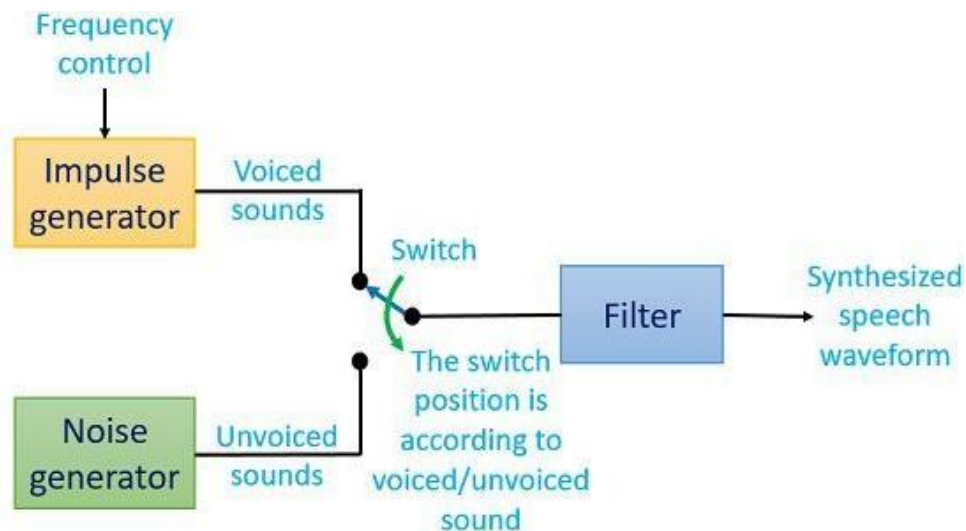
Vocoder is an audio processor that is used to transmit speech or voice signal in the form of digital data. The full form of vocoder is voice coder. Vocoders are used for digital coding of speech and voice simulation.

Vocoder operates on the principle of formants. Formants are the meaningful components of a speech that is generated due to the human voice. Whenever a speech signal is transmitted, it is not needed to transmit the precise waveform. We can

simply transmit the information by which one can reconstruct that particular waveform.

Vocoders are used for voice synthesis. The vocoder takes two signals and creates a third signal using the spectral information of the two input signals.

Speech model of vocoder-



A voice model is used to stimulate voice. As speech contains a sequence of voiced and unvoiced sounds. Voice sounds are the sounds generated by vibrations of the vocal cords. Unvoiced sounds are generated by expelling air through lips and teeth.

Voiced sounds are simulated by the impulse generator, the frequency of which is equal to the fundamental frequency of vocal cords. The noise source present in the circuit is used to simulate the unvoiced sounds. The position of the switch helps in determining whether the sound is voiced or unvoiced. Then the selected signal is passed through a filter that simulates the effect of mouth, throat and nasal passage of speaker.

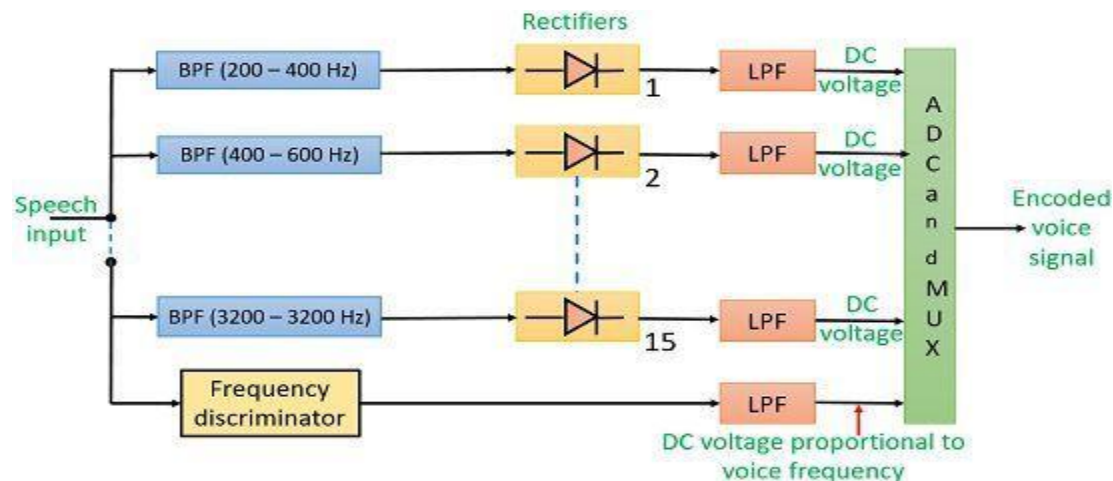
The filter unit then filters the input in such a way so as the required letter is pronounced. LPC is extensively used in case of speech and music application. Full form of LPC is Linear Predictive coding. This technique is used to predict the estimate future values. So, we can say, by analyzing two previous samples, it predicts the outcome. Vocoder is comprised of voice encoder and decoder.

### **Voice Encoder-**

The frequency spectrum of the speech signal is divided into 15 frequency ranges by using 15 band pass filter each having bandwidth range of 200Hz. The output of BPF acts as input for the rectifier unit. The signal is rectified and filtered so as to produce a dc voltage. This generated dc voltage is proportional to the amplitude of AC signal present at the output of the filter.



The input of the frequency discriminator is the speech signal. Frequency discriminator unit is followed by a low pass filter of 20 Hz. This low pass filter generates a dc voltage proportional to the voice frequency. The output at all the LPF's is DC voltage which is sampled, multiplexed and A/D converted. So, we have a digital equivalent of the speech signal at the output of the encoder. This encoded voice signal consists of frequency component from 200 Hz to 3200 Hz.

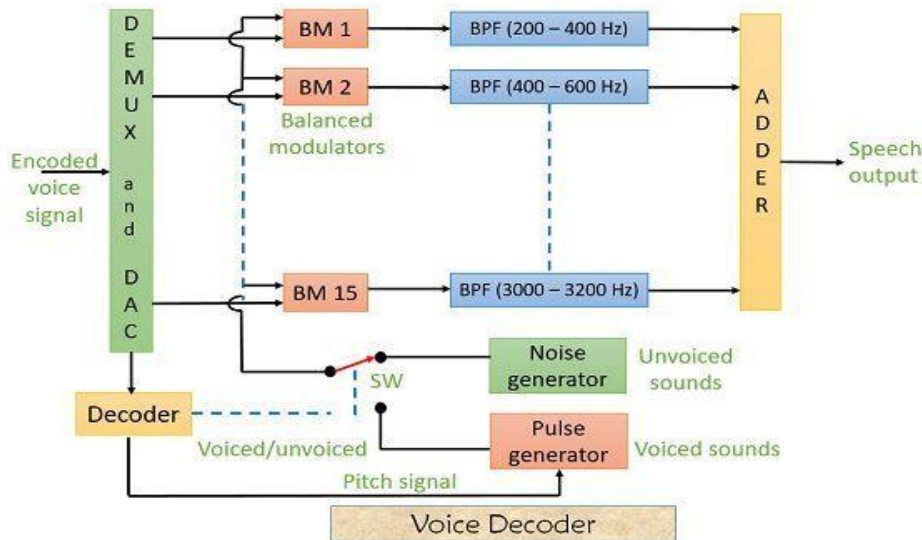


#### Voice Decoder-

The de-multiplexed and DAC section convert the received encoded signal back to its analog form. Here a balanced modulator- filter combination is used in correspondence to rectifier- filter combination at the encoder. The carrier to this balanced modulator is either the output of noise generator or pulse generator.

But this depends on the position of the switch. The switch position is decided by the decoder because when the voiced signal is received, the switch connects the pulse generator output to the input of all the balanced modulator. When an unvoiced signal is received the switch connects noise generator output to the input of all the balanced modulator.

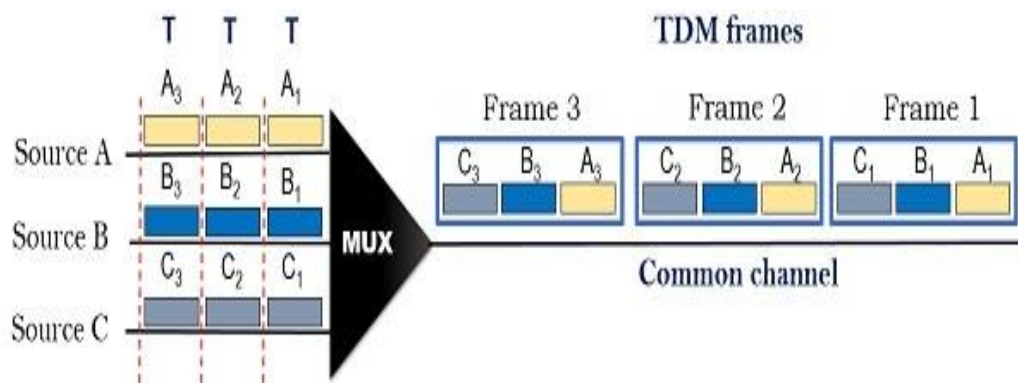
The adder will thus add up all the analog signal and produce voice or speech output. Speech transmission using vocoder is helpful technique but it has a disadvantage. This is because it leads to degradation in speech quality.



## 5.7 TDM-

Multiplexing is a technique in which multiple data signals can be transmitted over a single communication channel. In which multiplexing technique data signals are transmitted over a single channel in different timeslots is known as Time Division Multiplexing.

One may need to differentiate between the various signals for proper data transmission. So, in TDM the complete signal gets transmitted by occupying different time slots.



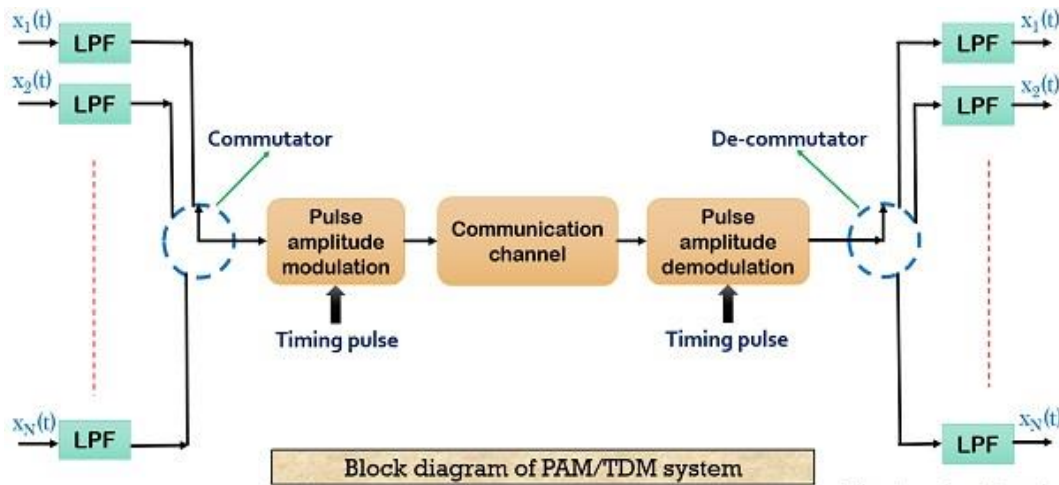
In the above diagram source A, B and C wants to transmit data through a common medium. Thus the signal from the 3 sources is divided into multiple segments each having their fixed time slots.

In this diagram we can see each signal divided into 3 segments. So by taking one segment from each source the multiplexer forms one frame. So, here 3 frames are formed. As these segments are entirely different from each other thus the chances of unnecessary signal mixing can be eliminated. When a frame gets transmitted over the

particular time slot, the next frame uses the same channel to get transmitted and the process is repeated until the completion of the transmission.

Here, we have taken the example of 3 different sources, but one can perform multiplexing of  $n$  source signals. Both analog and digital signals can be multiplexed using TDM, but its processing technique allows the multiplexing of digital signals.

TDM System-



This is a diagram of TDM system using PAM technique. Here at the beginning, the system consists of multiple LPF depending on the number of data inputs. These LPF are basically anti-aliasing filters that eliminate the aliasing of the data input signal.

The output of the LPF is then fed to the commutator. As per the rotation of the commutator the samples of the data inputs are collected by it. Here  $f_s$  is the rate of rotation of the commutator. Commutator perform the function of multiplexing. After that modulation is done and transmitted.

At the receiving end, a de-commutator is placed that is synchronized with the commutator at the transmitting end. This de-commutator separates the time division multiplexed signal at the receiving end. The commutator and de-commutator must have same rotational speed in order to get proper de-multiplexed signal at the receiving end.

After that signals given to the LPF and original data is recovered. In TDM

$$f_s \geq 2f_m$$

Thus the time duration in between successive sample is given as,

$$T_s = 1/f_s$$

We have considered that one can use this for 'n' input channels, then one sample is collected from each of the 'n' signals. Each frame will provide us with N samples and the spacing between the two is given as  $T_s/N$ .

Pulse frequency means the no. of pulses per second is also known as signaling rate denoted as 'r'.

$$r = 1 / \text{Spacing between 2 samples}$$

$$= \frac{1}{T_s/N}$$

$$= N / T_s = \frac{N}{1/f_s} = N f_s$$

The technique of time division multiplexing can be implemented in two ways.

- 1) Synchronous TDM
- 2) Asynchronous TDM

### 1) Synchronous TDM-

In this technique, the time slots are assigned at the beginning. This leads to the wastage of the capacity. As in the absence of any data unit, that particular time slot gets entirely wasted.



**Synchronous TDM**

### 2) Asynchronous TDM-

It eliminates the drawback of wastage of time slot present in synchronous TDM. Here a particular frame is transmitted by the transmitting end only when it gets completely filled by the data units. It exhibits higher efficiency than that of synchronous TDM. It allocates time slots as per demand

Application-

TDM mainly used in digital communication system i.e, in cellular radio and in satellite communication system.

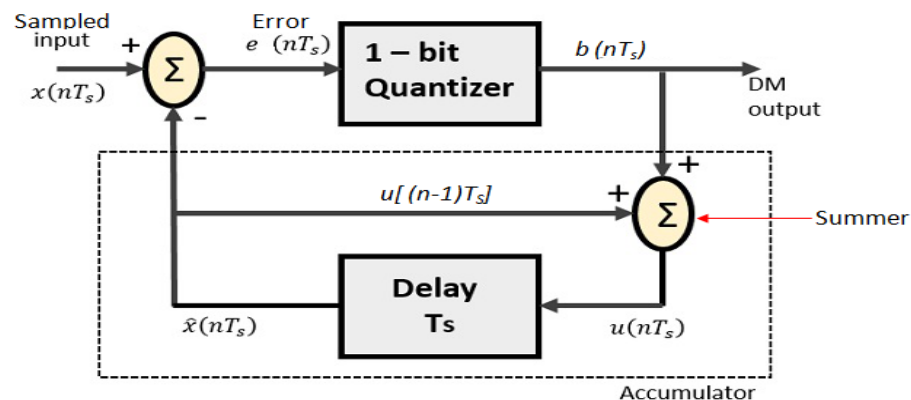
## **5.8 DELTA MODULATION-**

The sampling rate of a signal should be higher than the Nyquist rate, to achieve better sampling. If this sampling interval in DPCM is reduced considerably, the sample to sample amplitude difference is 1 bit quantization, then the step size will be very small i.e,  $\Delta$ .

The type of modulation, where the sampling rate is much higher and in which the step size after quantization is of a smaller value  $\Delta$ , such a modulation is termed as delta modulation. Delta modulation is a simplified form of DPCM technique, also viewed as 1 bit DPCM scheme. As the sampling interval is reduced the signal correlation will be higher.

Transmitter-

- Delta modulation transmits only one bit per sample. Here, the present sample value is compared with the previous sample value and this result whether the amplitude is increased or decreased is transmitted.
- Input signal  $x(t)$  is approximated to step signal by the delta modulator. This step size is kept fixed.
- The difference between the input signal  $x(t)$  and staircase approximated signal is confined to two levels, i.e.,  $+\Delta$  and  $-\Delta$ .
- Now, if the difference is positive, then approximated signal is increased by one step, i.e., ' $\Delta$ '. If the difference is negative, then approximated signal is reduced by ' $\Delta$ '.
- When the step is reduced, '0' is transmitted and if the step is increased, '1' is transmitted.
- Hence, for each sample, only one binary bit is transmitted.



The error between the sampled value of  $x(t)$  and last approximated sample is given as  $e(nTs) = x(nTs) - \hat{x}(nTs)$ .

$e(nTs)$  = error at present sample

$x(nTs)$  = sampled signal of  $x(t)$

$\hat{x}(nTs)$  = last sample approximation of the stair case waveform

if we assume  $u(nTs)$  as the present sample approximation of staircase output, then  $u(n-1)Ts = \hat{x}(nTs)$

Depending on the sign of error  $e(nTs)$ , the sign of step size  $\Delta$  is decided. In other words, we can write

$b(nTs) = +\Delta$  if  $x(nTs) \geq \hat{x}(nTs)$

$-\Delta$  if  $x(nTs) < \hat{x}(nTs)$

Also if  $b(nT_s) = +\Delta$  then a binary '1' is transmitted and if  $b(nT_s) = -\Delta$  then a binary '0' is transmitted.

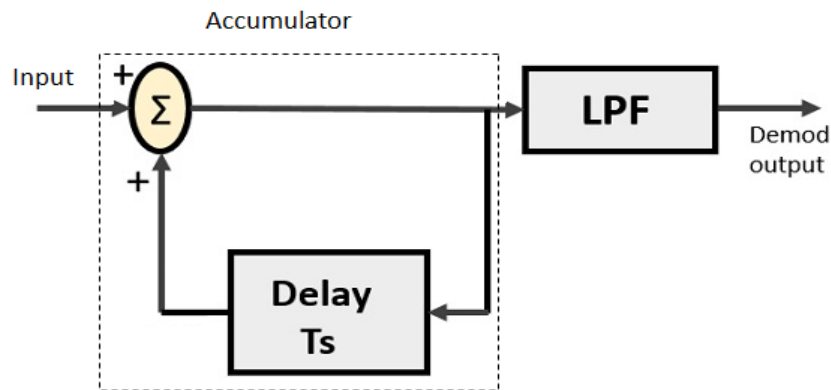
The summer in the accumulator adds quantizer output with the previous sample approximation. This gives present sample approximation i.e.,

$$u(nT_s) = u(nT_s - T_s) + \pm\Delta$$

$$u(nT_s) = u(n-1)T_s + b(nT_s)$$

The previous sample approximation  $u(n-1)T_s$  is restored by delaying one sample period  $T_s$ . The sampled input signal  $x(nT_s)$  and staircase approximation signal  $u(nT_s)$  are subtracted to get error signal  $e(nT_s)$ .

Receiver-



- The delta demodulator comprises of a low pass filter, a summer, and a delay circuit. The predictor circuit is eliminated here and hence no assumed input is given to the demodulator.
- The accumulator generates the staircase approximated signal output and is delayed by one sampling period  $T_s$ .
- It is then added to the input signal.
- If the input is binary '1' then it adds  $+\Delta$  step to the previous output (which is delayed).
- If the input is binary '0' then one step ' $\Delta$ ' is subtracted from the delayed signal.
- The low pass filter smoothens the staircase signal to reconstruct the original message signal  $x(t)$ .

Advantages and disadvantages-

Advantages-

- 1) It transmits only one bit for one sample.
- 2) The transmitter and receiver implementation is very much simple.

Disadvantages-

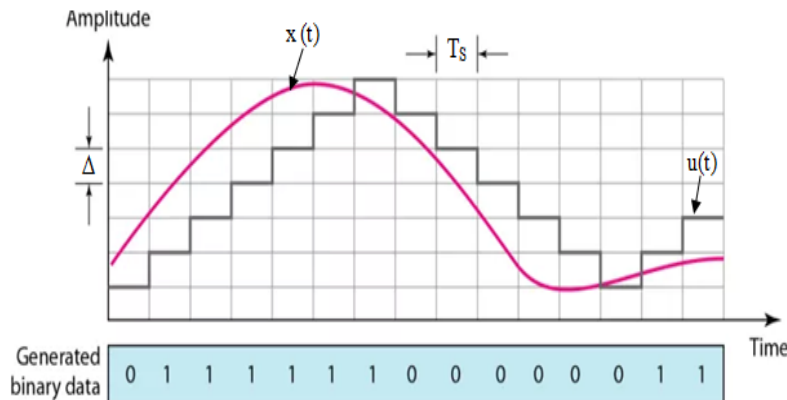
### 1) Slope overload distortion-

When the rate of rise of input signal  $x(t)$  is so high that the staircase signal cannot approximate it, the step size  $\Delta$  becomes too small for staircase signal  $u(t)$  to follow the step segment of  $x(t)$ . Here, there is a large error between the staircase approximated

signal and the original input signal  $x(t)$ . this error is known as slope overload distortion. To reduce this error, the step size must be increased when slope of signal  $x(t)$  is high.

## 2) Granular noise-

Granular noise occurs when the step size is too large compared to small variations in the input signal. This means that for very small variations in the input signal, the staircase signal is changed by large amount because of large step size. The error between the input and approximated signal is called granular noise. The solution to this problem is to make step size small.

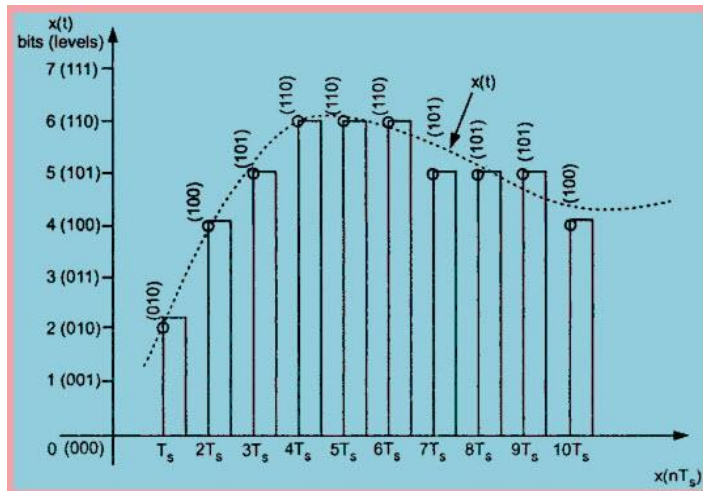


## 5.9 GENERATION & DEMODULATION OF DPCM-

We can observe that samples of a signal are highly correlated with each other. This is due to the fact that any signal does not change fast means values from present sample to next sample does not vary by a large amount. The adjacent samples of the signal carry the same information or with a little difference.

When these samples are encoded by a PCM system, the resulting encoded signal contains some redundant information.





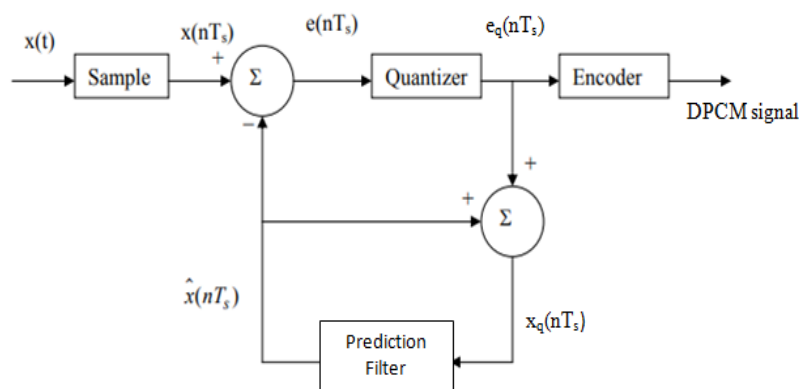
In this diagram dotted line represent the continuous time signal  $x(t)$ . This signal is sampled by flat top sampling at intervals  $T_s, 2T_s, 3T_s, \dots, nT_s$ . The sampling frequency is selected higher than nyquist rate. Here the samples are encoded by using 3 bit. The sample is quantized to the nearest digital level.

Here we can observe that the samples taken at  $4T_s, 5T_s$  and  $6T_s$  are encoded to same value i.e, 110. This information can be carried only by one sample. But three samples are carrying the same information means that it is redundant.

If this redundancy is reduced, then overall bit rate will decrease. This type of digital pulse modulation is called as Differential Pulse Code Modulation (DPCM).

The DPCM works on the principle of prediction. The value of the present sample is predicted from the past samples. The prediction may not be exact but it is very close to the actual sample value.

### DPCM Transmitter-



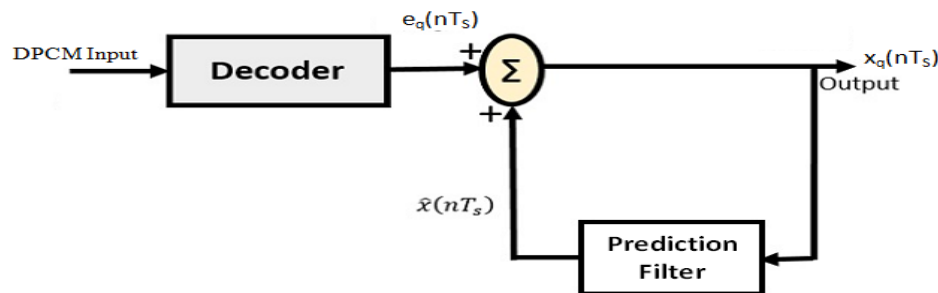
- The sampled signal is denoted by  $x(nT_s)$  and the predicted signal is indicated by  $\hat{x}(nT_s)$ . The comparator finds out the difference between the actual sample value  $x(nT_s)$  and the predicted value  $\hat{x}(nT_s)$ . This is called signal error and it is denoted as  $e(nT_s)$ .

$$e(nT_s) = x(nT_s) - \hat{x}(nT_s)$$

- Here the predicted value  $\hat{x}(nT_s)$  is produced by using a prediction filter.
- The quantizer output signal  $e_q(nT_s)$  and the previous prediction is added and given as input to the prediction filter, this signal is denoted by  $x_q(nT_s)$ . This makes the prediction closer to the actually sampled signal. The quantized error signal  $e_q(nT_s)$  is very small and can be encoded by using a small number of bits. Thus the number of bits per sample is reduced in DPCM.

### DPCM Receiver-

- In order to reconstruct the received digital signal, the DPCM receiver consists of a decoder and prediction filter.
- The input given to the decoder is processed and that output is summed up with the output of the predictor, to obtain better output. That means here first of all the decoder will reconstruct the quantized form of the original signal.
- Therefore the signal at the receiver differs from the actual signal by quantization error  $q(nT_s)$ , which is introduced permanently in the reconstructed signal.



## 5.10 COMPARISON BETWEEN PCM, DM, ADM AND DPCM-



S.NO	Parameter of Comparison	Pulse Code Modulation (PCM)	Delta Modulation (DM)	Adaptive Delta Modulation (ADM)	Differential Pulse Code Modulation (DPCM)
1.	Number of bits	It can use 4, 8, or 16 bits per sample.	It uses only one bit for one sample	It uses only one bit for one sample	Bits can be more than one but are less than PCM.
2.	Levels and step size	The number of levels depends on number of bits. Level size is fixed.	Step size is kept fixed and cannot be varied.	According to the signal variation, step size varies.	Number of levels is fixed.
3.	Quantization error and distortion	Quantization error depends on number of levels used.	Slope overload distortion and granular noise are present.	Quantization noise is present but other errors are absent.	Slope overload distortion and quantization noise is present.
4.	Transmission bandwidth	Highest bandwidth is required since numbers of bits are high.	Lowest bandwidth is required.	Lowest bandwidth is required.	Bandwidth required is less than PCM.
5.	Feedback	There is no feedback in transmitter or receiver.	Feedback exists in transmitter.	Feedback exists.	Feedback exists.
6.	Complexity of Implementation	System is complex.	Simple	Simple	Simple